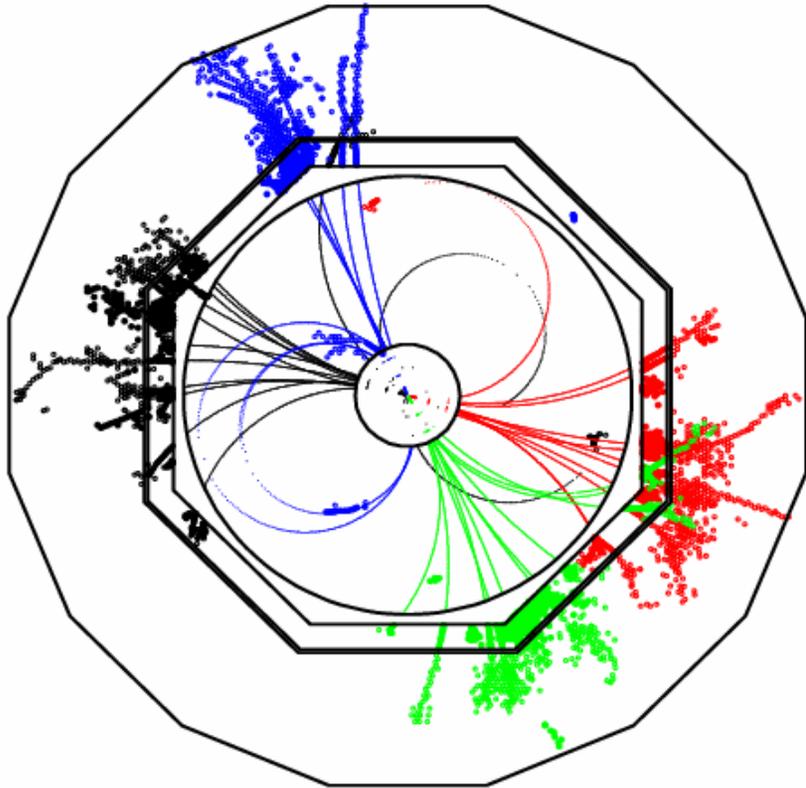


# Particle Flow Calorimetry

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University of Cambridge



## This Talk:

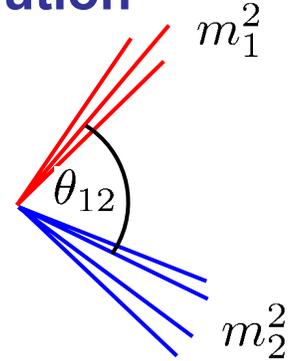
- ① Calorimetry at the ILC
- ② The Particle Flow Paradigm
- ③ The ILD Detector Concept
- ④ PandoraPFA
- ⑤ Particle Flow at the ILC
- ⑥ Particle flow at CLIC
- ⑦ CLIC Detector Considerations
- ⑧ Conclusions

# 1 Calorimetry at the ILC

★ Aim for jet energy resolution giving di-jet mass resolution similar to Gauge boson widths

★ For a pair of jets have:

$$m^2 = m_1^2 + m_2^2 + 2E_1E_2(1 - \beta_1\beta_2 \cos \theta_{12})$$



★ For di-jet mass resolution of order  $\Gamma_{W/Z}$

$$\frac{\sigma_m}{m} \approx \frac{2.5}{91.2} \approx \frac{2.1}{80.3} \approx 0.027$$



$$\sigma_{E_j}/E_j < 3.8\%$$

+ term due to  $\theta_{12}$  uncertainty

★ What jet energies are we interested in ?

▪ Depends on **physics**

▪ **Not**  $E_{\text{jet}} = \sqrt{s}/2$

▪ **Interested in 4-6+ fermion final states**

$$\alpha(E_j) < 0.027 \sqrt{E_{jj}(\text{GeV})}$$

★ Typical di-jet energies at **500 GeV ILC: (50-150 GeV)**

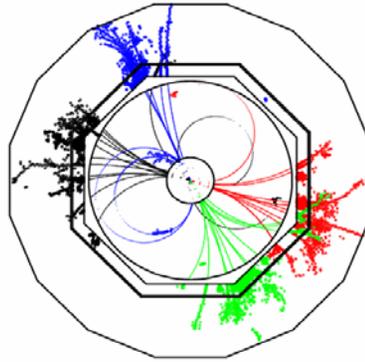
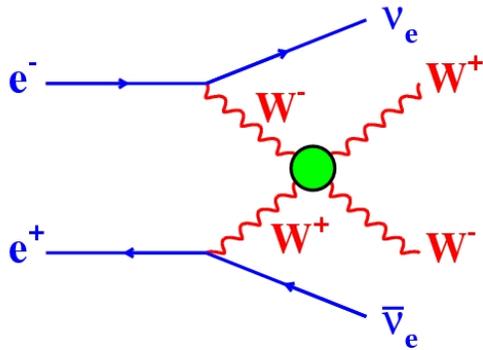
$$\sigma_E/E < 0.20/\sqrt{E_{jj}(\text{GeV})} - 0.33/\sqrt{E_{jj}(\text{GeV})}$$

★ Typical di-jet energies at **1 TeV ILC: (100-300 GeV)**

$$\sigma_E/E < 0.27/\sqrt{E_{jj}(\text{GeV})} - 0.46/\sqrt{E_{jj}(\text{GeV})}$$

# Why is this important ?

★ Direct impact on physics sensitivity, e.g. “WW-scattering”

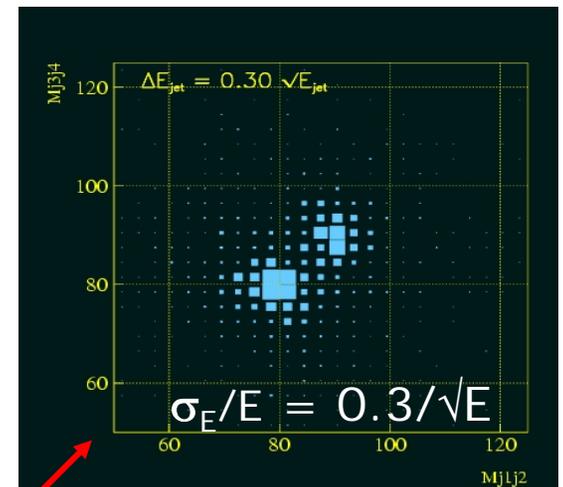
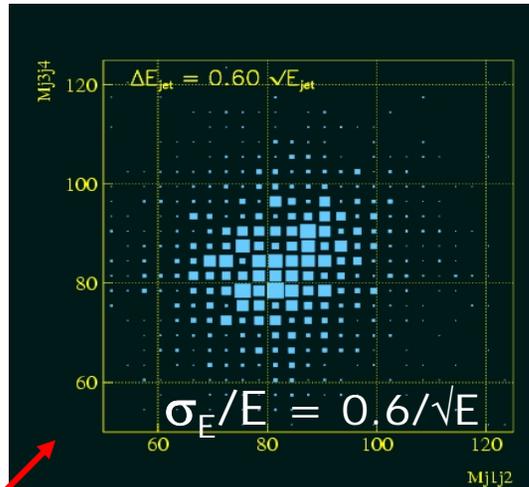


If the Higgs mechanism is not responsible for EWSB then WW fusion processes important

$$e^+e^- \rightarrow \nu\nu WW \rightarrow \nu\nu qqqq,$$

$$e^+e^- \rightarrow \nu\nu ZZ \rightarrow \nu\nu qqqq$$

Reconstruction of two di-jet masses allows discrimination of WW and ZZ final states



Best at LEP (ALEPH):  
 $\sigma_E/E = 0.6 (1+|\cos\theta_{jet}|) / \sqrt{E(\text{GeV})}$

ILC GOAL:  
 $\sigma_E/E \sim 0.3 / \sqrt{E(\text{GeV})}$

★ Want

$$\sigma_E/E < 0.30/\sqrt{E(\text{GeV})}$$

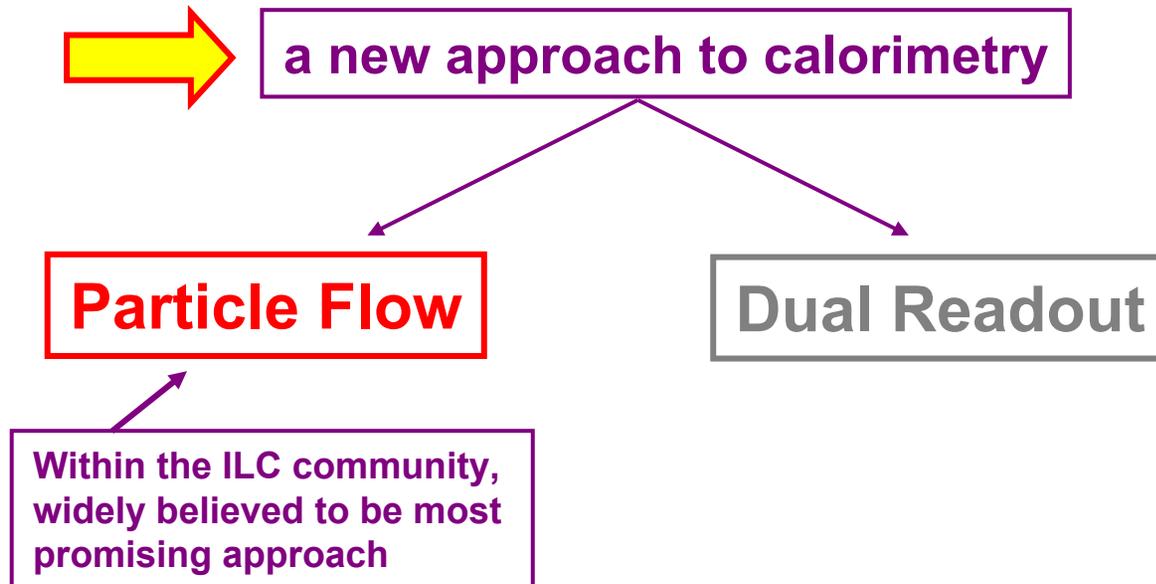
or more correctly

$$\sigma_E/E < 3.8\%$$

★ Unlikely to achieve this with a traditional approach to calorimetry

Remember this number

Limited by typical HCAL resolution of  $> 50\%/\sqrt{E(\text{GeV})}$



# 2 The Particle Flow Paradigm

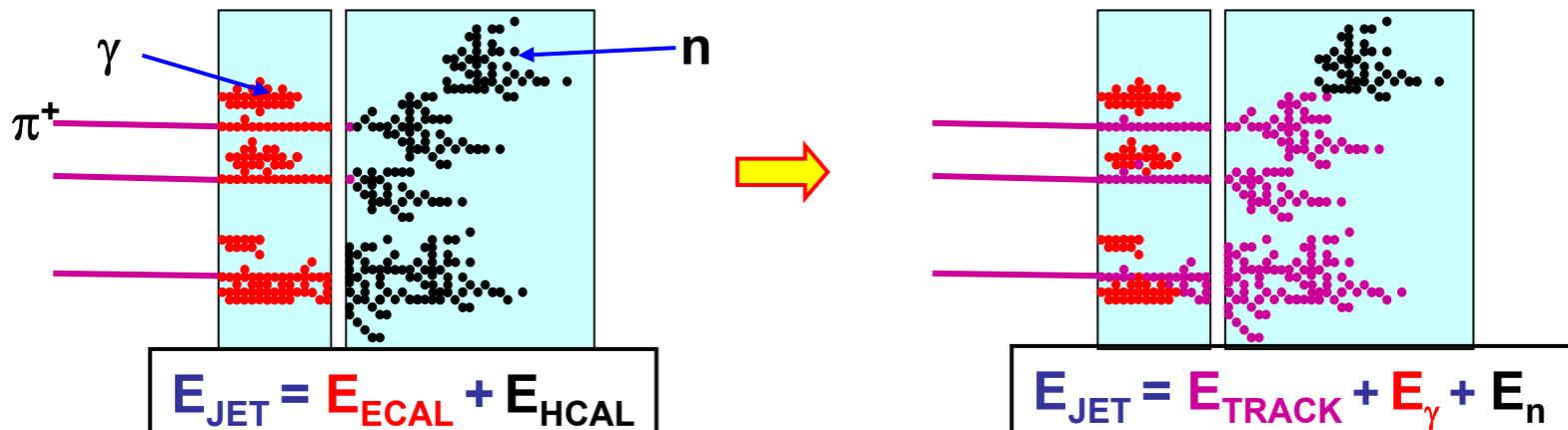
## ★ In a typical jet :

- ◆ 60 % of jet energy in charged hadrons
- ◆ 30 % in photons (mainly from  $\pi^0 \rightarrow \gamma\gamma$ )
- ◆ 10 % in neutral hadrons (mainly  $n$  and  $K_L$ )



## ★ Traditional calorimetric approach:

- ◆ Measure all components of jet energy in ECAL/HCAL !
- ◆ ~70 % of energy measured in HCAL:  $\sigma_E/E \approx 60\% / \sqrt{E(\text{GeV})}$
- ◆ Intrinsically “poor” HCAL resolution limits jet energy resolution



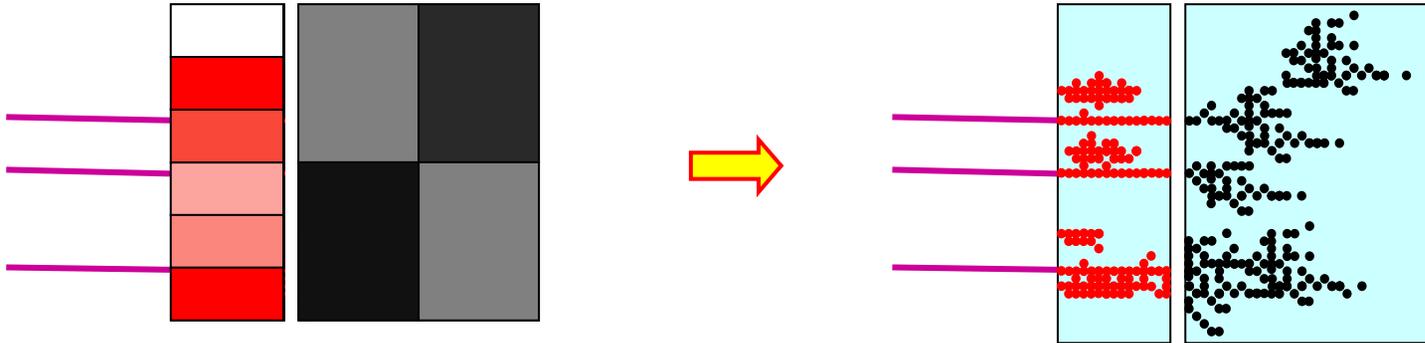
## ★ Particle Flow Calorimetry paradigm:

- ◆ charged particles measured in tracker (essentially perfectly)
- ◆ Photons in ECAL:  $\sigma_E/E < 20\% / \sqrt{E(\text{GeV})}$
- ◆ Neutral hadrons (ONLY) in HCAL
- ◆ Only 10 % of jet energy from HCAL  $\Rightarrow$  much improved resolution

# Particle Flow Calorimetry

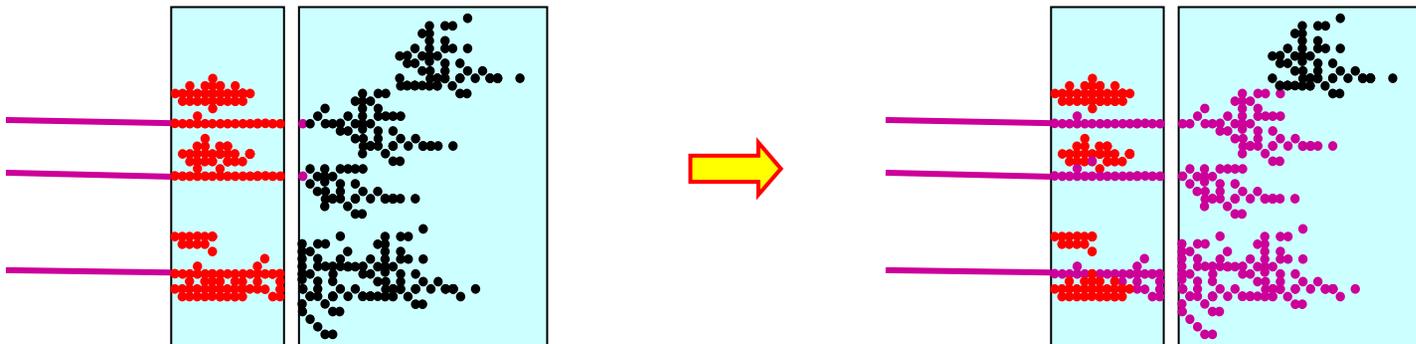
## Hardware:

- ★ Need to be able to resolve energy deposits from different particles
- ➔ **Highly granular detectors (as studied in CALICE)**



## Software:

- ★ Need to be able to identify energy deposits from each individual particle !
- ➔ **Sophisticated reconstruction software**



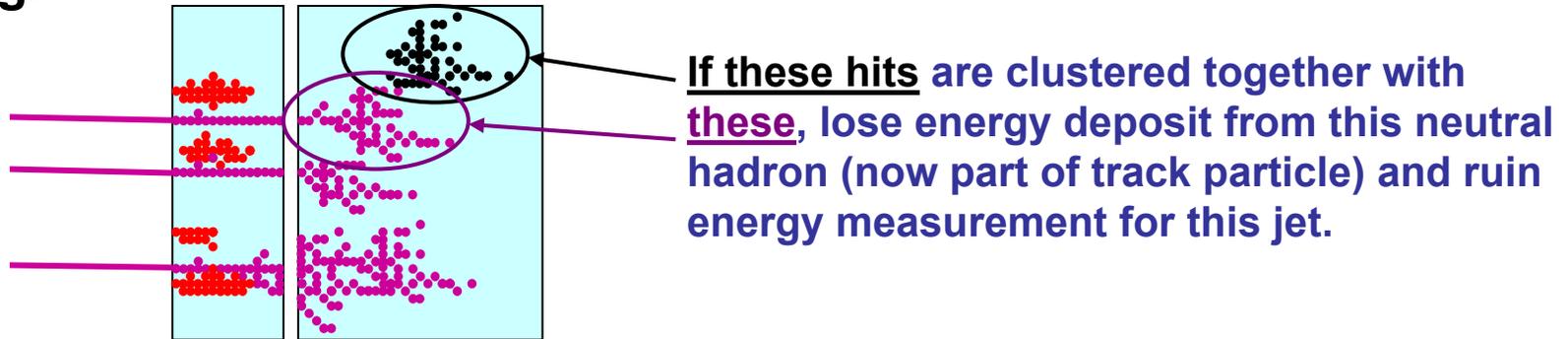
★ Particle Flow Calorimetry = **HARDWARE + SOFTWARE**

# Particle Flow Algorithms (PFA)

## Reconstruction of a Particle Flow Calorimeter:

- ★ **Avoid double counting of energy** from same particle
- ★ **Separate energy deposits** from different particles

e.g.



**Level of mistakes, “confusion”, determines jet energy resolution**  
**not the intrinsic calorimetric performance of ECAL/HCAL**

**sounds easy....**

- ★ **PFA performance** depends on detailed **reconstruction**
- ★ **Relatively new, still developing ideas**
- ★ **Studies need to be based on a sophisticated detector simulations**
  - **can't use fast simulation**

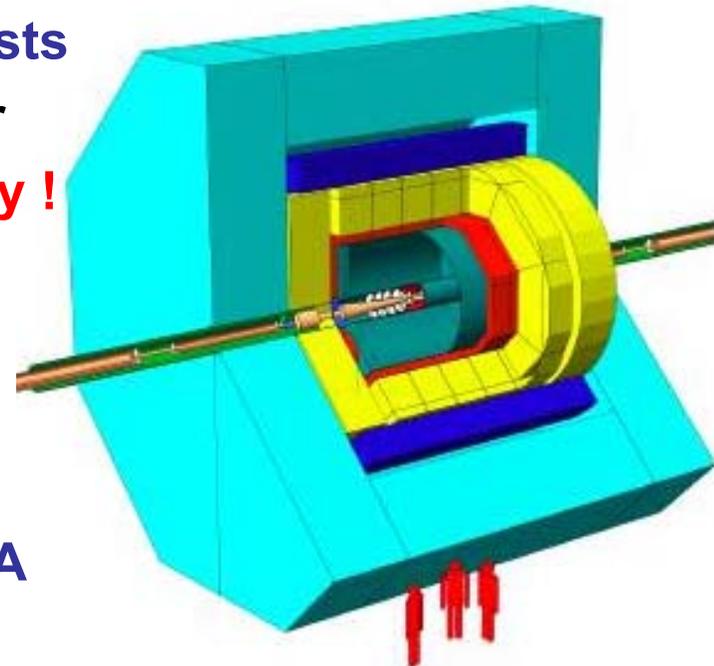
# ③ e.g. The ILD Detector Concept\*

## NOTE:

- ★ Particle flow reconstruction involves “whole detector”
- ★ To study potential performance need a detector model, tracking, calorimeters, ...

## ILC Detector Concepts:

- ★ Here performance of particle flow calorimetry shown in the context of the **ILD** detector concept for the **ILC**
- ★ Detailed GEANT 4 detector model exists
- ★ A potential design for an ILC detector
- ★ **Designed for Particle Flow calorimetry !**



## ILD Main Features:

- Large TPC central tracker ( $R=1.8$  m)
- CMS like solenoid ( $B = 3.5$  T)
- ECAL and HCAL inside solenoid
- ECAL/HCAL highly segmented for PFA

# ILD calorimetry concept\*

Very high longitudinal and transverse segmentation

## ECAL:

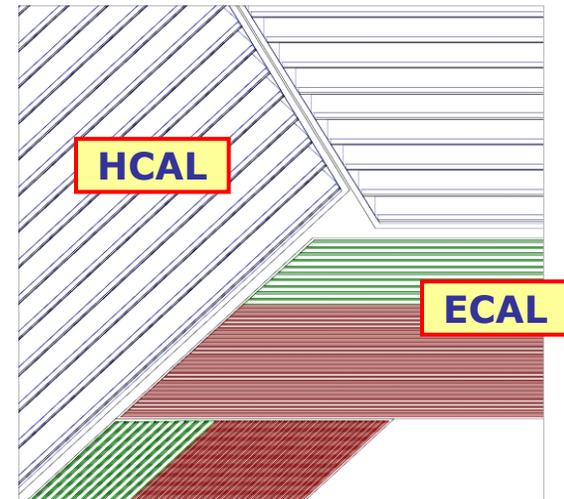
- SiW sampling calorimeter
- Tungsten:  $X_0/\lambda_{\text{had}} = 1/25$ ,  $R_{\text{Mol.}} \sim 9\text{mm}$ 
  - Narrow EM showers
  - longitudinal sep. of EM/had. showers
- longitudinal segmentation: 30 layers
- transverse segmentation:  $5 \times 5 \text{ mm}^2$  pixels

## HCAL:

- Steel-Scintillator sampling calorimeter
- longitudinal segmentation: 48 layers (6 interaction lengths)
- transverse segmentation:  $3 \times 3 \text{ cm}^2$  scintillator tiles

## Comments:

- ★ Technologically feasible (although not cheap)
- ★ Ongoing test beam studies (CALICE) see Nigel Watson's talk

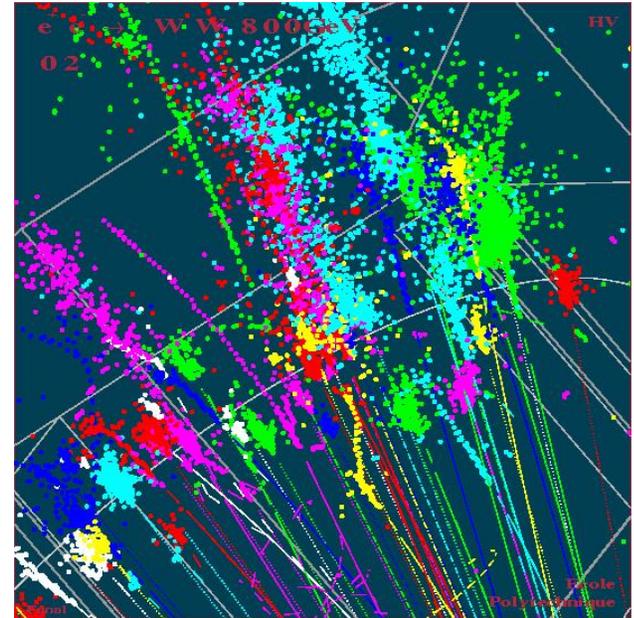


\*Other ILD calorimetry options being actively studied, e.g. RPC DHCAL, Scintillator strip ECAL

# Calorimeter Reconstruction

- ★ High granularity calorimeters – very different to previous detectors (except LEP lumi. calorimeters)
- ★ “Tracking calorimeter” – requires a new approach to ECAL/HCAL reconstruction

## Particle Flow Reconstruction



★ PFA calorimetric performance = HARDWARE + SOFTWARE

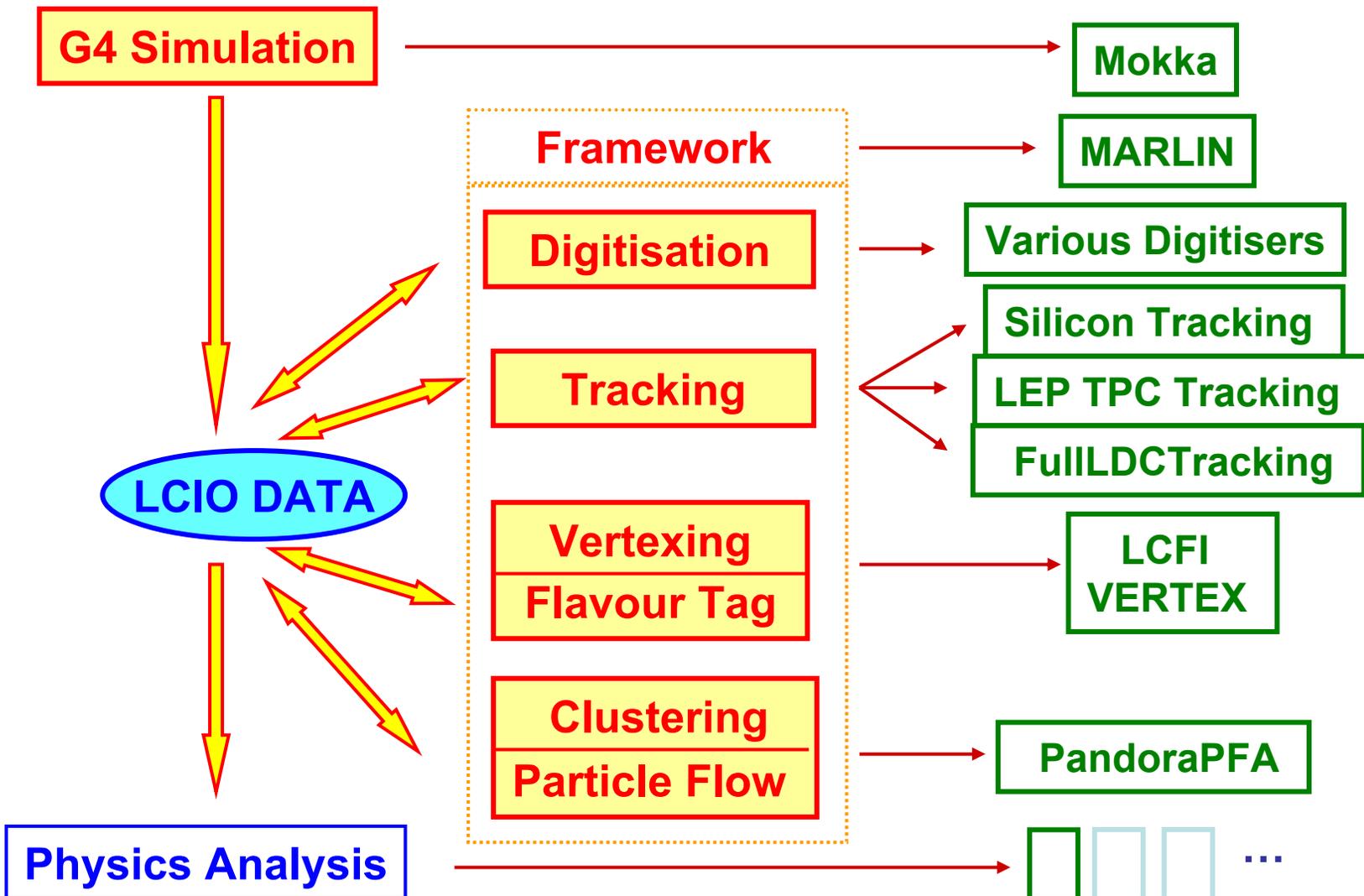
★ Performance will depend on the software algorithm

➡ difficult to evaluate full potential of particle flow  
 $\sigma_E/E = f(\text{software})$

To evaluate Particle Flow Calorimetry at ILC (or CLIC)  
need realistic reconstruction chain (PFA, tracking,...)

# ILD Reconstruction Framework (C++)

★ Everything exists – level of sophistication ~LEP experiment



# 4 The PandoraPFA Algorithm

This is **work-in-Progress** – currently best algorithm on market

- ★ ECAL/HCAL reconstruction and PFA performed in a single algorithm
- ★ Fairly generic algorithm
  - applicable to multiple detector concepts
- ★ Use **tracking** information to help **ECAL/HCAL** clustering
- ★ This is a sophisticated algorithm :  $\sim 10^4$  lines of code

## Eight Main Stages:

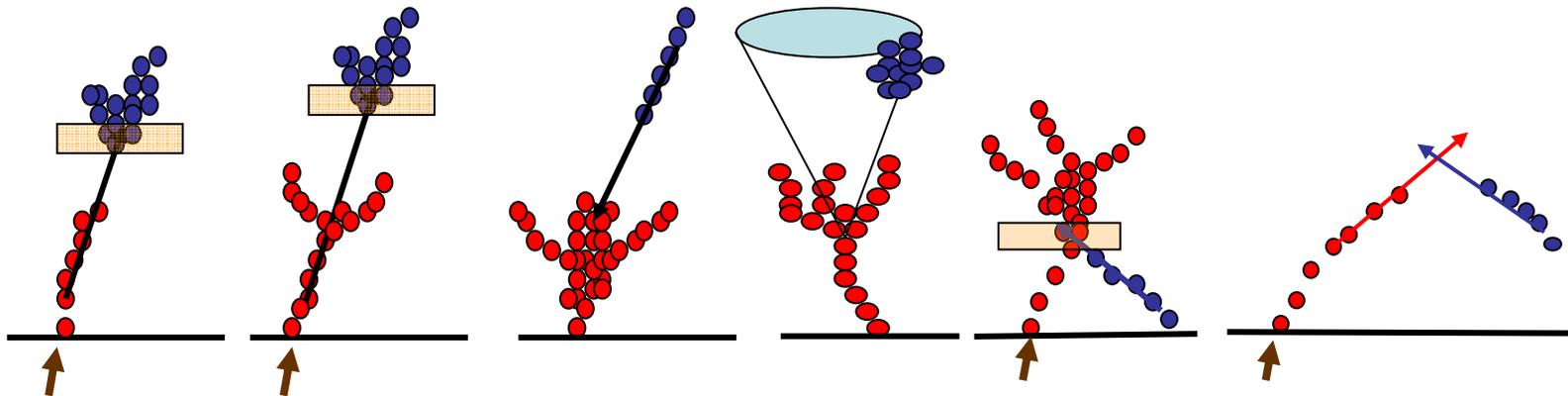
- i. Track classification/extrapolation
- ii. Loose clustering in ECAL and HCAL
- iii. Topological linking of clearly associated clusters
- iv. Coarser grouping of clusters
- v. Iterative reclustering
- vi. Photon Identification/Recovery
- vii. Fragment removal
- viii. Formation of final Particle Flow Objects  
(reconstructed particles)

# iii) Topological Cluster Association

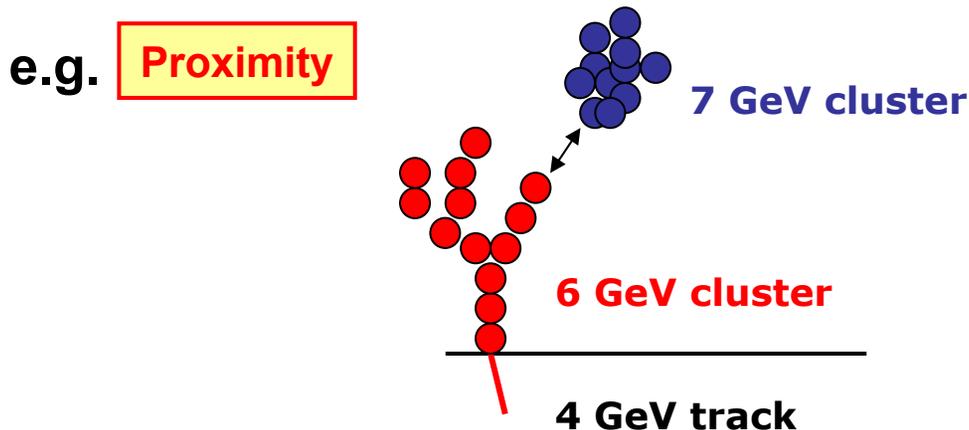
★ Clusters associated using a number of topological rules

## Clear Associations:

- Join clusters which are clearly associated making use of high granularity + tracking capability: **very few mistakes**



## Less clear associations:

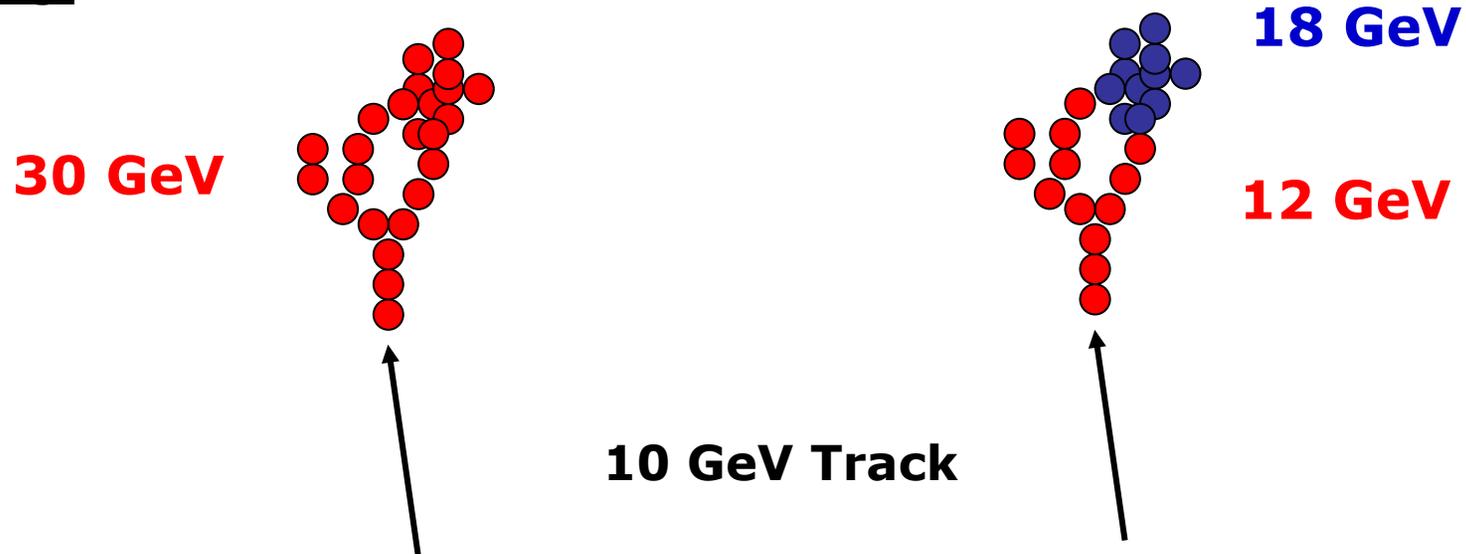


**Use E/p consistency  
to veto clear mistakes**

# v) Iterative Reclustering

★ If track momentum and cluster energy inconsistent : **RECLUSTER**

e.g.



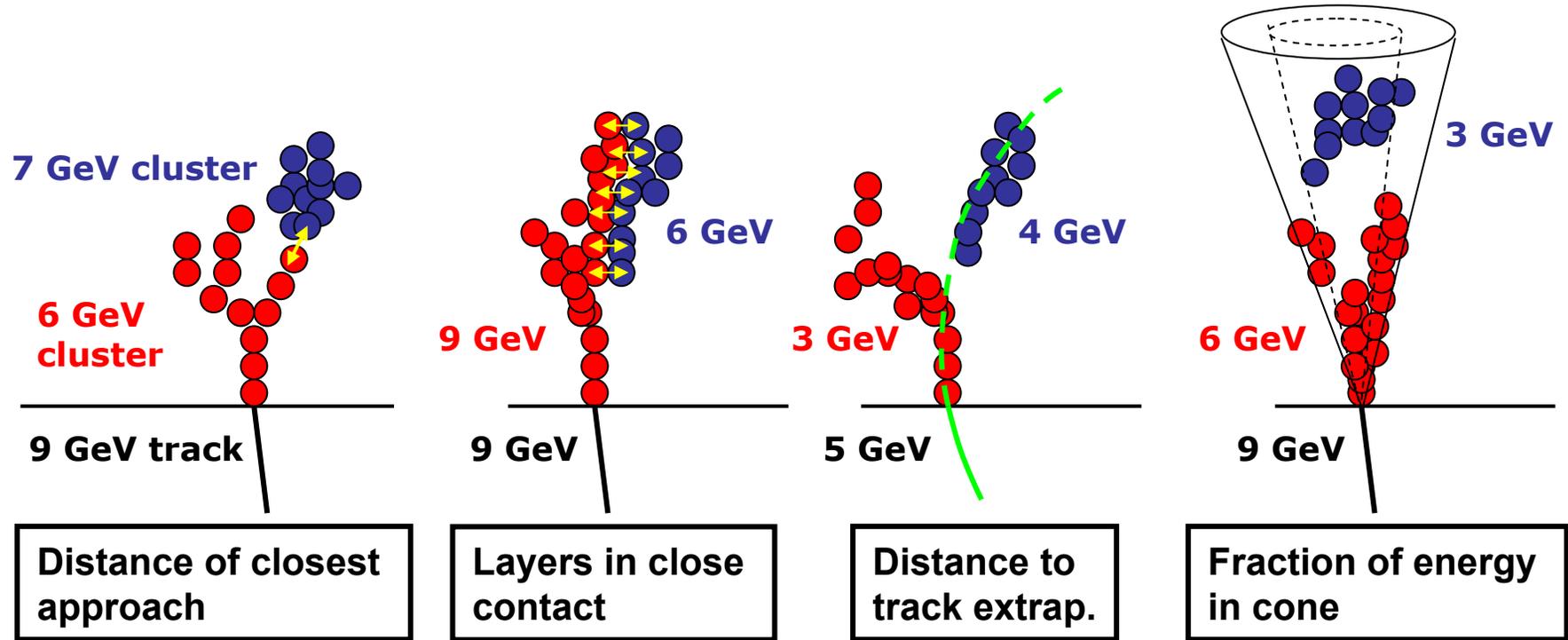
Change clustering parameters until cluster splits  
and get sensible track-cluster match

NOTE: clustering driven by track momentum (but not subtraction)

This is very important for higher energy jets

# viii) Fragment removal : basic idea

★ Look for “evidence” that a cluster is associated with another



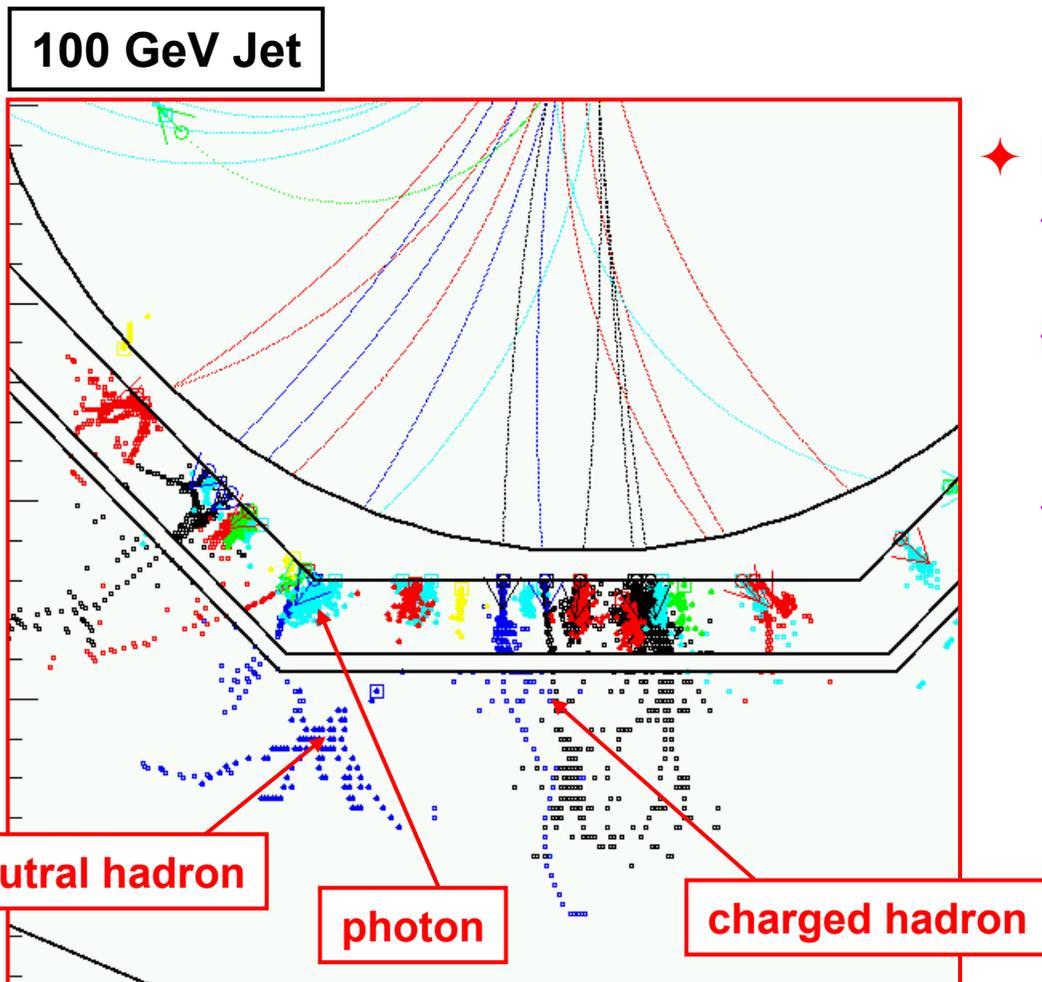
★ Convert to a numerical evidence score  $E$

★ Compare to another score “required evidence” for matching,  $R$ , based on change in  $E/p$  chi-squared, location in ECAL/HCAL etc.

★ If  $E > R$  then clusters are merged

★ Rather *ad hoc* but works well – but works well

# Putting it all together...

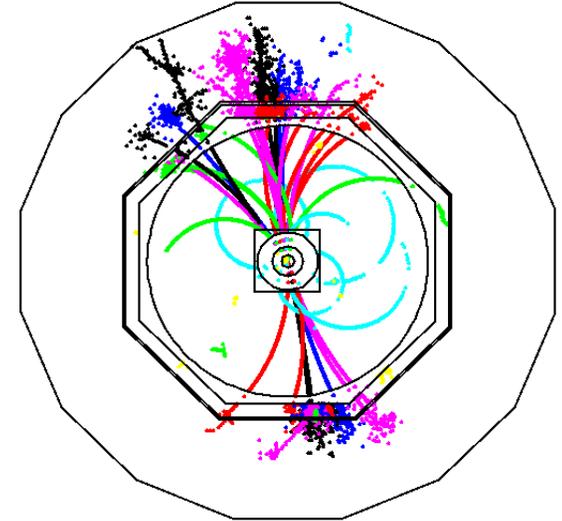


## ◆ If it all works...

- ◆ Reconstruct the **individual particles** in the event.
- ◆ Calorimeter energy resolution not critical: most energy in form of tracks.
- ◆ Level of mistakes in associating hits with particles, dominates jet energy resolution.

# 5 Particle Flow at the ILC

- ★ Benchmark performance using  $Z \rightarrow u\bar{u}$  and  $Z \rightarrow d\bar{d}$  events (clean, no neutrinos)
- ★ Test at for different energies with  $Z$  decays at rest
- ★ OPAL tune of Pythia fragmentation
- ★ Full reconstruction (track + calo) using no Monte Carlo “cheat” information

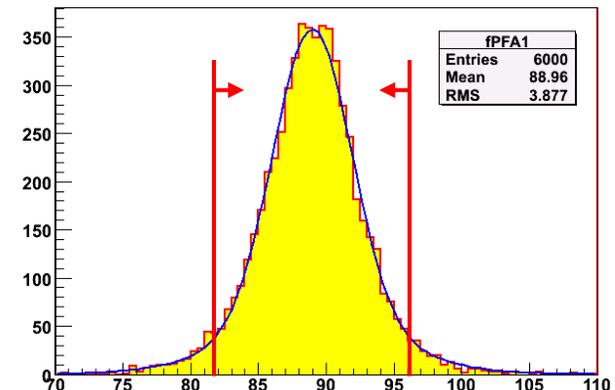


## NOTE:

- Quoting rms of reconstructed energy distribution is misleading
- Particle Flow occasionally goes very wrong → tails dominate rms
- Conventional to measure performance using **rms90** which is relatively insensitive to tails

**rms<sub>90</sub>**

- ★ Find smallest region containing 90 % of events
- ★ Determine rms in this region



## Performance (ILD) $Z \rightarrow d\bar{d}, Z \rightarrow u\bar{u}$

rms90

PandoraPFA v03- $\beta$

$E_{\text{JET}}$	$\sigma_E/E = \alpha/\sqrt{E_{jj}}$ $ \cos\theta  < 0.7$	$\sigma_E/E_j$
45 GeV	23.8 %	3.5 %
100 GeV	29.1 %	2.9 %
180 GeV	37.7 %	2.8 %
250 GeV	45.6 %	2.9 %

- Full G4 simulation
- “Realistic” detector, gaps etc.
- Full reconstruction

- ★ Particle flow achieves ILC goal of  $\sigma_E/E_j < 3.8 \%$
- ★ For lower energy jets Particle Flow gives **unprecedented** levels of performance, e.g. @ 45 GeV : 3.5% c.f. ~10% (ALEPH)
- ★ “Calorimetric” performance ( $\alpha$ ) degrades for higher energy jets
- ★ Current PFA code is not perfect – lower limit on performance

Proof of principle:

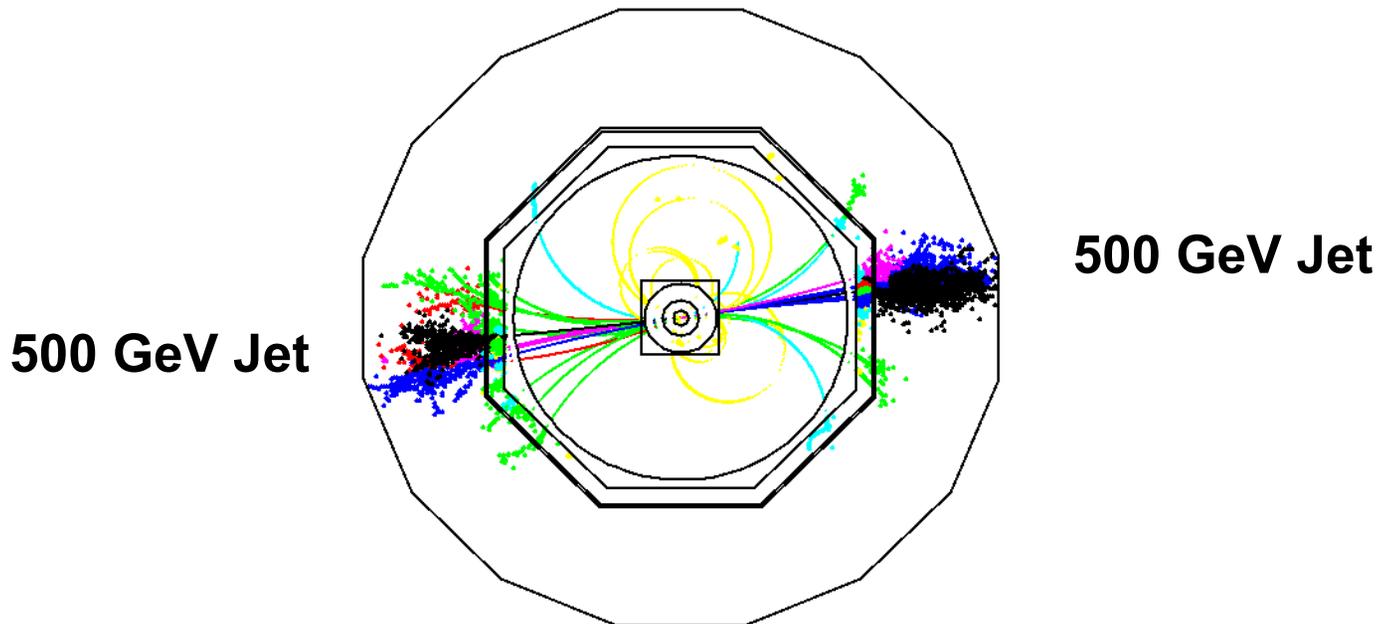
**PARTICLE FLOW CALORIMETRY WORKS**

At least in simulation

# ⑥ Particle Flow at CLIC

- ★ Particle Flow can deliver ILC jet energy goals
- ★ Detector concepts studied, and (partially) optimised  
e.g. **ILD**
- ★ What about Particle Flow for CLIC ?

STEP 1: take **ILD** and run...



# General Considerations

★ Traditional calorimetry  $\sigma_E/E \approx 60\% / \sqrt{E/\text{GeV}}$

★ Does not degrade significantly with energy (but leakage will be important at CLIC)

★ Particle flow gives **much better performance at “low” energies**

- very promising for ILC

What about at CLIC ?

★ PFA perf. degrades with energy

★ For 500 GeV jets, current alg. and ILD concept:

$$\sigma_E/E \approx 85\% / \sqrt{E/\text{GeV}}$$

★ Crank up field, HCAL depth...

$$\sigma_E/E \approx 65\% / \sqrt{E/\text{GeV}}$$

★ Algorithm not tuned for very high energy jets, so can probably do significantly better

63 layer HCAL ( $8 \lambda_1$ )  
B = 5.0 Tesla

rms90	PandoraPFA v03-β	
$E_{\text{JET}}$	$\sigma_E/E = \alpha/\sqrt{E_{jj}}$ $ \cos\theta  < 0.7$	$\sigma_E/E_j$
45 GeV	23.8 %	3.5 %
100 GeV	29.1 %	2.9 %
180 GeV	37.7 %	2.8 %
250 GeV	45.6 %	2.9 %
500 GeV	84.1 %	3.7 %
500 GeV	64.3 %	3.0 %

Conclude: for 500 GeV jets, PFA reconstruction not ruled out

★ For 1 TeV jets, particle flow will not give  $\sigma_E/E < 60\%/\sqrt{E/\text{GeV}}$   
(probably substantially worse)

★ This is probably not a problem for two reasons

i) Not interested in 1 TeV jets:

- ♦ most interesting physics likely to be 6, 8, ... fermion final states
- ♦ For 0.5 TeV jets, particle flow likely to be comparable or better than a traditional calorimetric approach

ii) A PFlow calorimeter still has good calorimetric resolution  
can design algorithm to move away from particle flow at higher energies



- ♦ Could be adapted on event, jet, locality basis
- ♦ Energy flow trivial to implement in PandoraPFA
- ♦ An adaptive algorithm should not be too difficult...

**But, a particle flow detector is expensive: possible to justify cost ?**

# Physics Considerations

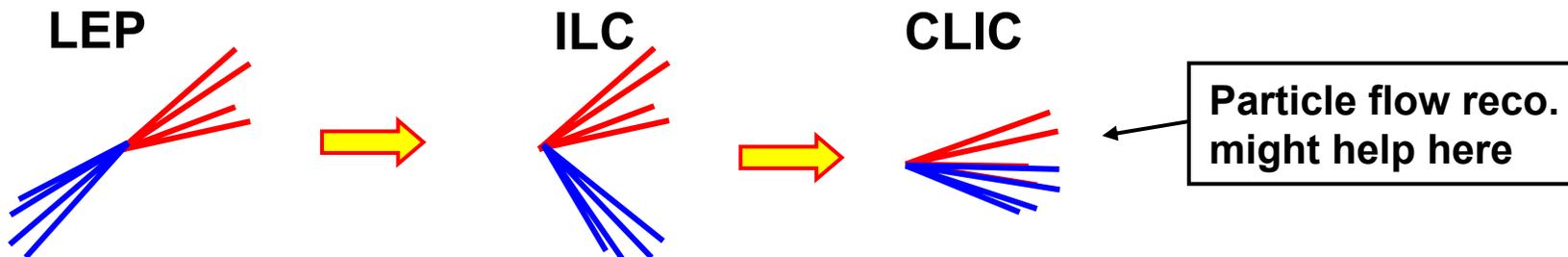
- ★ Whether particle flow is appropriate for a multi-TeV  $e^+e^-$  collider needs detailed study but depends on physics program, e.g.
  - ♦ **CLIC** is unlikely to operate solely at the highest energy
  - ♦ Likely to be a rich physics program below max. energy
    - lower  $\sqrt{s}$  to study Higgs, SUSY threshold scans, etc.
    - Here Particle Flow Calorimetry **highly desirable**

## For high energy running what are the calorimetry goals ?

- ★ For ILC reasonably well defined, wish to separate W/Z
- ★ For CLIC, less clear and again depends on **physics program**
- ★ What is most important:
  - direct reconstruction of high mass particles
    - What jet energy scale ? Not  $\sqrt{s}/2$
    - For 6 fermion final states **current** PFA already competitive (**ILD+**)
    - What mass resolution is needed ?
    - For 1TeV particle, e.g.  $X \rightarrow q\bar{q}$  decaying at rest **current PFA + ILD detector:** }  $\frac{\sigma_m}{m_X} \sim 2.7\%$
  - Missing transverse energy (i.e.  $p_T$ ) resolution ?
  - W/Z separation ?

# W/Z Separation at high Energies

★ On-shell W/Z decay topology depends on energy:



★ A few comments:

- Particle multiplicity does not change
- Boost means higher particle density
- PFA could be better for “mono-jet” mass resolution

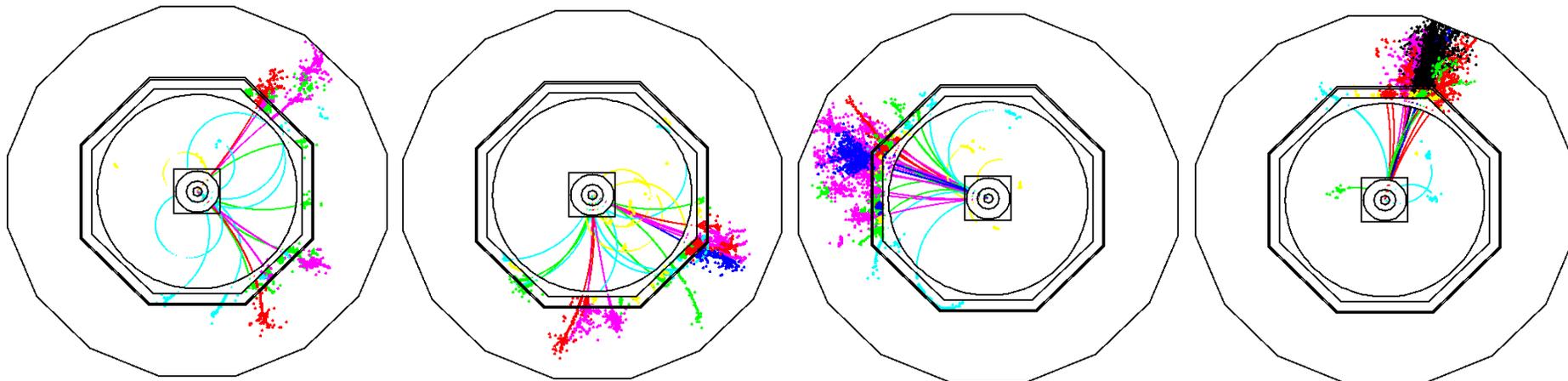
★ PandoraPFA + ILD performance studied for:

125 GeV Z

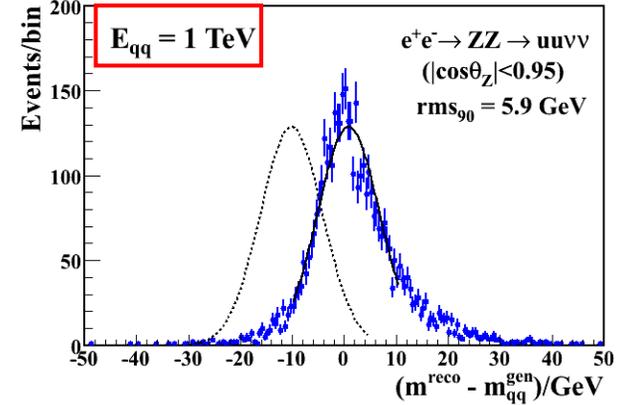
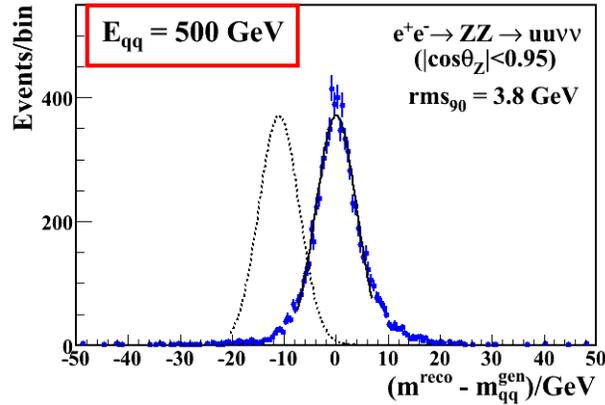
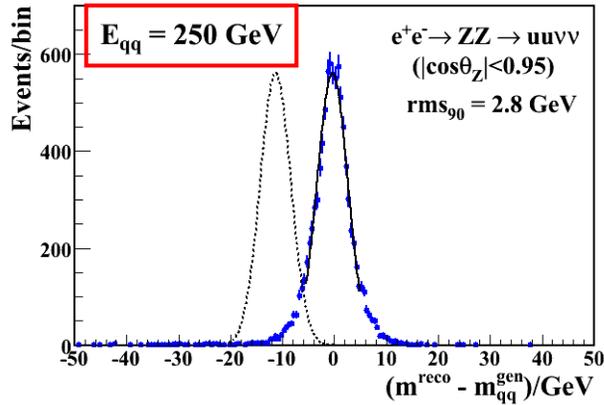
250 GeV Z

500 GeV Z

1 TeV Z



★ Study Z mass resolution as function of  $E_Z$   
with ILD detector (TPC based,  $B=3.5$  T,  $6 \lambda_1$  HCAL)

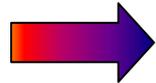


rms90 PandoraPFA v03- $\beta$

$E_Z$	$\sigma_E/E$	$\sigma_m/m$
125 GeV	2.4 %	2.7 %
250 GeV	2.5 %	3.1 %
500 GeV	3.1 %	4.1 %
1 TeV	4.2 %	6.2 %
1.5 TeV	5.6 %	8.2 %

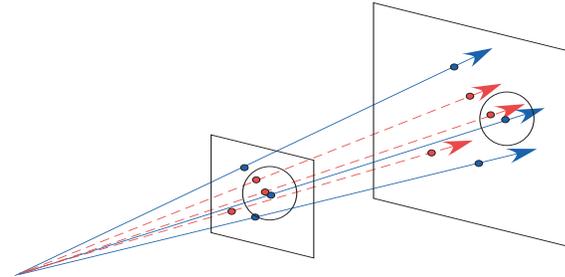
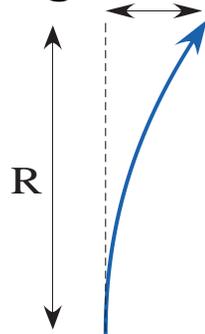
# 7 CLIC Detector Considerations

★ Particle Flow Calorimetry lives or dies on ability to separate energy deposits from individual particles.



- Large detector – spatially separate particles
- High B-field – separate charged/neutrals
- High granularity ECAL/HCAL – resolve particles

**WRONG**



Might expect “figure-of-merit”:

$$\frac{BR^2}{\sigma}$$

← Separation of charge/neutrals  
← Calorimeter granularity/ $R_{\text{Moliere}}$

★ Argues for: **large** + high granularity +  $\uparrow$  B

★ Cost considerations: **small** + lower granularity +  $\downarrow$  B

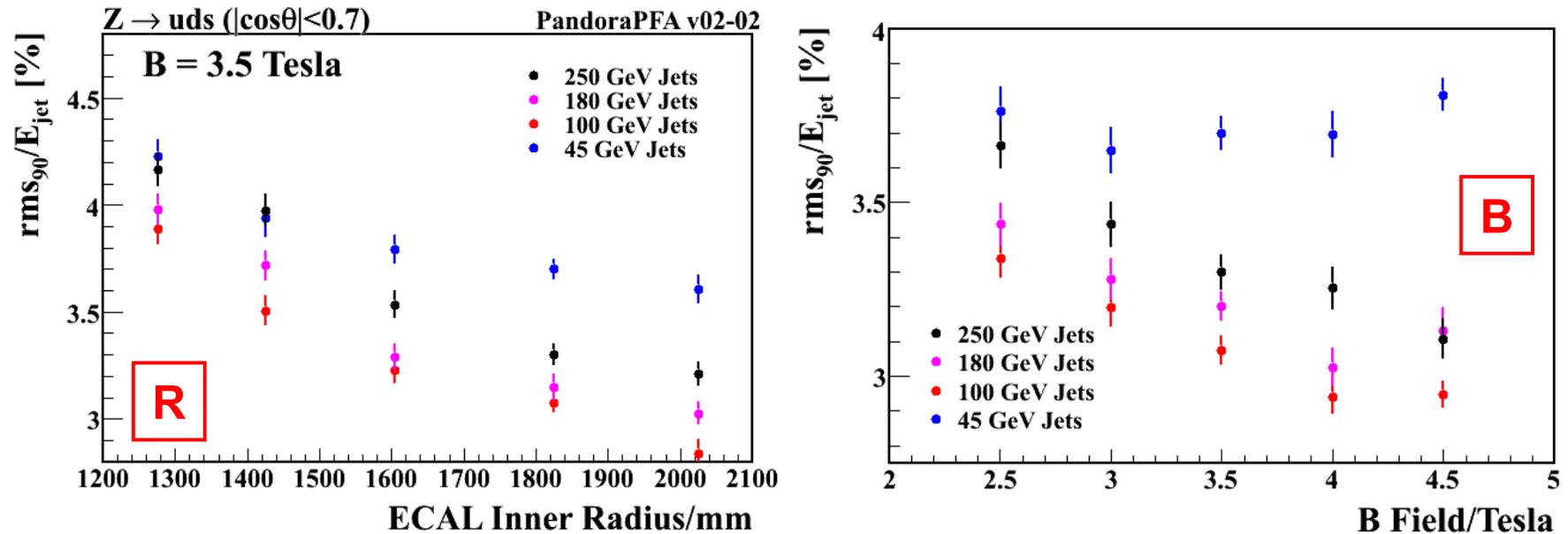


**Study ILC (CLIC) detector parameters using PandoraPFA**



**Interpretation: observing effects of detector + imperfect software**

# ILC/ILD: vary ECAL Inner Radius



★ Empirically (for current algorithm) find

$$\frac{\sigma_E}{E} = \frac{0.021}{\sqrt{E}} \oplus 0.01 \oplus 0.02 \left( \frac{R}{1825} \right)^{-1.0} \left( \frac{B}{3.5} \right)^{-0.35} \left( \frac{E}{100} \right)^{+0.4}$$

Resolution      Tracking/Leakage/Fragments      Confusion

- As expected, larger + higher field gives best performance
- R more important than B

➡ motivates choice of ILD detector concept parameters

(SiD concept team investigating small, high B-field option)

# B vs R at CLIC

- ★ CLIC energies will push limits of Particle Flow Calorimetry
- ★ Particle Flow argues more strongly for large R rather than high B
- ★ For high energy jets, estimate (based on ILC/ILD studies)

R: 1.25m → 2.0m : +60 % improvement

B: 5.0 T → 3.5 T : +13 % improvement

**Argument for high B-field is not Particle Flow !**

B impacts inner radius of Vertex Detector

Dependence not strong

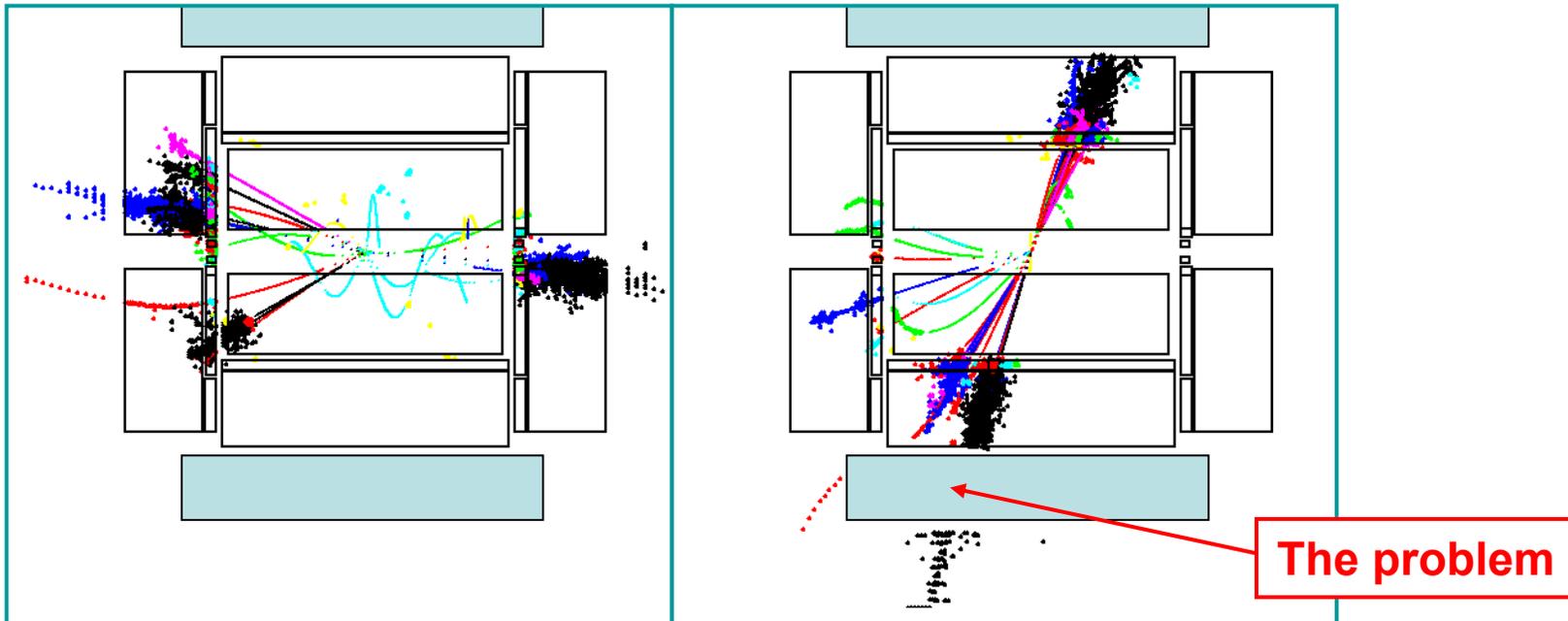
$$r_{\text{inner}} \propto \sqrt{B}$$

# ILC Optimisation Studies: HCAL Depth

## Two interesting questions:

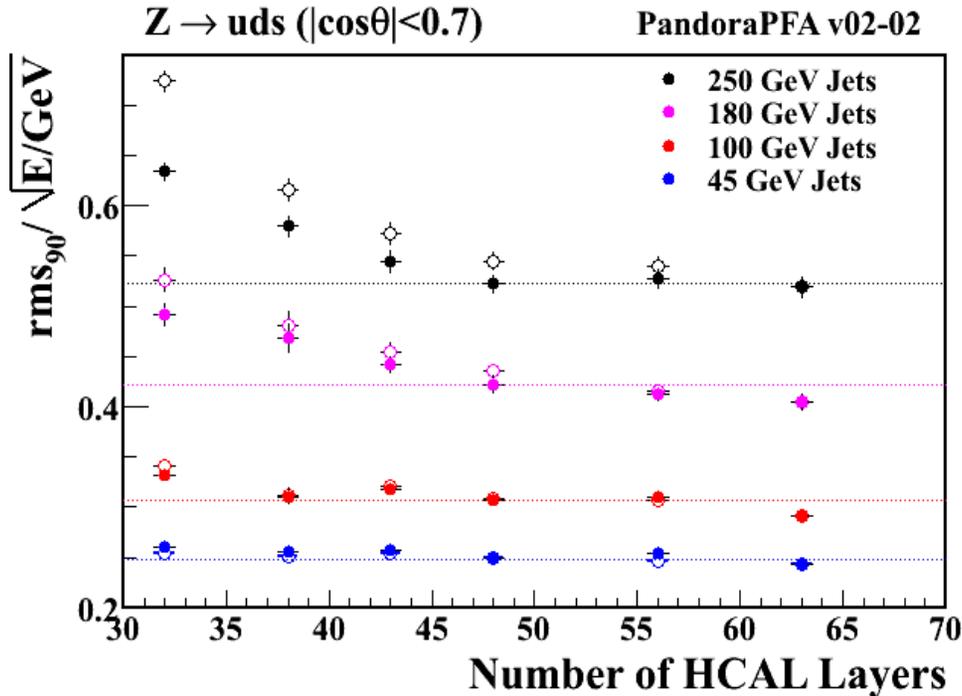
- ★ **How important is HCAL leakage ?**
  - vary number of HCAL layers
- ★ **What can be recovered using MUON chambers as a “Tail catcher”**
  - PandoraPFA now includes MUON chamber reco.
  - Switched off in default version
  - Simple standalone clustering (cone based)
  - Fairly simple matching to CALO clusters (apply energy/momentum veto)
  - Simple energy estimator (digital) + some estimate for loss in coil

e.g.



# ILC/ILD HCAL Depth Results

- Open circles = no use of muon chambers as a “tail-catcher”
- Solid circles = including muon chamber as “tail-catcher”



HCAL Layers	$\lambda_I$	
	HCAL	+ECAL
32	4.0	4.8
38	4.7	5.5
43	5.4	6.2
48	6.0	6.8
63	7.9	8.7

ECAL :  $\lambda_I = 0.8$

HCAL :  $\lambda_I$  includes scintillator

- ★ Results will depend on Hadron Shower simulation
- ★ “Tail-catcher”: corrects ~50% effect of leakage, limited by **thick solenoid**

For 1 TeV machine “reasonable range” ~ 40 – 48 layers ( $5 \lambda_I - 6 \lambda_I$ )

# HCAL Depth at CLIC

Not much data:

$E_{\text{JET}}$	HCAL	$\sigma_E/E = \alpha/\sqrt{E_{jj}}$ $ \cos\theta  < 0.7$	$\sigma_E/E_j$
500 GeV	$6 \lambda_I$	84.1 %	3.7 %
500 GeV	$8 \lambda_I$	$\sim 70$ %	3.4 %

63 layer HCAL ( $8 \lambda_I$ )  
B = 5.0 T, corrected  
to B = 3.5 T

For 3 TeV machine:  $6 \lambda_I$  not sufficient

For 3 TeV machine:  $8 \lambda_I$  ?

Needs study

# 8 Conclusions

## ★ Particle Flow at the ILC

Now have a proof of principle of Particle Flow Calorimetry



Unprecedented Jet Energy Resolution

- Based on full simulation/reconstruction (gaps and all) of **ILD** detector concept

## ★ Particle Flow at CLIC

Particle Flow Calorimetry **certainly not ruled out**

- Need to consider in context of the full CLIC physics programme
  - what drives jet energy resolution goals at CLIC ?
- For Higgs + threshold studies, CLIC would be likely to run at lower energy: **here there is a strong argument for PFA**
- For mono-jet mass resolution, PFA may help at high energies (needs study)
- Perhaps surprisingly, ILD detector concept looks like it **will** give “OK” performance for 500 GeV jets and 1 TeV Zs: i.e. TPC, 3.5 T, 6  $\lambda_1$

# Conclusions cont.

## ★ A Particle Flow Detector for CLIC

- Tracker should be as large as possible
  - $r = 1.25$  m, almost certainly too small for CLIC
- Argument for high B is **not from Particle Flow**
  - momentum resolution/vertex tagging
- Argument for  $B = 5$  T at CLIC may not be that strong
- From ILD studies, no evidence (yet) for problems related to a TPC, don't rule it out yet

## ★ A Particle Flow Development for CLIC

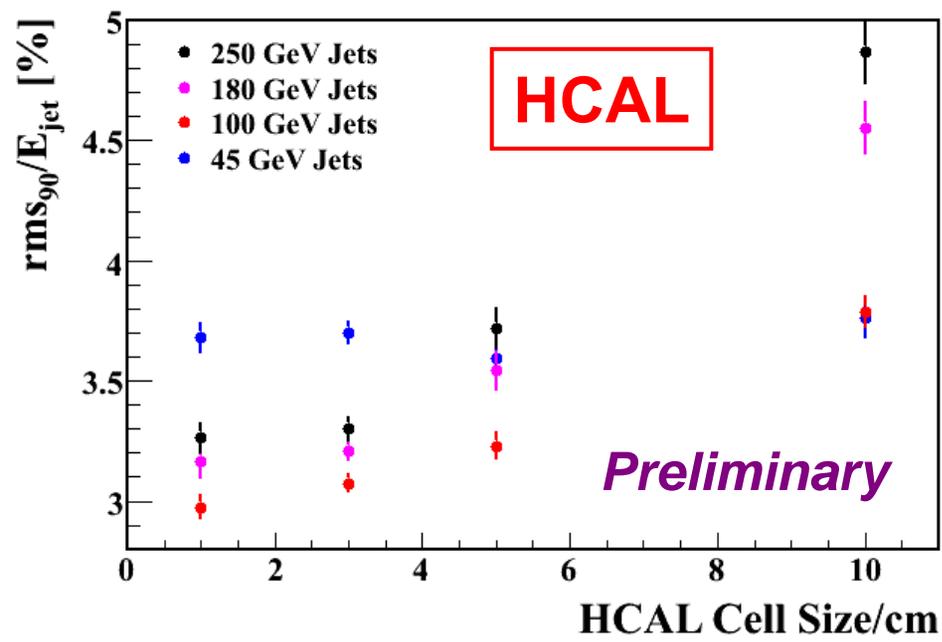
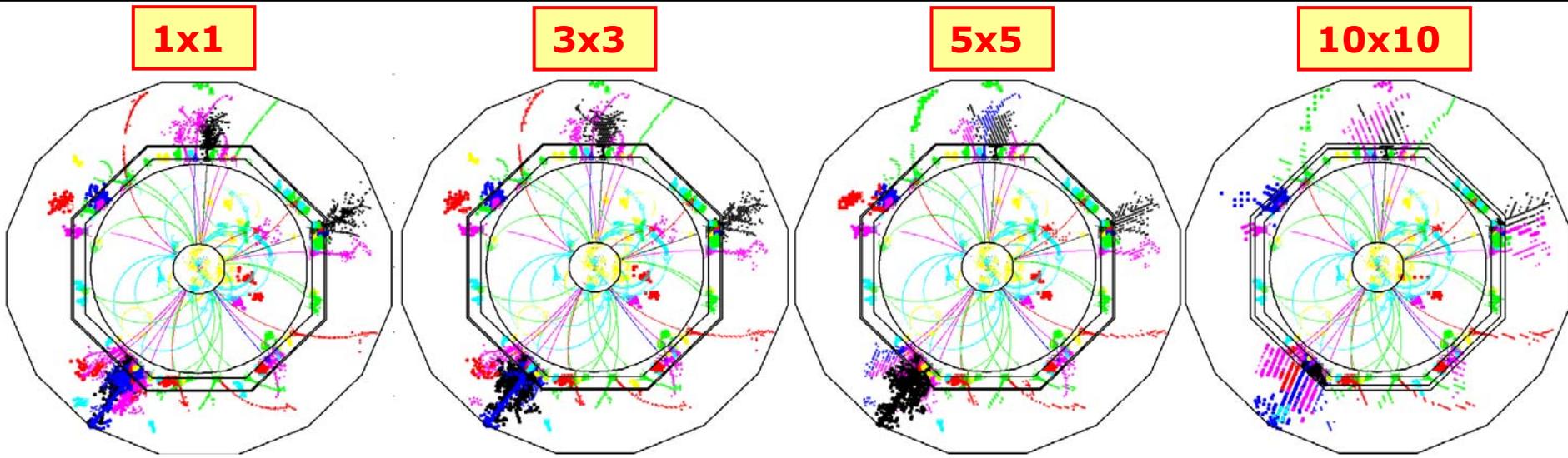
- Not *a priori* obvious that Particle Flow is the right approach for CLIC
- Will require study/development
  - correcting for leakage
  - evolution from PFlow to EFlow to pure calorimetry
  - understanding of jet mass reconstruction...

**Requires new effort**

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**End**

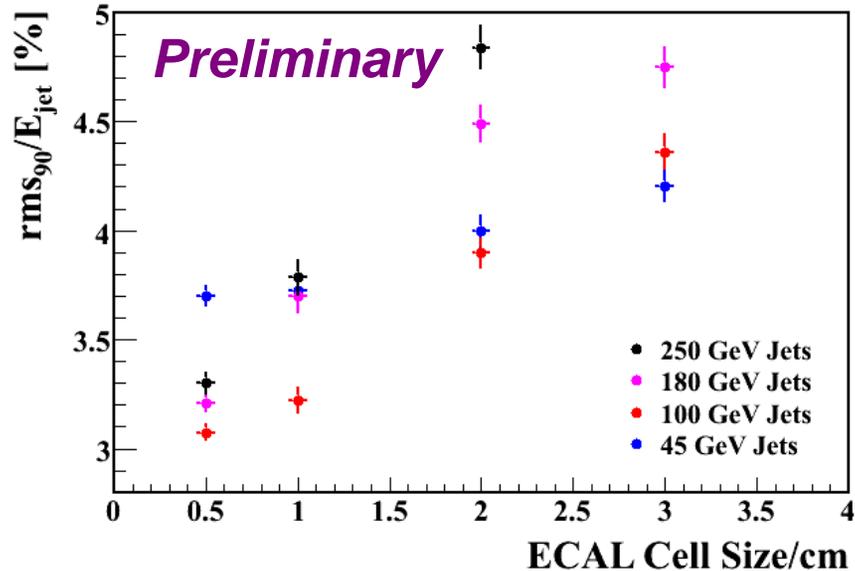
# How important is segmentation ?



- **3×3cm<sup>2</sup> looks reasonable**
- **Hint of gain going to 1×1cm<sup>2</sup>**
- **Significant degradation for larger tile sizes, e.g. 5×5cm<sup>2</sup>**

# and ECAL Segmentation ?

- ★ Investigate  $10\times 10\text{mm}^2$ ,  $20\times 20\text{mm}^2$  and  $30\times 30\text{mm}^2$ 
  - Note: retuned PandoraPFA clustering parameters



- ★ Performance is a **strong function** of pixel size
- ★ High ECAL segmentation is vital for PFA

Caveat:



- Remember results are algorithm dependent
- Could reflect flaw in reconstruction

★ Nevertheless: **highly segmented HCAL/ECAL clearly essential**