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Consider T_{gi} = \langle g|\hat{H}_{int}|i\rangle + \sum_{ij>\neq ii\rangle} \frac{\langle g|\hat{H}_{int}|j\rangle\langle j|\hat{H}_{int}|i\rangle}{E_i - E_j} + \dots
                                                       ( a = shorthand for Pa)
                                                    Mom Con> => a+b=c+d
For special case of
                                                      "| $>" = | = , 4>
 What are states 1; > being summed over!
 Everything
       | j > ∈ { | o >, | a piano >, | a ½ ⊆ d >, | Elon Musk >, | i, | jy >, .... }
 In this giant list, consider just two special entries:
        |j_x|^2 = |c, b, x = a - c| x = particle with mass m & mon <math>x^2
        "|jy > = | a, d, y=b-d > y="particle with mass m & mom y"
 Notes: (1) (mom cons P_{initu} = P_{fru}) \Rightarrow (a+b=c+d) \Rightarrow (z=-y)
                 .. z & y ore heading in opposite directions,
                 and E_x = \sqrt{m^2 + |x|^2} = \sqrt{m^2 + |y|^2} = E_y,
             2 x & y have correct 3-momenta to conserve
               momentum in the following ways:
             3 4-momentum is not conserved, though!
                    (i.e. if ET, = Ec+Ex+Eb
                        and ETZ In Ea+ Ey+ Ed
                       then (a^{M}+b^{M}=c^{M}+\lambda^{M}) \Longrightarrow (E_{a}+E_{b}=E_{c}+E_{\lambda})
                       but (a^{n}+b^{n}=c^{n}+\lambda^{n}) \Rightarrow (E_{a}+E_{b}=E_{T_{1}})
                       and (a^{n}+b^{n}=c^{n}+\lambda^{n}) \Rightarrow (E_{a}+E_{b}=E_{\tau_{2}}).
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A feel for terms in the interaction Hamiltonian

\hat{H}_{int} \stackrel{?}{=} e \hat{\phi} \stackrel{?}{\psi} \stackrel{?}{\psi} \stackrel{?}{+} e \hat{\phi} \stackrel{?}{\psi} \stackrel{?}{\phi} \stackrel{?}{+} \stackrel{?}{=} \frac{1}{4}
\hat{\phi} \sim \int \hat{a}_{p} + \hat{a}_{p}^{\dagger} dp
\hat{\phi} \sim \int \hat{b}_{p} + \hat{b}_{p}^{\dagger} dp
\hat{\phi} \stackrel{?}{\phi} \stackrel{?}{\phi}
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Since "|i) = |a,b) and "|f)" = (s,d) consider the following My:
                             Mgi = JZE, JZE, JZE, JZE, Tgi
                                                       = \sqrt{2E_a} \sqrt{2E_b} \sqrt{2E_c} \sqrt{2E_b} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{a}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{a}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{a}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{a}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{a}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{a}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{a}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{a}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{a}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{c}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{c}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{c}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{c}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{c}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{c}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{c}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{c}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{c}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{c}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{c}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{c}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{c}, \underline{b} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{c}, \underline{d} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \hat{H}_{i,t} | \underline{c}, \underline{d} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \underline{d}, \underline{d} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \underline{d}, \underline{d} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \underline{d}, \underline{d} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \underline{d}, \underline{d} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \underline{d}, \underline{d} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \underline{d}, \underline{d} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \underline{d}, \underline{d} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \underline{d}, \underline{d} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \underline{d}, \underline{d} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \underline{d}, \underline{d} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \underline{d}, \underline{d} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d} | \underline{d}, \underline{d} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle \underline{c}, \underline{d}, \underline{d} \right\rangle + \sum_{|j\rangle \neq |i\rangle} \left\langle 
                                                  = \langle \underline{c}', \underline{a}' | \hat{H}_{int} | \underline{a}', \underline{b}' \rangle + \sum_{\substack{|j\rangle \neq |i\rangle}} \langle \underline{c}', \underline{a}' | \hat{H}_{int} | \underline{a}', \underline{b}' \rangle + \dots
                                                   = \langle \underline{c}', \underline{a}' | \hat{H}_{int} | \underline{a}', \underline{b}' \rangle + \sum_{\substack{ij > \neq i i}} \frac{\langle \underline{c}', \underline{a}' | \hat{H}_{int} | \underline{i} \rangle \langle \underline{i} | \hat{H}_{int} | \underline{a}', \underline{b}' \rangle}{\langle \underline{E}_{x} + \underline{E}_{b} \rangle - \underline{E}_{i}} + \dots
                                                    = M_{cd;ab} + \frac{\langle \underline{c}',\underline{d}'|\hat{H}_{int}|\hat{J}_{x}\rangle\langle \hat{J}_{x}|\hat{H}_{int}|\underline{a}',b'\rangle}{\langle E_{x}+E_{b}\rangle-E_{b}} \(\int\) in sum
                                                                                              + \( \left( \frac{\( \) \\ \left( \) \\ \lef
                                                Ea-Ec-Ex

Ea-Ec-Ex

(ancellations shown rely on \hat{H}_{int}

though certain undiscussed proporties.

Eb-Ed-Ey

Eb-Ed-Ey

(abed)-type fields

(abed)-type fields
                                                        = M_{cd;ab} + \frac{M_{d;bx} M_{cx;a}}{E_a - E_c - E_x} \cdot \frac{1}{2E_x}
                                                                                                                                + \frac{M_{c;ay} M_{dy;b}}{E_{c}-E_{a}-E_{y}} \cdot \frac{1}{2E_{y}} + \cdot \cdot \cdot \cdot [Since (E_{a}+E_{b}=E_{c}+E_{d})=) (E_{b}-E_{d}=E_{c}-E_{a})]
                                         + \frac{9_{ac} \( \xi_{c} - E_{a} - \frac{E_{z}}{E_{z}} \) \frac{2E_{z}}{2E_{z}}
                                                                                                                                                                                                                                                                                                                                                                                                         Md; bx ~ 962 Sd, 5+25. E Kronecker deltas.
                                                                                                                                                                                                                                                                                                                                                                                                  Continuous case would contain Dirac delte-functions ....
                               = h.1 + \frac{9ac9bd}{(Ea-Ec-Ex)} = \frac{5iace}{(Ea-Ec-Ex)} = \frac{5iace}{(Ea-Ex)} = \frac{5iac
                                                                                                                                                                                                                                                                                                                                                                                                                                      \int M_{d;bx} d^3x \sim g(\delta^3(\underline{d}-(\underline{b}+\underline{x}))d^3x \text{ otc.}
                                                                                                                                                                                                                                                                                                                                                                                             (Such J-fines would actually also ensure == - 1/2, so
                                                                                                     - Sac Sbd. 1

(-Ec+Ea+En) 2Ex
                                                                                                                                                                                                                                                                                                                                                                                              no need to separate | jx) and | jy) either!
                                                                                                                                                                                                                                                                                                                                                                                         However - as this is only sketch such details one ignored.
                                   = h + \frac{9_{ac}9_{bh}}{2E_{x}} \frac{[(E_{a}-E_{c})+E_{x}]-[(E_{a}-E_{c})-E_{x}]}{((E_{a}-E_{c})-E_{x})((E_{a}-E_{c})+E_{x})} + \cdots See QFT & AQFT courses for full details.
                                      = h + \frac{9_{ac}9_{bl}}{(E_{a}-E_{c})^{2}-E_{x}^{2}} + \cdots
                 So now, and only now Define a quantity of by:

\boxed{9} = \sqrt[4-mon conserving) . \qquad (a^{1/2}+b^{1/2}=c^{1/2}+d^{1/2}\Rightarrow q^{1/2}=d^{1/2}-b^{1/2} too)

Clearly q'' = \begin{pmatrix} E_a - E_c \\ a - c \end{pmatrix} . q' = q'' q_r = (E_a - E_c)^2 - |a - c|^2
   "
Mg_i \sim h + \frac{9ac9bl}{9^2 + |9-c|^2 - E_x^2} + \dots
                                                                      =h+\frac{9nc911}{9^2+[975]^2-(m^2+12)^2}+\cdots
                                                                      = h + \frac{9ac911}{9^2 - m^2}.
```