

# Flavour - Physics

- Introduction
- Starting time
- lecture notes
- reading?

- LHCb  $\chi$
- DATT  $\chi$  heavy
- EFT • DATT: PDF, RST
- Particle
- ATLAS: loop like
- LHCb LU  $B \rightarrow K_{s,0}$   
 $B \rightarrow K^*_{s,0}$
- V- Exp
- V- Exp
- NLO: Weak boson prod.

• 10:00

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① Flavour - Overview Chapter 1  
2.1-2.3  
2.4.3  
3.1  
3.2  
3.4

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② Ref Chapter 4.1  
4.2  
4.4  
5

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③ B-mixing Chapter 8  
Chapter 9.1  
9.2  
9.3.1  
9.3.2  
9.3.3

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④ BSM searches

Lecture 1

Flavour

Physics

Overview

## Motivation for Standard Physics:

① Precise determination of SM parameter:  
 $m_c, m_b, V_{CKM}, \dots$

② Study of  $\cancel{CP} \Rightarrow$  Matter in Universe

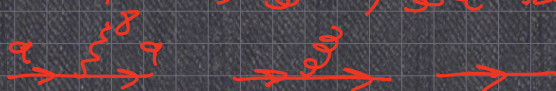
③ Indirect search for BSM

$$P^{Exp} \pm \delta^{Exp} = P^{SM} \pm \delta^{SM} + P^{BSM}(\mu_x, g_x)$$

④ To control QCD to fulfill ① - ③

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i \bar{\psi} \cancel{D} \psi$$

$\gamma, \beta, \alpha, \dots$   $\rightarrow$   $\mu, \nu, \rho, \dots$   $\rightarrow$   $\sigma, \tau, \dots$   $\rightarrow$  Maxwell Eq.




$$+ (\partial_\mu \phi)^2 - V(\phi) \quad \rightarrow \text{Higgs}$$

$$+ \bar{\psi} \gamma \phi \psi + h.c. \quad \rightarrow \text{Yukawa; } m_F$$

$\rightarrow \cancel{CP}, CKM + \text{matrix}$

$m_W, m_Z$



$$+ \mathcal{L}_{BSM}$$



## Particle masses

virtual	$m_t = 172.9(4) \text{ GeV}$
	$m_H = 125.10(14) \text{ GeV}$
	$m_Z = 91.1876(21) \text{ GeV}$
	$m_W = 80.379(12) \text{ GeV}$
$m_b = 4.78(6) \text{ GeV}$	
decay	$m_\tau = 1.77682(12) \text{ GeV}$
	$m_c = 1.67(7) \text{ GeV}$
	$m_\mu = 105.658... \text{ MeV}$
	$m_s = 93_{-2}^{+11} \text{ MeV}$
⋮	⊙

⑬ Heavy Hadrons:

	Mass [GeV]	Lifetime [ps]	$\frac{\tau(X)}{\tau(B_d)}$
$B_d = \bar{b}d$	5.28	1.519 (4)	1
$B^+ = \bar{b}u$	5.28	1.638 (4)	1.076 (4)
$B_s = \bar{b}s$	5.37	1.516 (6)	0.998 (5)
<u><math>B_c^+ = \bar{b}c</math></u>	6.27	0.510 (9)	0.336 (6)
$\Lambda_b = bud$	5.62	1.471 (9)	0.969 (6)
$\Xi_b^0 = bus$	5.79	1.480 (30)	0.974 (20)
$\Xi_b^- = bds$	5.79	1.572 (40)	1.035 (26)
$\Omega_b^- = bss$	6.05	1.64 (+18, -17)	1.08 (+12, -11)

Remarks:

- Heavy Quark Expansion (HQE)

$$\Gamma_{\text{total}} = \underbrace{\Gamma_0}_{\substack{\text{free} \\ b\text{-quark} \\ \text{decay}}} + \underbrace{\left(\frac{\Lambda}{m_b}\right)^2}_{\substack{\text{corrections} \\ \left(\frac{1}{5}\right)^2 = 4\%}} \dots$$

$$\rightarrow \tau(B^+) \simeq \tau(B_d) \simeq \tau(B_s)$$

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## Heavy Hadrons:

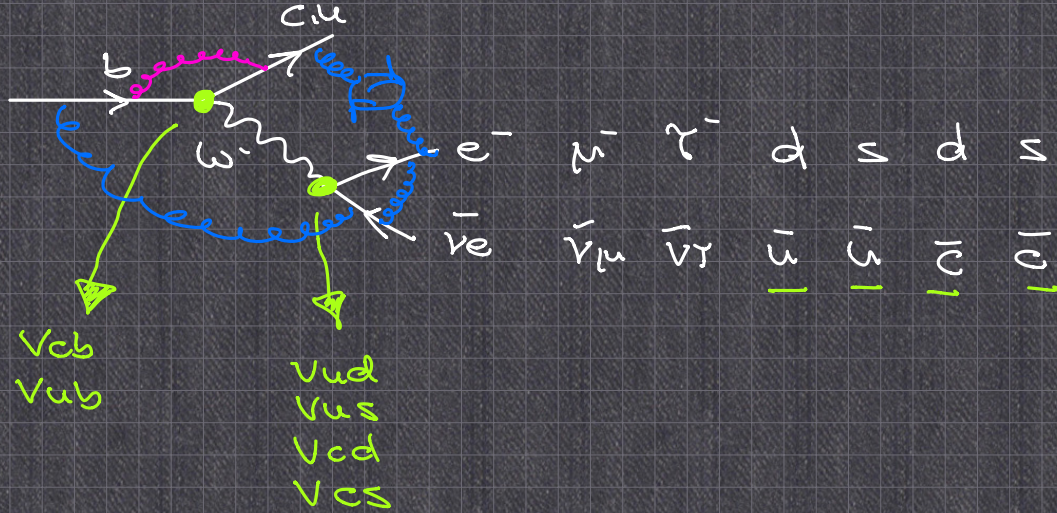
	Mass [GeV]	Lifetime [ps]	$\frac{\tau(X)}{\tau(D^0)}$
$D^0 = c\bar{u}$	1.86	0.410(15)	1
$D^+ = c\bar{d}$	1.87	1.040(7)	2.535(17)
$D_s^+ = c\bar{s}$	1.97	0.504(4)	1.229(10)
$\Lambda_c = cd u$	2.29	0.200(6)	0.488(15)
$\Xi_c^+ = cs u$	2.47	0.442(26)	1.08(6)
$\Xi_c^0 = cs d$	2.47	0.112 (+13/-10)	0.27(3)
$\Omega_c = css$	2.70	0.268(26)	0.65(6)

## HQE

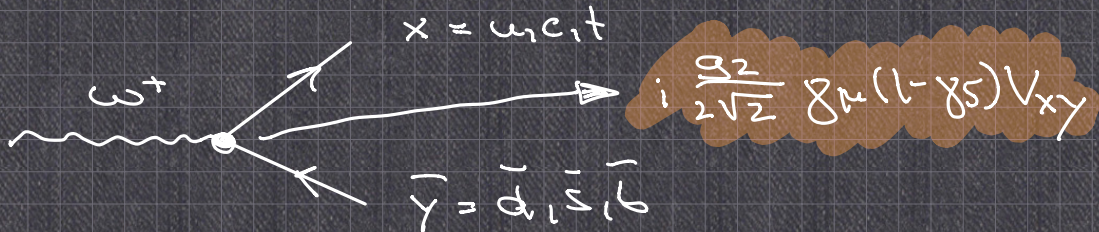
$$\Gamma_{\text{total}} = \Gamma_0 + \left(\frac{v}{mc}\right)^2 \dots$$

$$\left(\frac{1}{1.5}\right)^2 = 36\% \quad ?$$

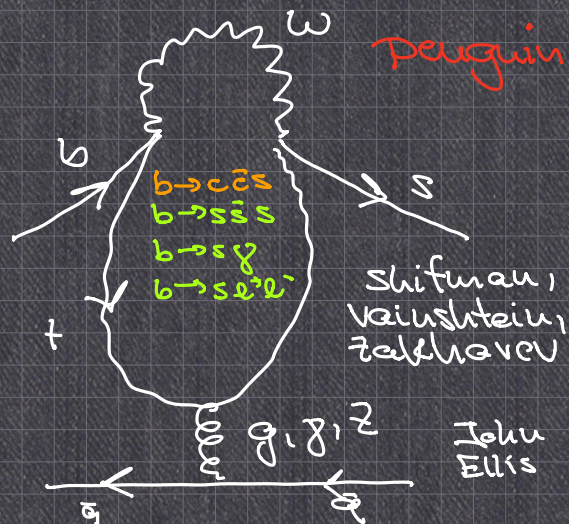
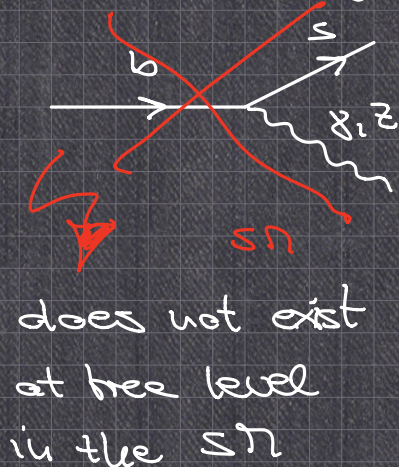
# Decay of heavy quarks!



## Elementary vertex



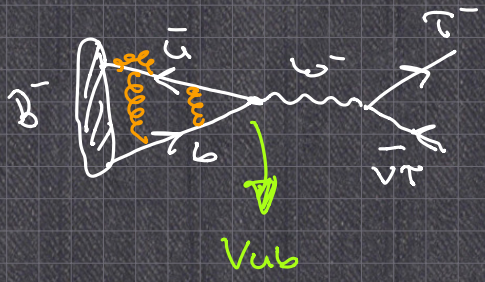
## Flavor changing neutral current





# Decay of heavy Hadrons:

a) Leptonic e.g.  $\underbrace{B^- \rightarrow \tau^- \bar{\nu}_\tau}_{\text{tree}}, \underbrace{B_s \rightarrow \mu^+ \mu^-}_{\text{loop}}$



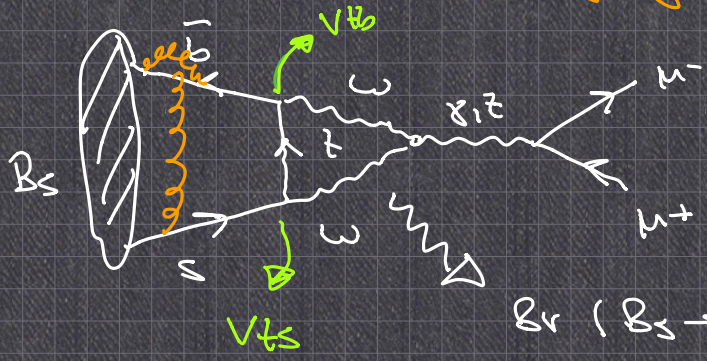
non-perturbative physics

$$\langle 0 | \bar{u} \gamma^\mu \gamma_5 b | B_q(p) \rangle = i f_{B_q} p^\mu$$

decay constant

→ Lattice QCD

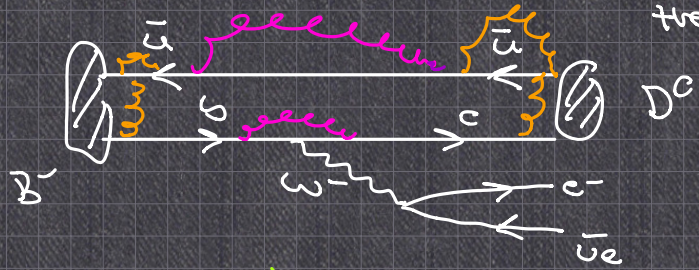
numbers: Google "FLAG lattice"



→  $f_{B_s}$

$$\text{Br}(B_s \rightarrow \mu\mu) \simeq 3 \cdot 10^{-9}$$

b) semileptonic e.g.  $\underbrace{B^- \rightarrow D^0 e^- \bar{\nu}_e}_{\text{tree}}, \underbrace{B^0 \rightarrow K^* \mu^+ \mu^-}_{\text{loop}}$

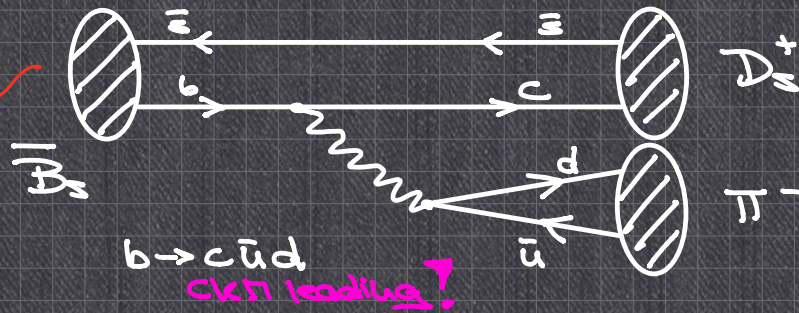


non-perturbative physics

$$\langle D^0 | \bar{c} \gamma^\mu \gamma_5 b | B \rangle \sim \text{Form factor } f(q^2)$$

→ lattice QCD, sum rules

c) neu-leptonic



$PDG \quad 3.00(23) \cdot 10^{-3} \rightarrow 4.67$  <sup>2007, 10338</sup>  
 $QCD f \quad \underline{4.42(21) \cdot 10^{-3}} \rightarrow$  <sup>references</sup>

Additional assumption for neu-  
 perturbative physics

QCD factorisation

## CKM matrix

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

loop

B-decays

## Remarks:

- $V_{CKM}$  is unitary per construction
- 4 parameters

3 real  
angles

1 phase

$\equiv \cancel{\phi}$



$\Rightarrow$  Wolfenstein parametrization

(Taylor expansion of  $V_{CKM}$  in "standard parametrization  $\equiv$  product of 3 rotation matrices);  $V_{us} \doteq \lambda = 0.224837\dots$  small

$$V_{CKM} = \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3 \sin\eta \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \sin\eta) - A\lambda^2 & \lambda & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

"CKM fitter" (see also "UTfit")

$$\lambda = 0.224837 \begin{matrix} +0.000251 \\ -0.000001 \end{matrix}$$

$$A = 0.8235 \begin{matrix} +0.0056 \\ -0.0145 \end{matrix}$$

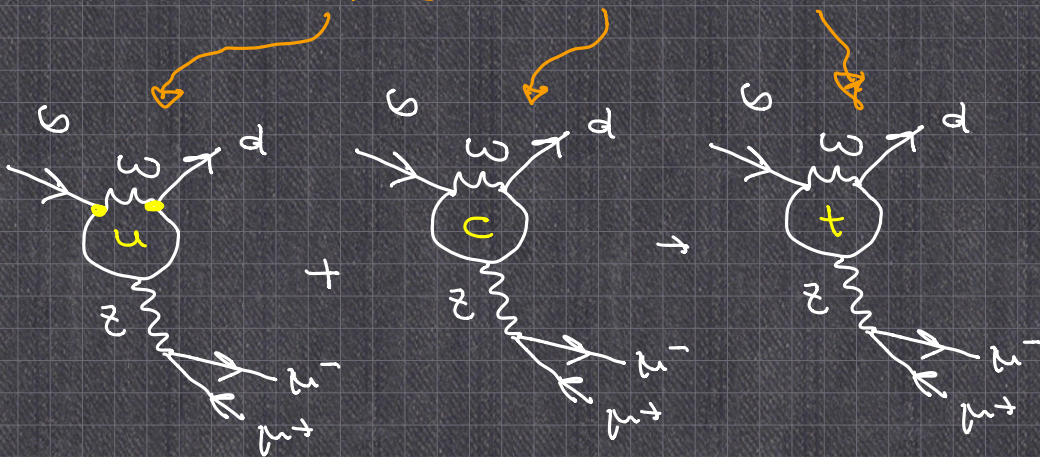
$$\rho = 0.1568 \begin{matrix} +0.0102 \\ -0.0061 \end{matrix}$$

$$\eta = 0.3499 \begin{matrix} +0.0079 \\ -0.0065 \end{matrix} \equiv \overline{\text{CP}}$$

The Unitarity Triangle

$$V_{cb}^\dagger V_{cs} + V_{cb}^\dagger V_{cb} + V_{cb}^\dagger V_{cb} = \mathbb{1} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$\ominus = \underbrace{V_{ud} V_{us}^* + V_{cd} V_{cb}^*}_{\text{yellow}} + \underbrace{V_{cd} V_{cb}^*}_{\text{yellow}} + \underbrace{V_{td} V_{tb}^*}_{\text{yellow}}$$



Assume:  $m_u = m_c = m_t$

$$\Rightarrow A(b \rightarrow d \mu^+ \mu^-) = \ominus$$

GIM mechanism

B-mixing: -

$$\begin{array}{ccc}
 \begin{array}{c} b \quad u \quad d \\ \rightarrow \quad \rightarrow \quad \rightarrow \\ \text{wavy } \omega \quad \text{wavy } \omega \\ \leftarrow \quad \leftarrow \quad \leftarrow \\ \bar{d} \quad \bar{u} \quad \bar{b} \end{array} & + & \begin{array}{c} b \quad c \quad d \\ \rightarrow \quad \rightarrow \quad \rightarrow \\ \text{wavy } \omega \quad \text{wavy } \omega \\ \leftarrow \quad \leftarrow \quad \leftarrow \\ \bar{d} \quad \bar{c} \quad \bar{b} \end{array} & + & \begin{array}{c} b \quad t \quad d \\ \rightarrow \quad \rightarrow \quad \rightarrow \\ \text{wavy } \omega \quad \text{wavy } \omega \\ \leftarrow \quad \leftarrow \quad \leftarrow \\ \bar{d} \quad \bar{t} \quad \bar{b} \end{array} \\
 \sim (V_{ud} V_{ub}^*)^2 & & \sim |V_{cd} V_{cb}^*|^2 & & \sim |V_{td} V_{tb}^*|^2
 \end{array}$$

$$+ \sum_c^u \sum_c^c + \dots \Rightarrow \text{mixing is proportional to}$$

$$(V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^*)^2$$