

The contribution of diagram (a) is given by

$$M = \frac{(-ig_W)^2}{8} \bar{v}(p_+) \not{q}_+(1 - \gamma_5) \frac{i}{\not{p}_- - \not{q}_-} \not{q}_-(1 - \gamma_5) u(p_-) . \quad (8.114)$$

Inserting the leading term for the polarizations from Eq. (8.113) and dropping non-leading terms, we obtain

$$M = -i \frac{(-ig_W)^2}{8M_W^2} \bar{v}(p_+) (\not{q}_+ - \not{q}_-) (1 - \gamma_5) u(p_-) . \quad (8.115)$$

The contribution of the photon exchange diagram (b), using the Feynman rules of Figs. 8.2(updated) and 8.5, is

$$\begin{aligned} M &= (-ig_W)^2 Q_e \sin^2 \theta_W \bar{v}(p_+) \gamma^\rho u(p_-) \frac{-ig_{\rho\alpha}}{(q_+ + q_-)^2} \\ &\times V^{\beta\delta\alpha}(-q_+, -q_-, q_+ + q_-) \varepsilon_\beta(q_+) \varepsilon_\delta(q_-) . \end{aligned} \quad (8.116)$$

The contribution of the  $Z$  exchange diagram (c) is

$$\begin{aligned} M &= \frac{(-ig_W)^2}{2} \bar{v}(p_+) \gamma^\rho (V_e - A_e \gamma_5) u(p_-) \frac{-ig_{\rho\alpha}}{(q_+ + q_-)^2 - M_Z^2} \\ &\times V^{\beta\delta\alpha}(-q_+, -q_-, q_+ + q_-) \varepsilon_\beta(q_+) \varepsilon_\delta(q_-) . \end{aligned} \quad (8.117)$$

where

$$V^{\beta\delta\alpha}(p, q, r) = g^{\beta\delta}(p^\alpha - q^\alpha) + g^{\delta\alpha}(q^\beta - r^\beta) + g^{\alpha\beta}(r^\delta - p^\delta) . \quad (8.118)$$

Hence we find, using the approximate longitudinal polarization vector of Eq. (8.113),

$$\begin{aligned} &V^{\beta\delta\alpha}(-q_+, -q_-, q_+ + q_-) \varepsilon_\beta(q_+) \varepsilon_\delta(q_-) \\ &= \frac{(q_+ + q_-)^2}{2M_W^2} [q_+^\alpha - q_-^\alpha] + O(1) . \end{aligned} \quad (8.119)$$

The result for the sum of the  $Z$  and  $\gamma$  exchange contributions, after inserting the values for  $V_e$  and  $A_e$ , is

$$M = i \frac{(-ig_W)^2}{8M_W^2} \bar{v}(p_+) (\not{q}_+ - \not{q}_-) (1 - \gamma_5) u(p_-) , \quad (8.120)$$

which cancels exactly with Eq. (7.115). So we see that the leading high-energy behaviour is cancelled, as a result of the relationship between the three-boson couplings and the couplings to fermions imposed by the gauge structure.