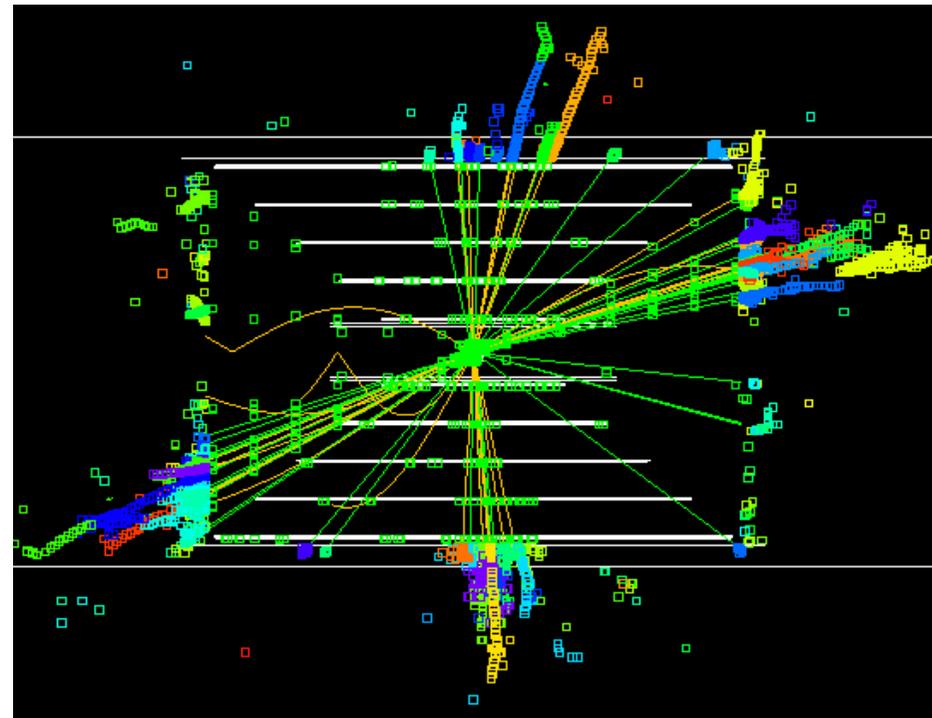
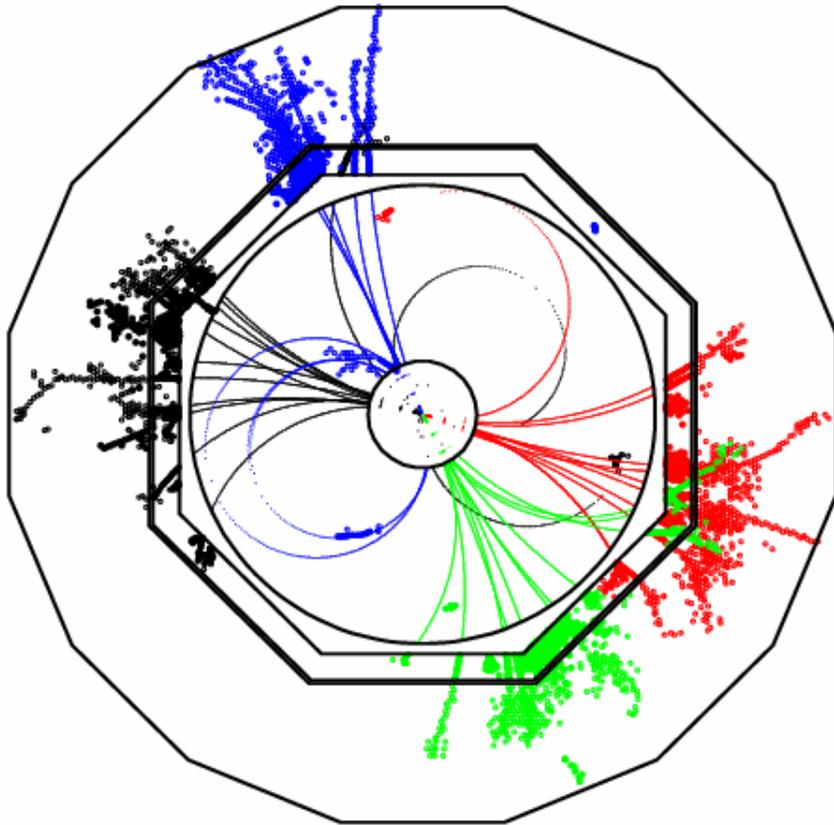


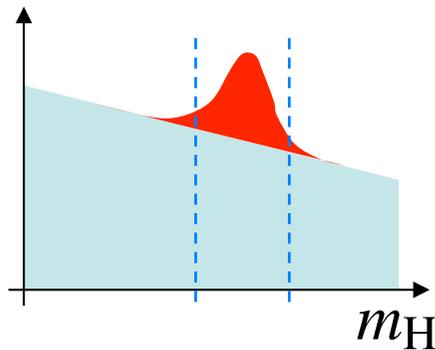
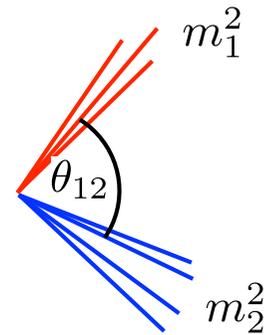
Status of Particle Flow Calorimetry

Mark Thomson
University of Cambridge



1 Calorimetry at a Future Lepton Collider

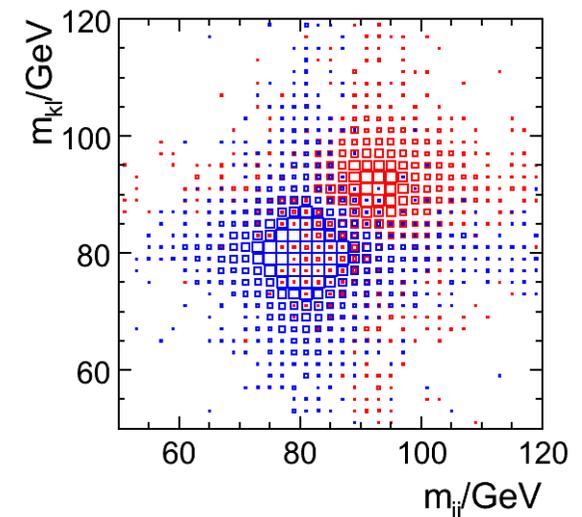
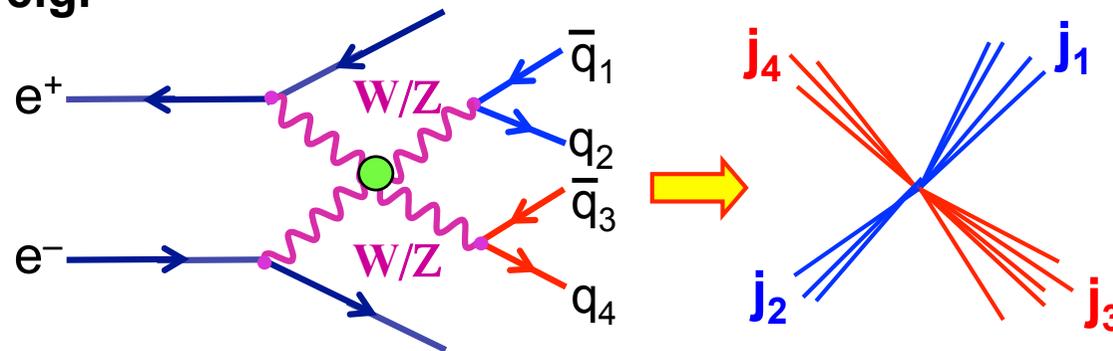
- ★ What are the jet energy requirements at a future LC ?
 - in part, depends on physics
- ★ Likely to be primarily interested in di-jet mass resolution
 - For a narrow resonance, want **best possible di-jet mass res.**



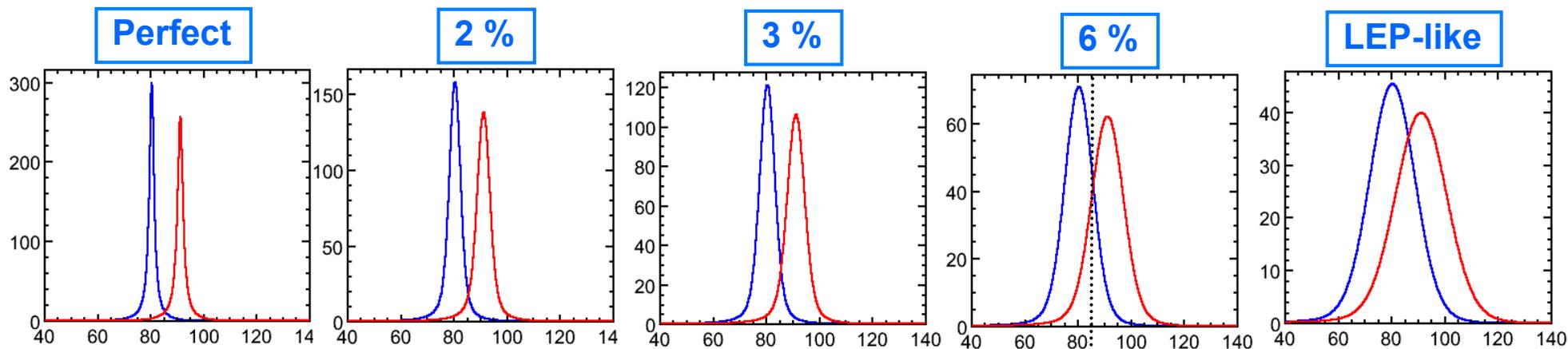
$$\text{signif.} \propto \frac{S}{\sqrt{B}} \propto (\text{resolution})^{-\frac{1}{2}}$$

- **At very least**, need to separate W/Z hadronic decays

e.g.



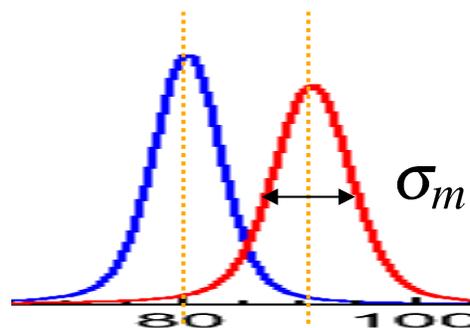
- Gauge boson width sets “natural” goal for **minimum** jet energy resolution



- Quantify by **effective W/Z separation**

$$W/Z \text{ sep} = (m_Z - m_W) / \sigma_m$$

Jet E res.	W/Z sep
perfect	3.1 σ
2%	2.9 σ
3%	2.6 σ
4%	2.3 σ
5%	2.0 σ
10%	1.1 σ



Defined as **effective**
Gaussian equivalent
Mass resolution

- **3 – 4 %** jet energy resolution give decent W/Z separation **2.6 – 2.3 σ**
- sets a **reasonable** choice for Lepton Collider jet energy **minimal** goal **~3.5 %**
- for W/Z separation, not much to gain beyond this as limited by W/Z widths

Physics Context : LC jet energies

- ★ At 500 GeV (ILC) primarily interested in 4-fermion/6-fermion final states
 - e.g. $e^+e^- \rightarrow ZH \rightarrow q\bar{q}b\bar{b}$ and $e^+e^- \rightarrow t\bar{t} \rightarrow bq\bar{q}bq\bar{q}$
- ★ For higher centre-of-mass energies (CLIC, muon-collider), fermion multiplicities will tend to be higher, e.g. SUSY cascade decays
- ★ Sets scale of typical jet energies:

\sqrt{s}	#fermions	Jet energy
250 GeV	4	~60 GeV
500 GeV	4 – 6	80 – 125 GeV
1 TeV	4 – 6	170 – 250 GeV
3 TeV	6 – 8	375 – 500 GeV

} ILC - like

} CLIC - like

ILC Goals: ~3.5 % jet energy resolution for 50 – 250 GeV jets

CLIC Goals: ~3.5 % jet energy resolution for 100 – 500 GeV jets

Sets the goal for calorimetry at a future LC

Can this be achieved with particle flow technique?

2 Particle Flow Calorimetry

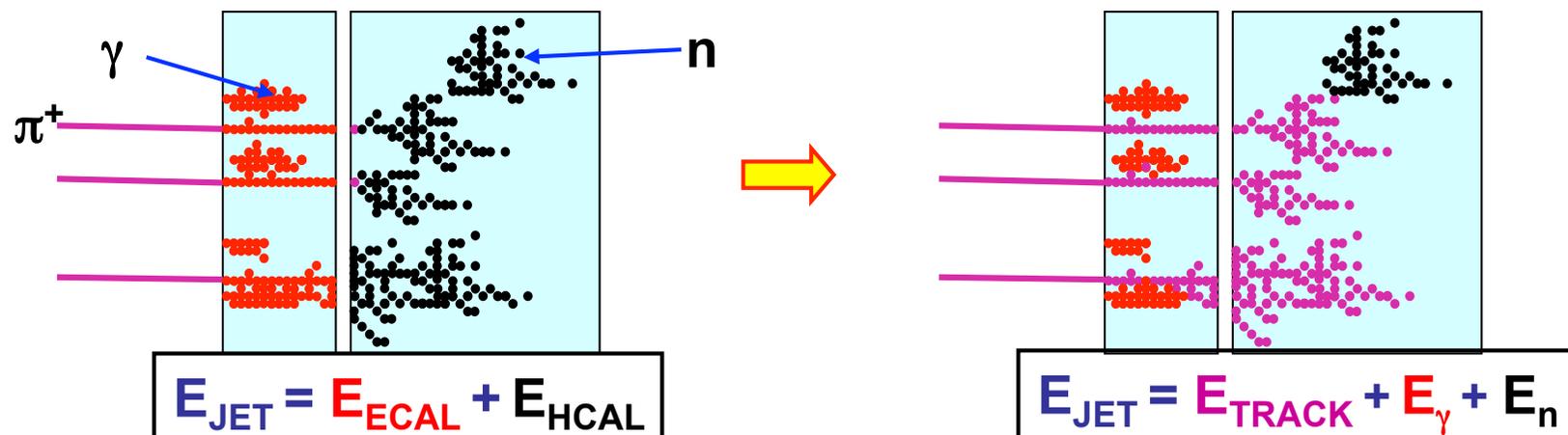
★ In a typical jet :

- ◆ 60 % of jet energy in charged hadrons
- ◆ 30 % in photons (mainly from $\pi^0 \rightarrow \gamma\gamma$)
- ◆ 10 % in neutral hadrons (mainly n and K_L)



★ Traditional calorimetric approach:

- ◆ Measure all components of jet energy in ECAL/HCAL !
- ◆ ~70 % of energy measured in HCAL: $\sigma_E/E \approx 60\% / \sqrt{E(\text{GeV})}$
- ◆ Intrinsically “poor” HCAL resolution limits jet energy resolution

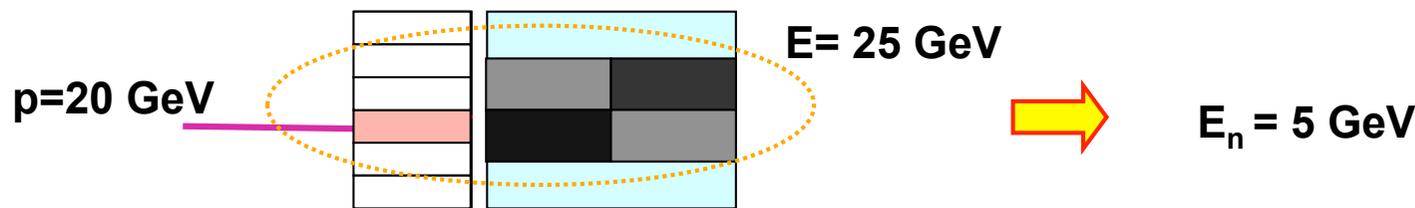


★ Particle Flow Calorimetry paradigm:

- ◆ charged particles measured in tracker (essentially perfectly)
- ◆ Photons in ECAL: $\sigma_E/E < 20\% / \sqrt{E(\text{GeV})}$
- ◆ Neutral hadrons (ONLY) in HCAL
- ◆ Only 10 % of jet energy from HCAL \Rightarrow much improved resolution

“Energy Flow” vs “Particle Flow”

- ★ The idea *behind* particle flow calorimetry is not new
- ★ a *similar* idea was first (?) used by ALEPH NIM A360:481-506, 1995
 - ♦ Jet energies reconstructed using an “ENERGY FLOW” algorithm
 - ♦ Remove ECAL deposits from IDed electrons/photons
 - ♦ Left (mostly) with charged and neutral hadrons
 - ♦ **However**, insufficient HCAL granularity to identify neutral hadrons
 - ♦ Neutral hadrons identified as significant excesses of CAL energy



- ♦ Energy of neutral hadron obtained by **subtraction**: $E_n = E_{\text{calo}} - p_{\text{track}}$
 - ➔ $\sigma_E/E \sim 10\%$ jet E resolution for 45 GeV jets

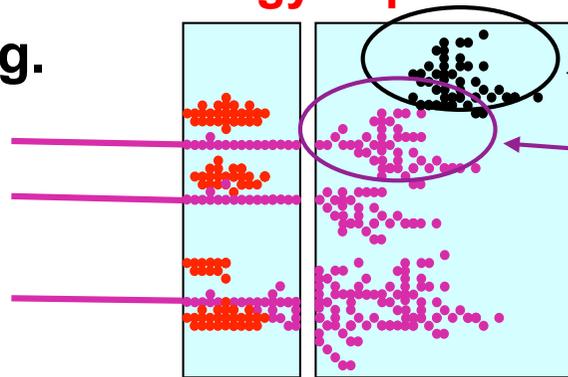
- ★ Similar approach used by a number of other collider experiments, e.g CMS
- ★ “PARTICLE FLOW” significantly extends this approach to a high granularity calorimeter
 - ♦ Now directly **reconstruct neutral hadrons**
 - ♦ Potentially much better performance
 - ♦ **but need highly granular calorimeter + sophisticated software**“particle flow algorithm”

Particle Flow Reconstruction

Reconstruction of a Particle Flow Calorimeter:

- ★ Avoid double counting of energy from same particle
- ★ Separate energy deposits from different particles

e.g.

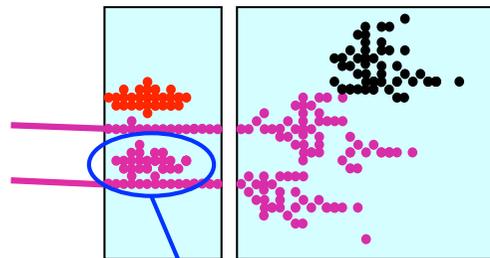


If these hits are clustered together with these, lose energy deposit from this neutral hadron (now part of track particle) and ruin energy measurement for this jet.

Level of mistakes, “confusion”, determines jet energy resolution
not the intrinsic calorimetric performance of ECAL/HCAL

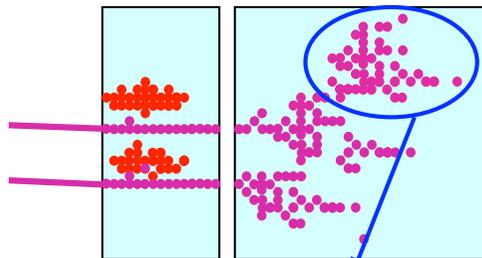
Three types of confusion:

i) Photons



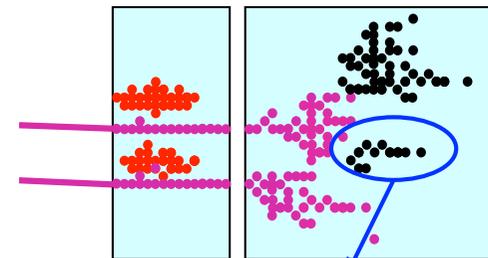
Failure to resolve photon

ii) Neutral Hadrons



Failure to resolve neutral hadron

iii) Fragments

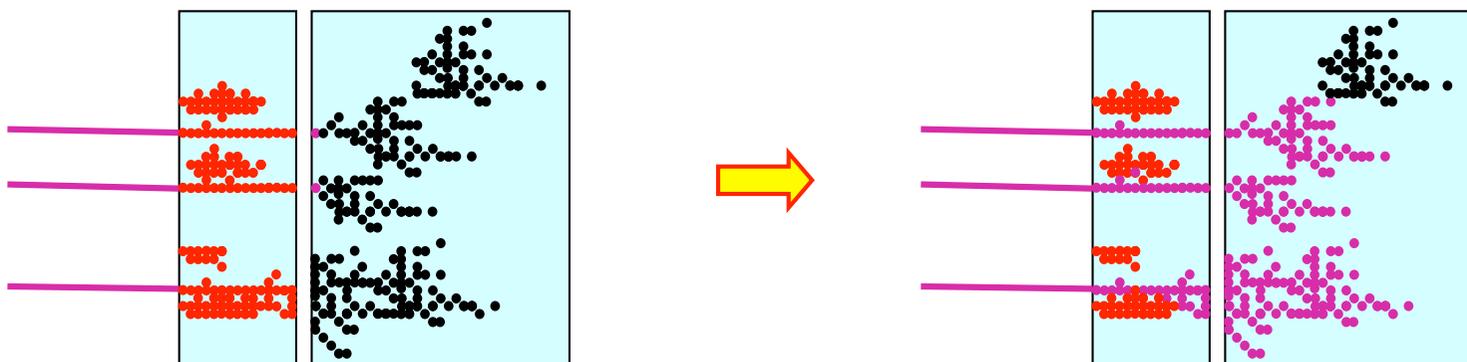


Reconstruct fragment as separate neutral hadron

Towards Particle Flow Calorimetry

- ★ Particle Flow Calorimetry = **HARDWARE + SOFTWARE**
- ★ Need to study both aspects to demonstrate Pflow concept
 - ✦ CALICE studying a number of technological options for a **high granularity ECAL/HCAL**
 - ✦ No obvious show-stoppers...

➡ Then need sophisticated PFlow reconstruction software

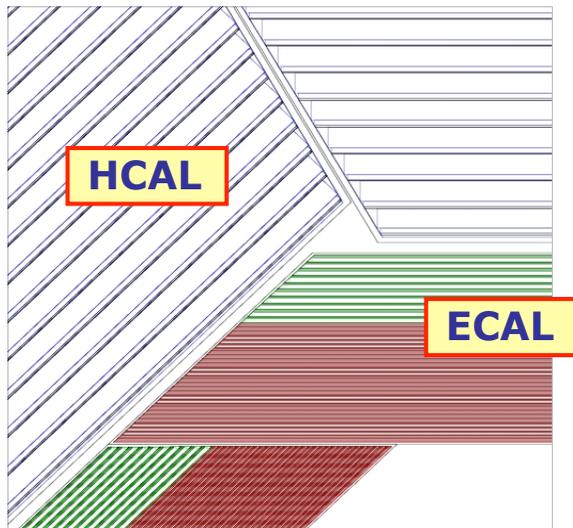
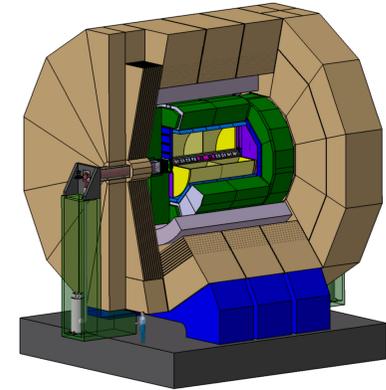


ILC Detector Concepts

- ★ Particle Flow needs to be studied in the context of the whole detector
 - ♦ tracking is central to particle flow reconstruction
- ★ Need detailed GEANT 4 simulations of potential detector designs, e.g. the ILC detector concepts (ILD and SiD)

e.g. ILD: International Large Detector

“Large” : tracker radius 1.8m
B-field : 3.5 T
Tracker : TPC
Calorimetry : **high granularity particle flow**
ECAL + HCAL inside large solenoid



ECAL:

- SiW sampling calorimeter
- longitudinal segmentation: 30 layers
- transverse segmentation: 5x5 mm² pixels

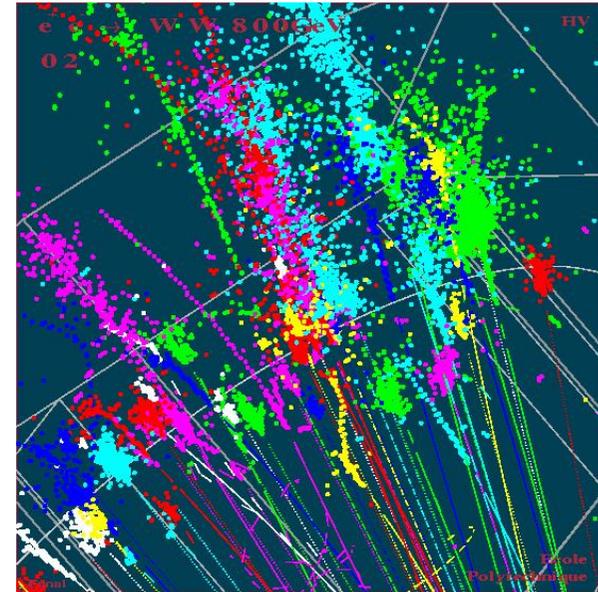
HCAL:

- Steel-Scintillator tile sampling calorimeter
- longitudinal segmentation: 48 layers (6 λ_1)
- transverse segmentation: 3x3 cm² tiles

Calorimeter Reconstruction

- ★ High granularity calorimeters – very different to previous detectors
- ★ “Tracking calorimeter” – requires a new approach to ECAL/HCAL reconstruction – a new problem

Particle Flow Algorithms (PFA)



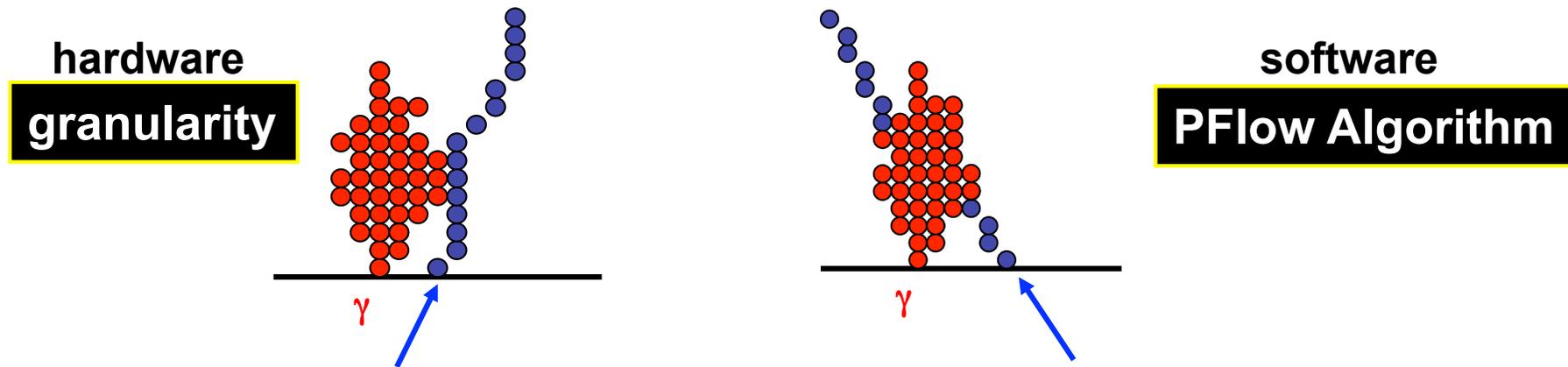
- ★ To assess full potential of Particle Flow need a “realistic” algorithm
 - + full detector reconstruction (no use of Monte Carlo information) many years before project is approved !
- ★ Most sophisticated and best performing Particle Flow Algorithm (PFA) is “PandoraPFA”
- ★ Has been used to:
 - ✦ demonstrate the potential of high granularity Particle Flow Calorimetry
 - ✦ gain an understanding of what drives performance

PFA : Basic issues

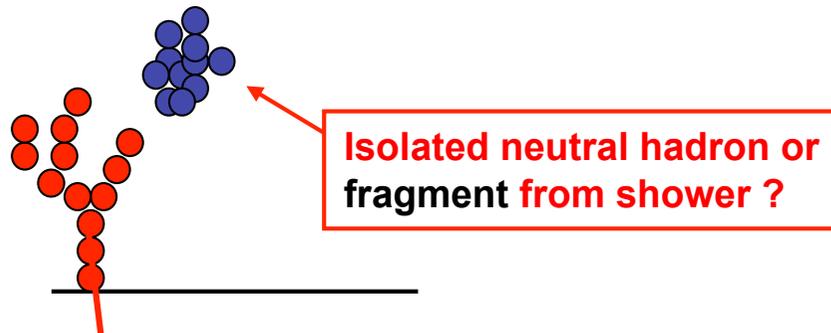
- ★ Separate energy deposits from different particles
- ★ Avoid double counting of energy from same particle
- ★ Mistakes drive particle flow jet energy resolution

e.g.

- ★ Need to separate “tracks” (charged hadrons) from photons



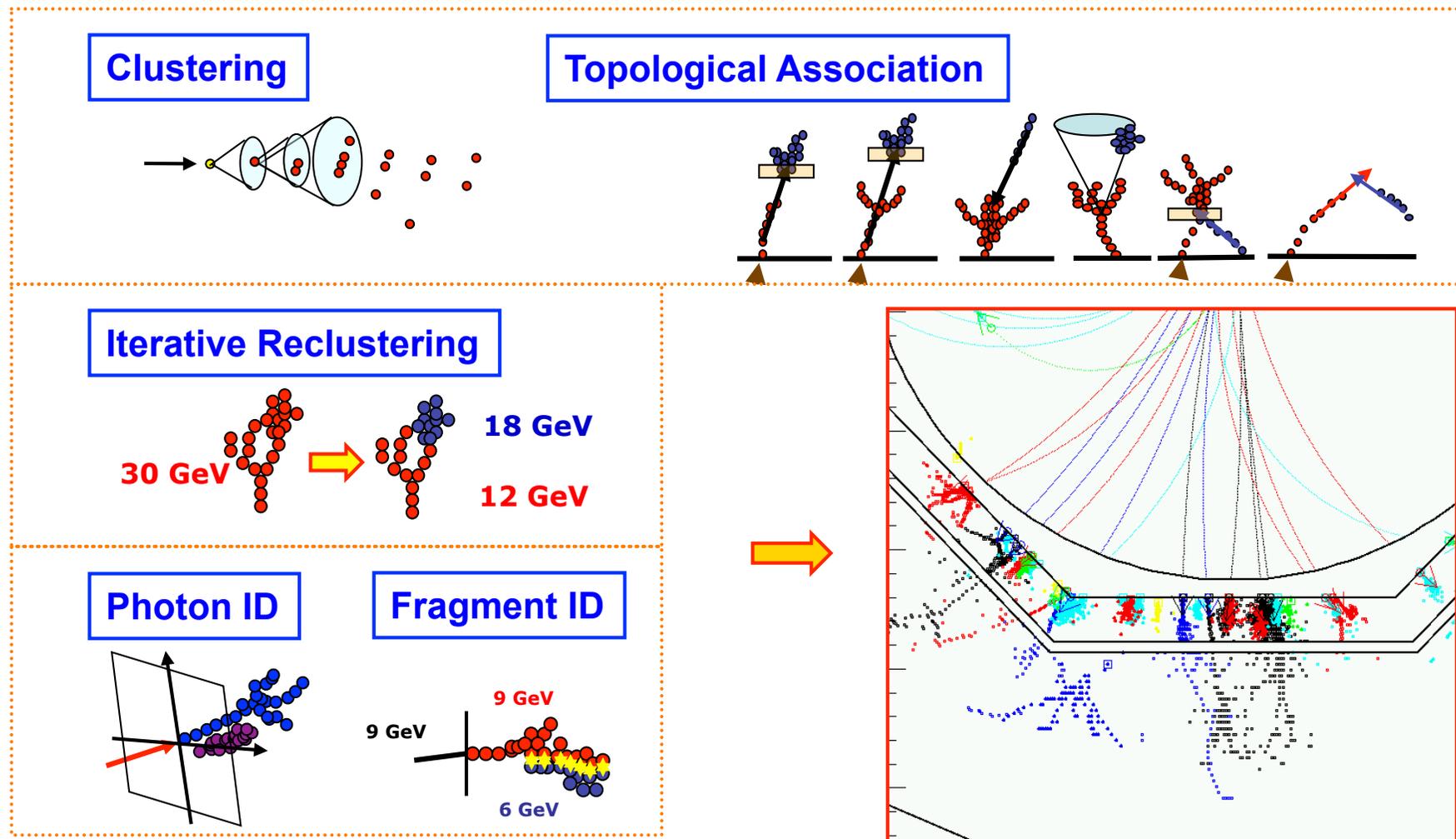
- ★ Need to separate neutral hadrons from charged hadrons



- ★ Requires novel/sophisticated reconstruction techniques...

The PandoraPFA Algorithm

- ★ High granularity Pflow reconstruction is highly non-trivial !
PandoraPFA consists of a many complex steps (not all shown)



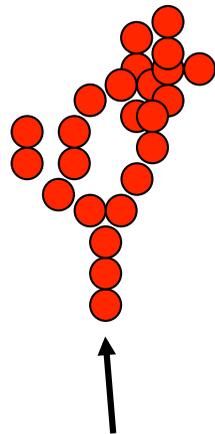
MT, NIM 611 (2009) 24-40

e.g. Iterative Reclustering

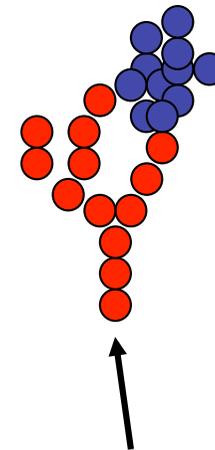
- ★ At some point, in high density jets (high energies) reach the limit of “pure” particle flow
 - ◆ i.e. can’t cleanly resolve neutral hadron in a hadronic shower
- ★ If track momentum and cluster energy inconsistent : **RECLUSTER**

e.g.

30 GeV



10 GeV Track



18 GeV

12 GeV

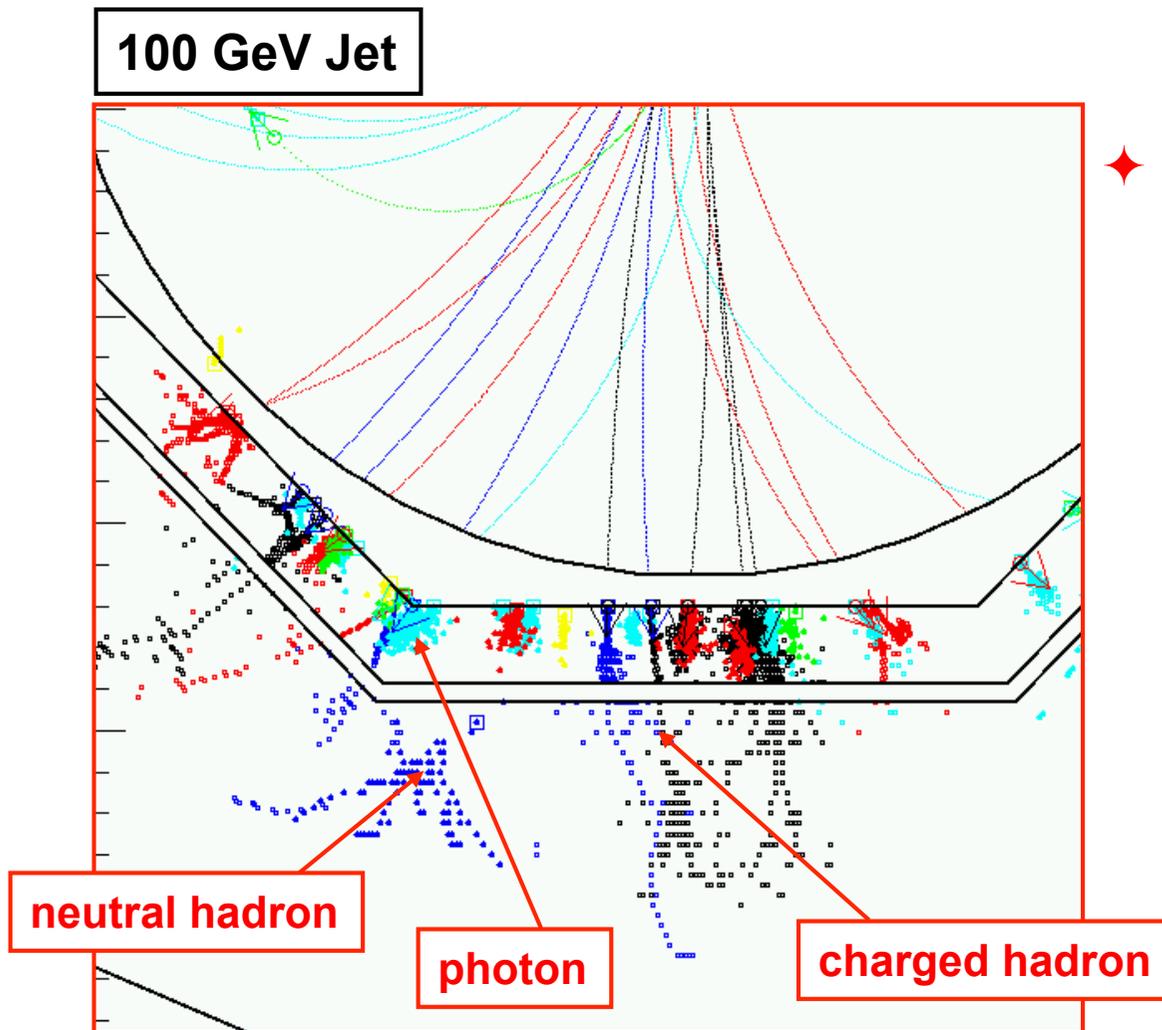
Iteratively Change clustering parameters until cluster splits and get sensible track-cluster match

+ (soon) plug in different clustering algorithms

NOTE:

- clustering “guided” by track momentum
- much more powerful than subtraction (Energy Flow)

The output... reconstructed particles



◆ If it all works...

- ◆ Reconstruct the **individual particles** in the event.
- ◆ Calorimeter energy resolution not critical: most energy in form of tracks.
- ◆ Level of mistakes in associating hits with particles, dominates jet energy resolution.

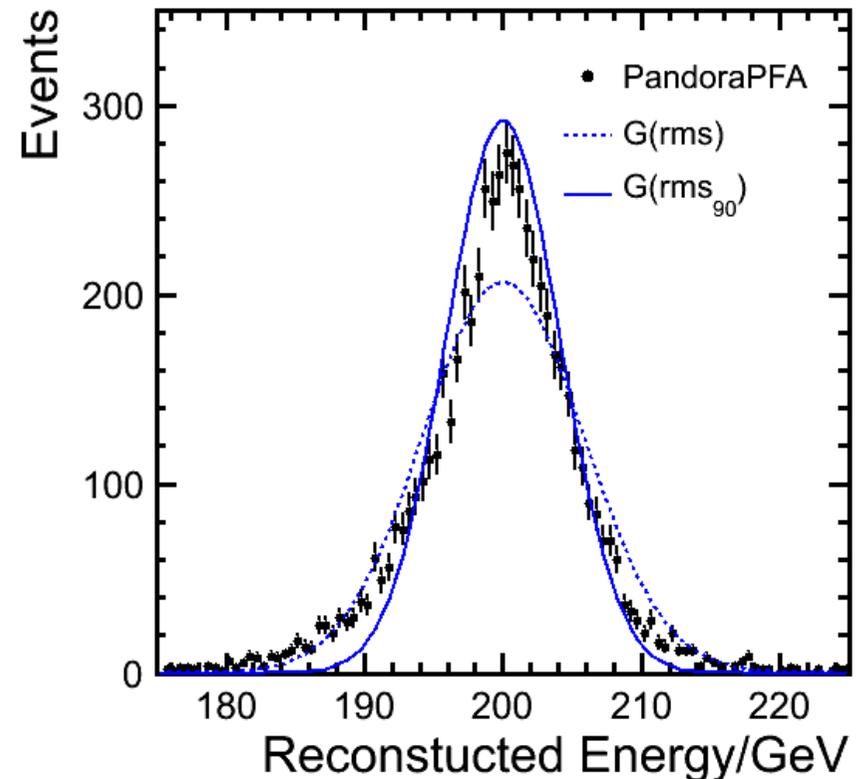
★ Can start to understand performance of a Particle Flow detector...

PFA Resolution: rms_{90}

- ★ PFA resolution is inherently non-Gaussian
 - resolution driven by number of mistakes (confusion)
 - leads to narrow core + tails
 - rms/Gaussian fits do not give representative resolution
 - instead use rms_{90}
 - defined as “rms in smallest region containing 90 % of events”

- ★ How to interpret rms_{90} ?
 - study analysing power

$$\text{rms}_{90} \approx 0.9\sigma_{\text{Gaus}}$$



Jet Energy Resolution

- ★ Recall, motivation for high granularity PFlow Calorimetry

Jet energy resolution: $\sigma_E/E < 3.5\%$

- ★ Current Pflow performance (PandoraPFA + ILD)
 - uds jets

E_{JET}	$\sigma_E/E = \alpha/\sqrt{E_{jj}}$ $ \cos\theta < 0.7$	σ_E/E_j
45 GeV	25.2 %	3.7 %
100 GeV	29.2 %	2.9 %
180 GeV	40.3 %	3.0 %
250 GeV	49.3 %	3.1 %

rms_{90}

- ★ Equivalent stochastic term shown for comparison, PFA resolution is not stochastic, **CONFUSION**

- ★ For 45 GeV jets, a factor three better than LEP best (ALEPH)
- ★ For ILC energies, Particle Flow Calorimetry has potential to deliver **unprecedented** jet energy resolution

Proof of Principle – PFA can deliver required performance

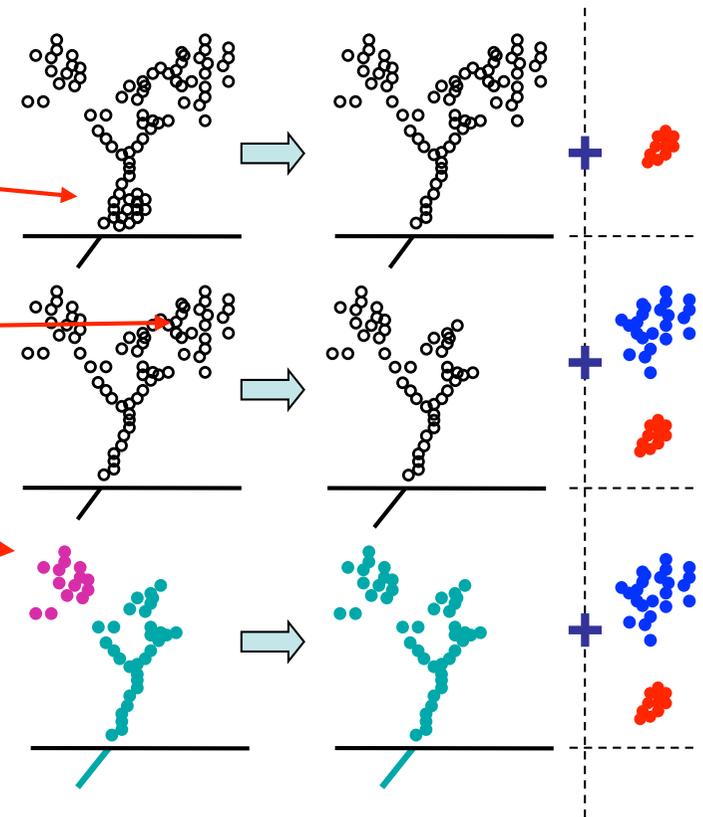
3 Understanding PFA Performance

What drives Particle Flow performance ?

- ★ Treat PFA reconstruction as a black box
- ★ Empirically determine contributions to jet energy resolution
- ★ Use MC to “cheat” various aspects of Particle Flow

PandoraPFA options:

- **PerfectPhotonClustering**
hits from photons clustered using MC info
and removed from main algorithm
- **PerfectNeutralHadronClustering**
hits from neutral hadrons clustered
using MC info...
- **PerfectFragmentRemoval**
after PandoraPFA clustering “fragments”
from charged tracks identified from MC and
added to charged track cluster
- **PerfectPFA**
perfect clustering and matching to tracks



- ★ Also consider leakage (non-containment) of hadronic showers

Contributions to resolution

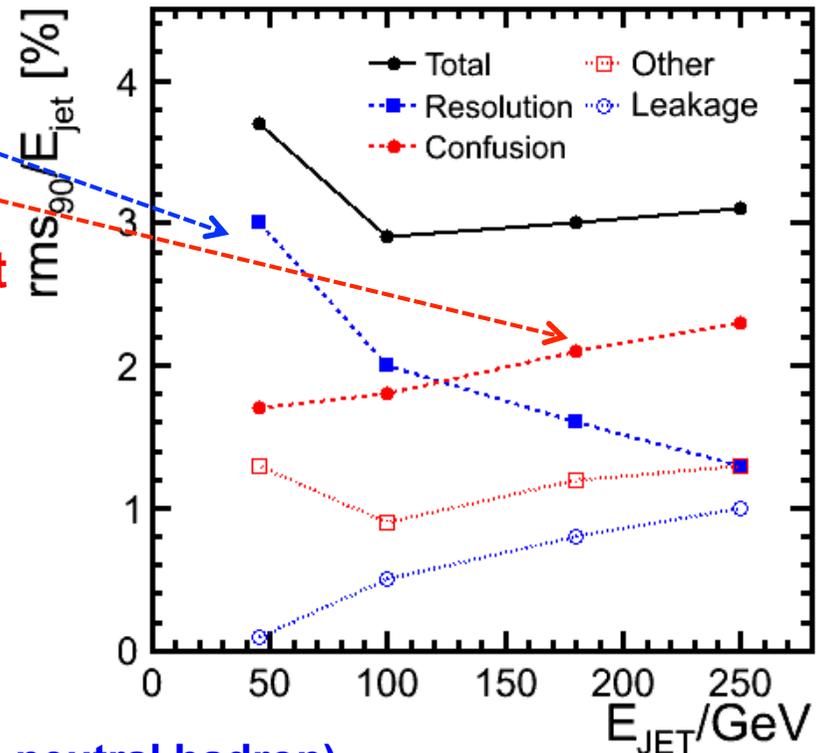
★ Answer depends on jet energy

- Low energy jets: **RESOLUTION**
- High energy jets: **CONFUSION**
- Cross-over at **~100 GeV**
- Very high energy jets: **leakage important**

★ What kind of confusion ?

- **i) photons**
(γ merged into charged had. shower)
- **ii) neutral hadrons**
(K_L/n merged into charged had. shower)
- **iii) charged hadron fragments**
(fragments of charged had. reconstructed as neutral hadron)

★ At high energies **ii)** is the largest contribution, e.g. for 250 GeV jets



Total Resolution	3.1 %
Confusion	2.3 %
i) Photons	1.3 %
ii) Neutral hadrons	1.8 %
iii) Charged hadrons	0.2 %

Not insignificant

Largest single contribution, but remember, enters in quadrature

4 Dependence on hadron shower simulation

- ★ Modelling of hadronic showers in GEANT4 is far from perfect...
 - Can we believe PFA results based on simulation ?
- ★ PandoraPFA/ILD performance for 5 **very** different Geant4 physics lists...

Physics List	Jet Energy Resolution				
	45 GeV	100 GeV	180 GeV	250 GeV	
LCPhys	3.74 %	2.92 %	3.00 %	3.11 %	← Default
QGSP_BERT	3.52 %	2.95 %	2.98 %	3.25 %	
QGS_BIC	3.51 %	2.89 %	3.12 %	3.20 %	
FTFP_BERT	3.68 %	3.10 %	3.24 %	3.26 %	
LHEP	3.87 %	3.15 %	3.16 %	3.08 %	← ~GHEISHA
χ^2	23.3 / 4	17.8 / 4	16.0 / 4	6.3 / 4	
rms	4.2 %	3.9 %	3.5 %	2.5 %	

- ★ Only a weak dependence < 5 %
 - NOTE: 5 % is on the total, not just the hadronic confusion term

e.g.

Total Resolution	3.11 %	→ ×1.05 →	Total Resolution	3.27 %
Conf: neutral hads	1.80 %	→ ×1.14 →	Conf: neutral hads	2.05 %
Other contributions	2.54 %	→ ×1.00 →	Other contributions	2.54 %

Suggests PFA performance is rather robust

- MC results likely to be reliable, despite shower model uncertainties

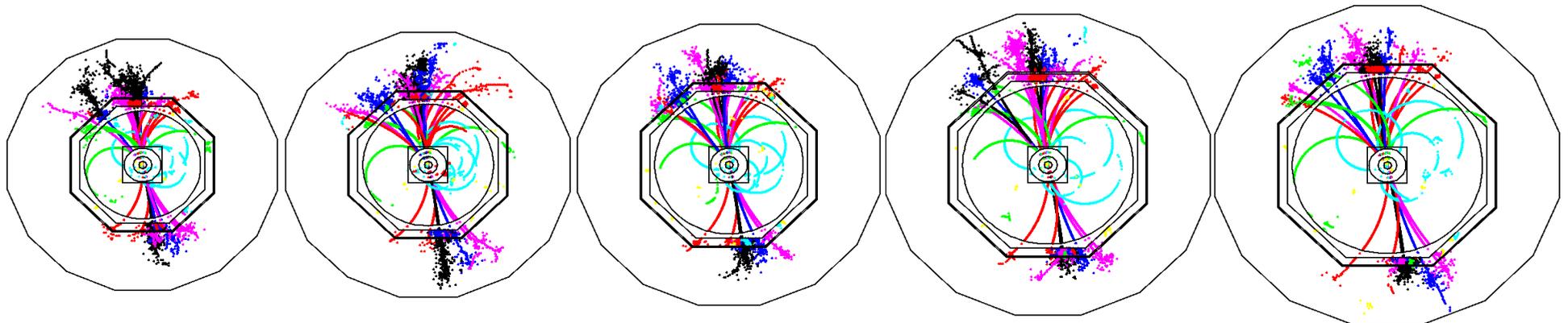
see talk of Oleg Markin (this p.m.) for CALICE data/MC comparisons

5 Optimising a Particle Flow Detector

Cost drivers:

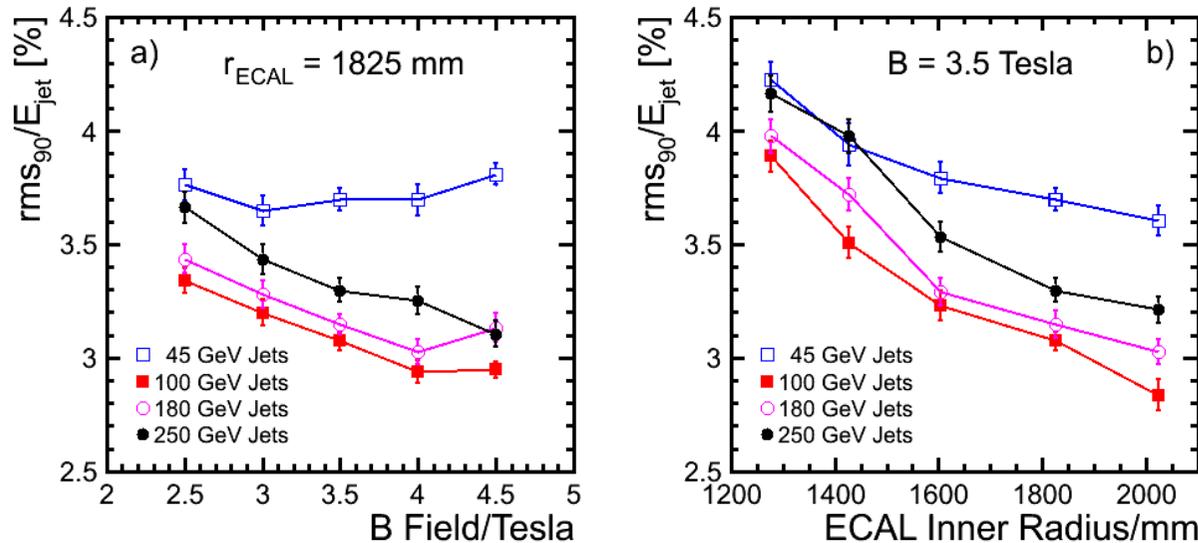
- Calorimeters and solenoid are the main cost drivers of an ILC detector optimised for particle flow
- Most important detector design considerations are:
 - ♦ B-field
 - ♦ R : inner radius of ECAL
 - ♦ L : length, equivalently aspect ratio L/R
 - ♦ HCAL thickness : number of interaction lengths
 - ♦ ECAL and HCAL segmentation
- Study jet energy resolution as a function of these cost critical issues

★ e.g. vary ECAL radius and B-field



B vs R

★ Empirically find (PandoraPFA/ILD)



$$\frac{\sigma_E}{E} = \frac{21}{\sqrt{E/\text{GeV}}} \oplus 0.7 \oplus 0.004E \oplus 2.1 \left(\frac{R}{1825} \right)^{-1.0} \left(\frac{B}{3.5} \right)^{-0.3} \left(\frac{E}{100} \right)^{+0.3} \%$$

Resolution
 Tracking
 Leakage
 Confusion

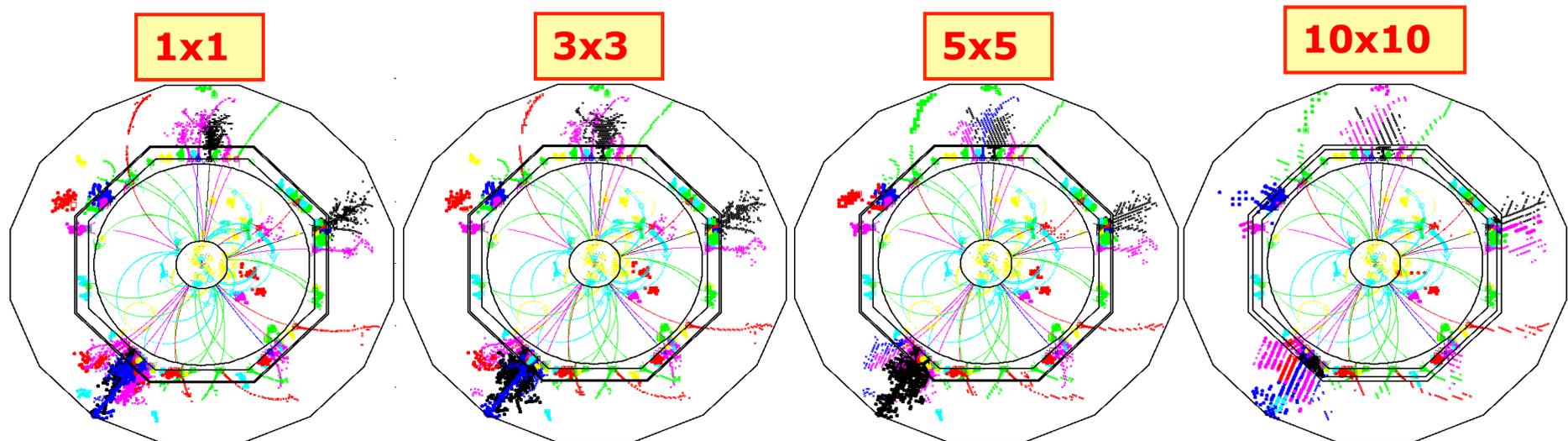
◆ Confusion $\propto B^{-0.3} R^{-1}$ (1/R dependence “feels right”, geometrical factor !)

Conclusions:

Detector should be fairly large
Very high B-field is less important

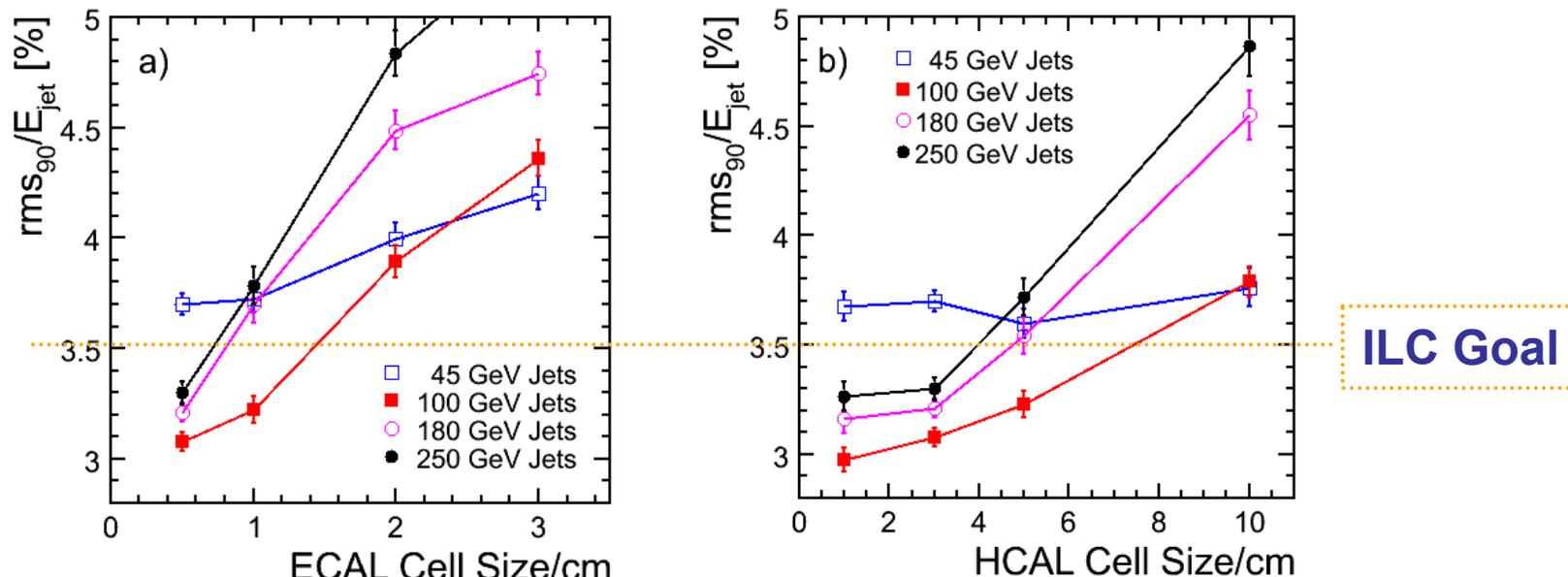
ECAL/HCAL Segmentation

- ★ Assumed particle flow reconstruction requires **very highly segmented ECAL and HCAL**
- ★ What does “highly segmented” mean ?
- ★ In ILD detector model vary **ECAL Si pixel size and HCAL tile size**
 - e.g. HCAL tile size [cm²]



- ★ “By eye” can see that pattern recognition becomes harder for 10x10 cm²
- ★ Dependence of jet energy resolution on segmentation obtained with full particle flow reconstruction

★ In ILD detector model vary **ECAL Si pixel size** and **HCAL tile size**



★ **ECAL Conclusions:**

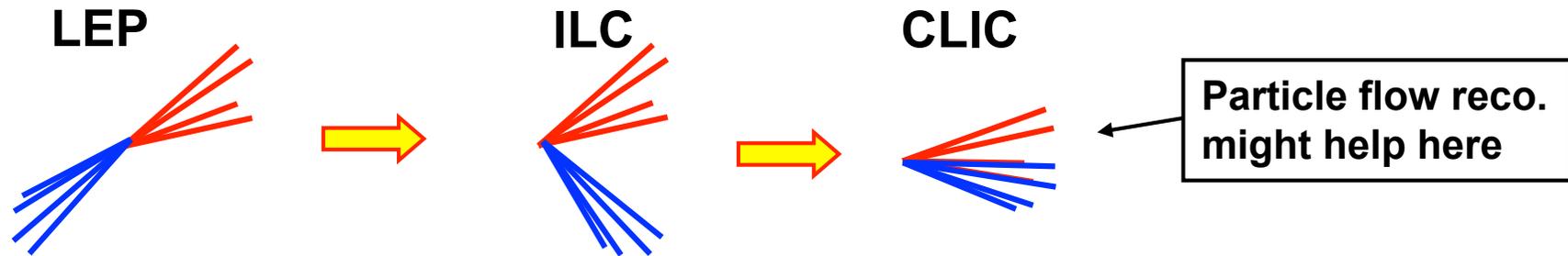
- Ability to resolve photons in **current PandoraPFA algorithm** strongly dependent on transverse cell size
- Require at least as fine as **10x10 mm²** to achieve **4.0 %** jet E resolution
- Significant advantages in going to **5x5 mm²**

★ **HCAL Conclusions:**

- For **current PandoraPFA algorithm** and for Scintillator HCAL, a tile size of **3x3 cm²** looks optimal
- May be different for a digital/semi-digital RPC based HCAL

7 PFA at high Energies

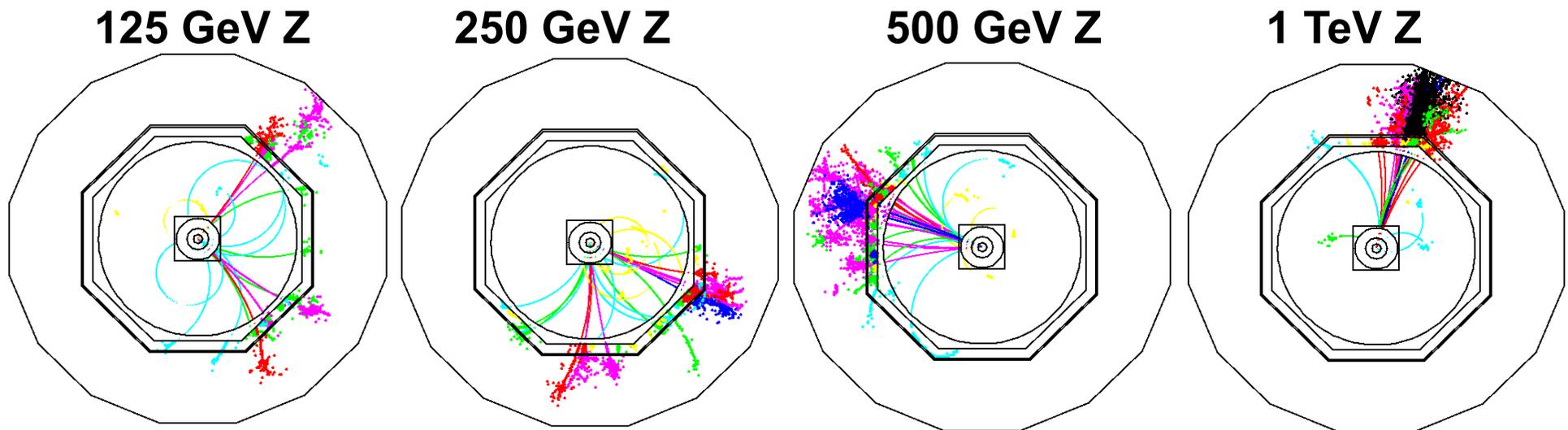
★ On-shell W/Z decay topology depends on energy:



★ A few comments:

- Particle multiplicity does not change
- Boost means higher particle density
- PFA could be better for “mono-jet” mass resolution

More confusion

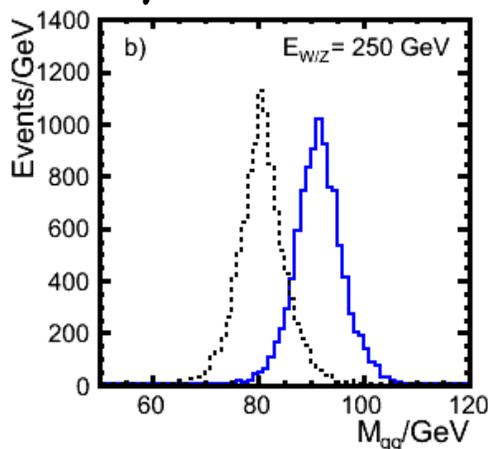
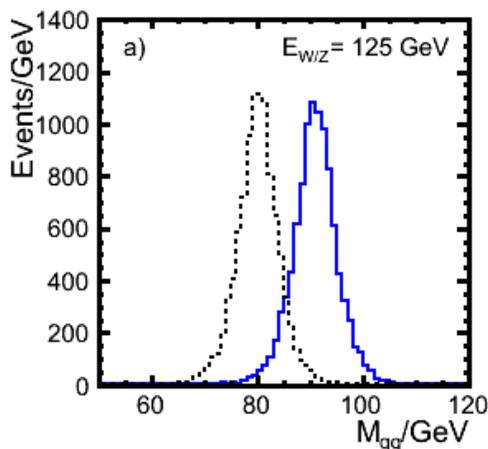


W/Z Separation at high Energies

★ Studied W/Z separation using **ILD⁺** (8 λ_1 HCAL) samples of

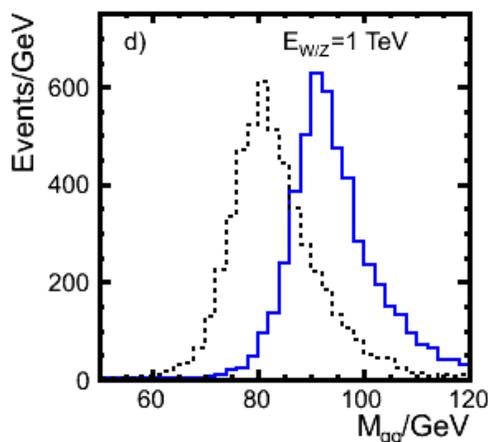
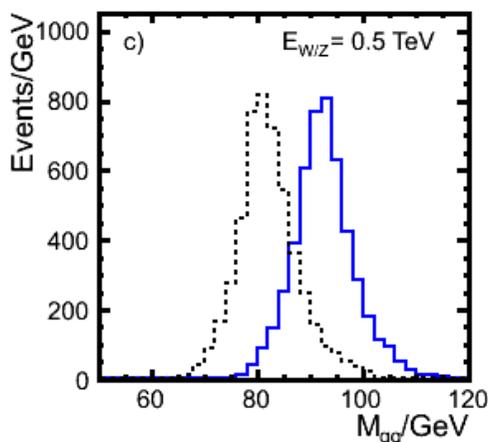
$$e^+e^- \rightarrow WW \rightarrow u\bar{d}\nu\mu$$

$$e^+e^- \rightarrow ZZ \rightarrow d\bar{d}\nu\bar{\nu}$$



ILC-like energies

Clear separation



CLIC-like energies

There is separation,
although less clear

- Current PandoraPFA/ILD⁺ gives good W/Z separation for 0.5 TeV bosons
- Still fair separation for 1 TeV bosons
- **NOTE** PandoraPFA not designed/tuned for such high energies

9 Conclusions

- ★ **High granularity calorimeters being “prototyped” by CALICE**
 - ✦ such a detector can be built (at a cost)
- ★ **Clear demonstration that PFA can deliver ILC performance goals**
 - excellent performance for both $\sqrt{s} = 500$ GeV and $\sqrt{s} = 1$ TeV
 - modelling uncertainties do not appear to be large
 - + remember, not yet reached ultimate PFA performance
- ★ **Have developed a reasonably good understanding of Particle Flow**
- ★ **Initial studies demonstrate the Particle Flow Calorimetry will work (at least to some extent) at $\sqrt{s} = 3$ TeV:**
 - For 375-500 GeV jets can achieve 3.2-3.5 % jet energy resolution
 - For 0.5-1.0 TeV achieve reasonable (2.1-1.5 σ) separation of W/Z bosons
 - But full reach at $\sqrt{s} = 3$ TeV needs significant algorithm devel.



Particle Flow can deliver unprecedented performance for the next LC

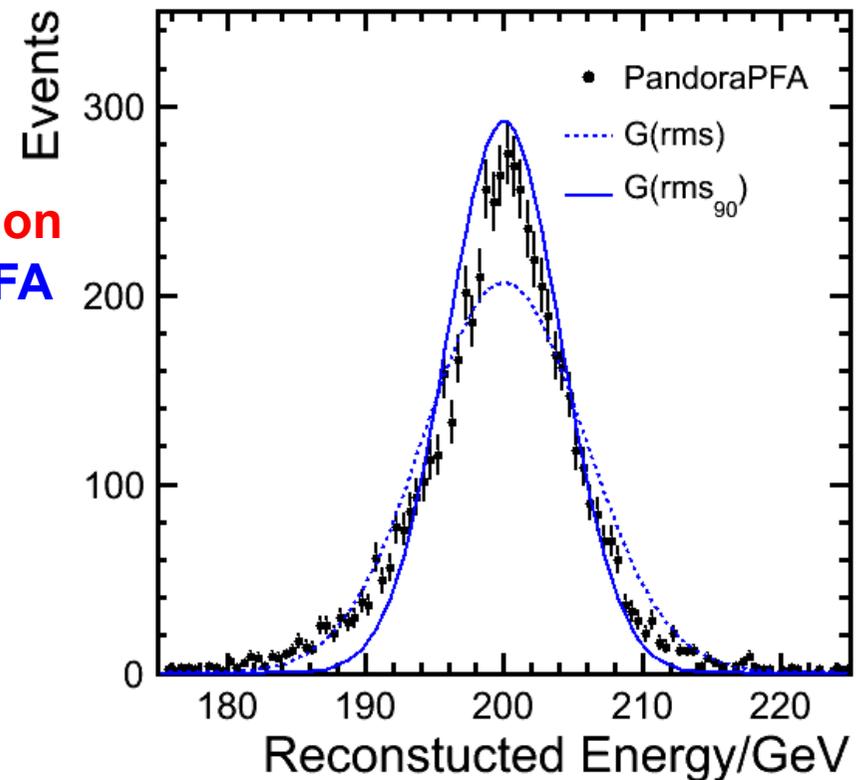
fin

Backup Slides

Backup: rms_{90}

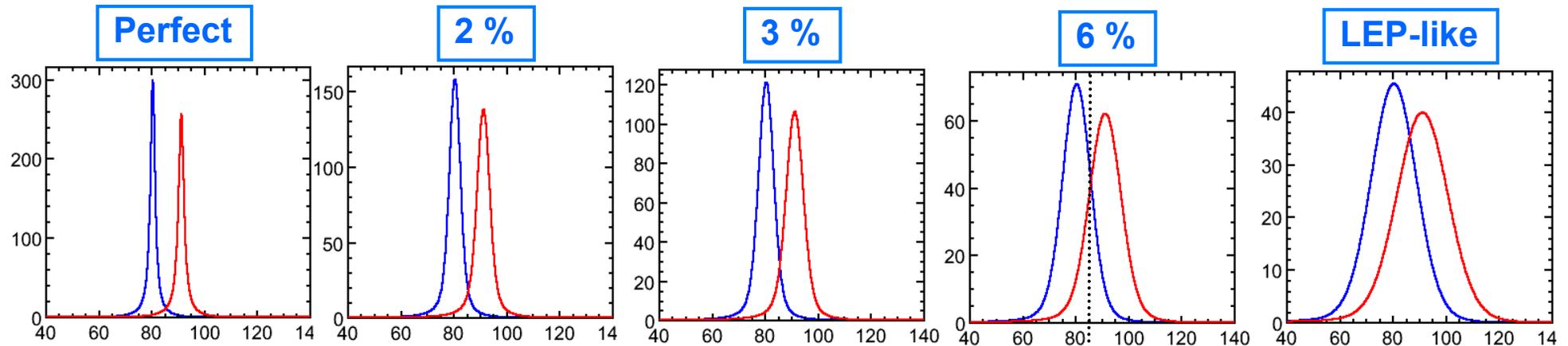
- ★ PFA resolution presented in terms of rms_{90}
 - defined as “rms in smallest region containing 90 % of events”
 - introduced to reduce sensitivity to tails in a well defined manner
 - in addition, PFA resolution is inherently non-Gaussian
- ★ How to interpret rms_{90} ? **With care...**
 - how to compare 4 GeV PFA rms_{90} with 5 GeV Gaussian resolution
- ★ For a **true** Gaussian distribution
 - $\text{rms}_{90} = 0.79 \sigma$
- ★ Highly mis-leading...
 - **distributions always have tails:**
“Gaussian” usually = fit to some region
 - rms_{90} larger than central peak from PFA
 - e.g. for 200 GeV di-jets (from rest):
 $\text{rms}(E) = 5.8 \text{ GeV}$
 $\text{rms}_{90}(E) = 4.1 \text{ GeV}$
fit to 196-205 GeV : 3.8 GeV
- ★ MC studies to determine equivalent statistical power show

$$\text{rms}_{90} \approx 0.9 \sigma_{\text{Gaus}}$$



Backup: requirements

- Gauge boson width sets “natural” goal for jet energy resolution

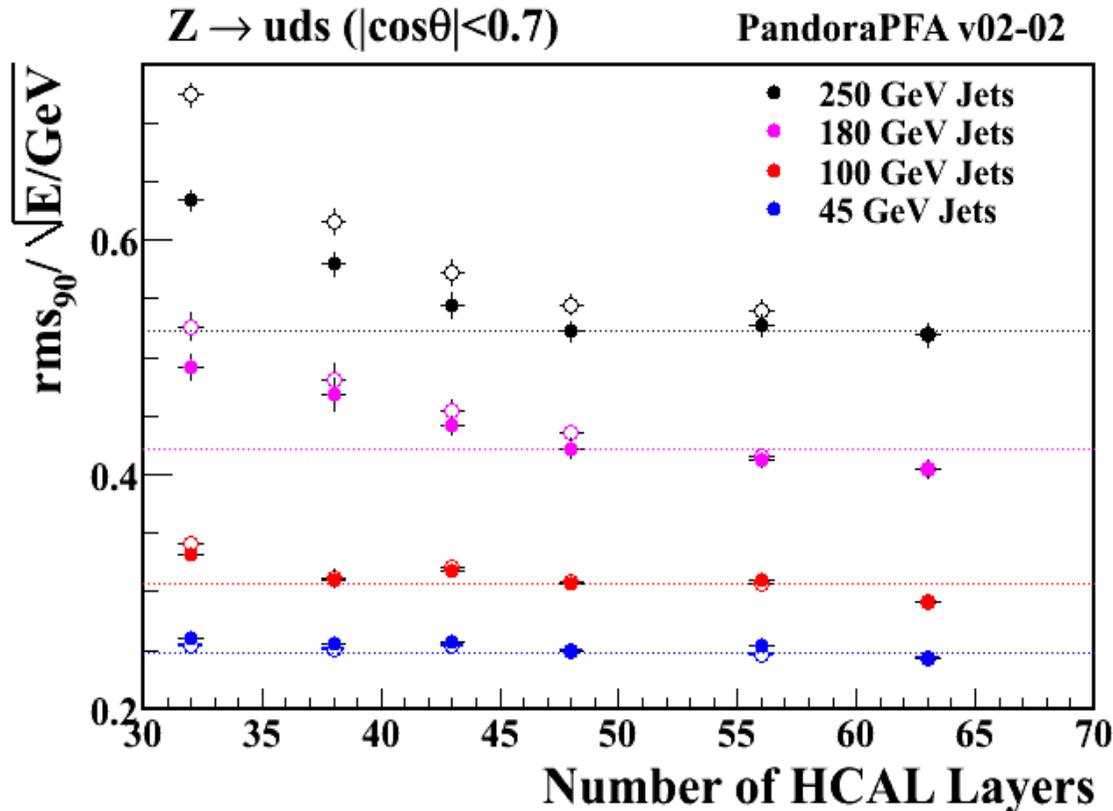


- Quantify by purity of W/Z samples

Jet E res.	Effic.	Back.	Eff*pur	W/Z sep
perfect	94 %	6 %	0.88	3.1 σ
2%	93 %	8 %	0.86	2.9 σ
3%	91 %	10 %	0.82	2.6 σ
4%	88 %	14 %	0.76	2.4 σ
5%	84 %	19 %	0.68	2.0 σ
10%	71 %	41 %	0.41	1.1 σ

Backup: HCAL Depth Results

- Open circles = no use of muon chambers as a “tail-catcher”
- Solid circles = including “tail-catcher”



HCAL Layers	λ_I	
	HCAL	+ECAL
32	4.0	4.8
38	4.7	5.5
43	5.4	6.2
48	6.0	6.8
63	7.9	8.7

ECAL : $\lambda_I = 0.8$

HCAL : λ_I includes scintillator

- ★ Little motivation for going beyond a 48 layer ($6 \lambda_I$) HCAL
- ★ Depends on Hadron Shower simulation
- ★ “Tail-catcher”: corrects ~50% effect of leakage, limited by thick solenoid

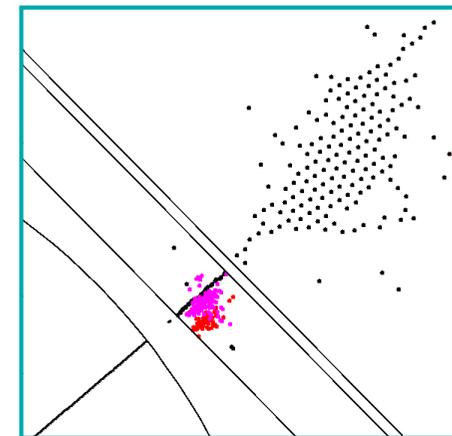
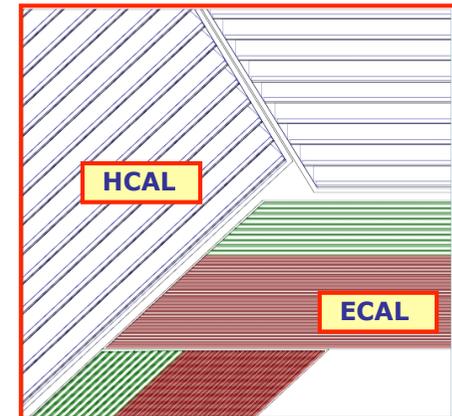
For 1 TeV machine “reasonable range” ~ 40 – 48 layers ($5 \lambda_I - 6 \lambda_I$)

Backup: Particle Flow ECAL considerations

★ **Require: high longitudinal and transverse segmentation**

★ **ECAL:**

- minimise transverse spread of EM showers
 - ➔ small Moliere radius
- transverse granularity ~ Moliere radius
- longitudinally separate EM and Hadronic showers
 - ➔ large ratio of λ_I/X_0
- longitudinal segmentation to cleanly ID EM showers



Material	X_0/cm	ρ_M/cm	λ_I/cm	X_0/λ_I
Fe	1.76	1.69	16.8	9.5
Cu	1.43	1.52	15.1	10.6
W	0.35	0.93	9.6	27.4
Pb	0.56	1.00	17.1	30.5

★ Favoured option : **Tungsten absorber**

◆ need to keep **sensitive material**

“thin” to maintain small ρ_M

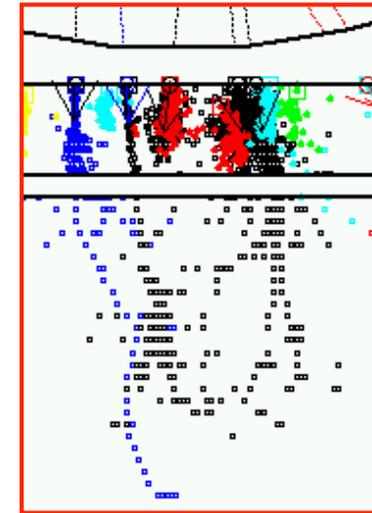


Backup: Particle Flow HCAL considerations

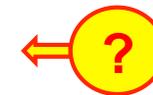
★ Require: high longitudinal and transverse segmentation

★ HCAL:

- resolve structure in hadronic showers
 - ⇒ longitudinal and transverse segmentation
- contain hadronic showers
 - ⇒ small λ_1
- HCAL will be large: absorber cost/structural properties important



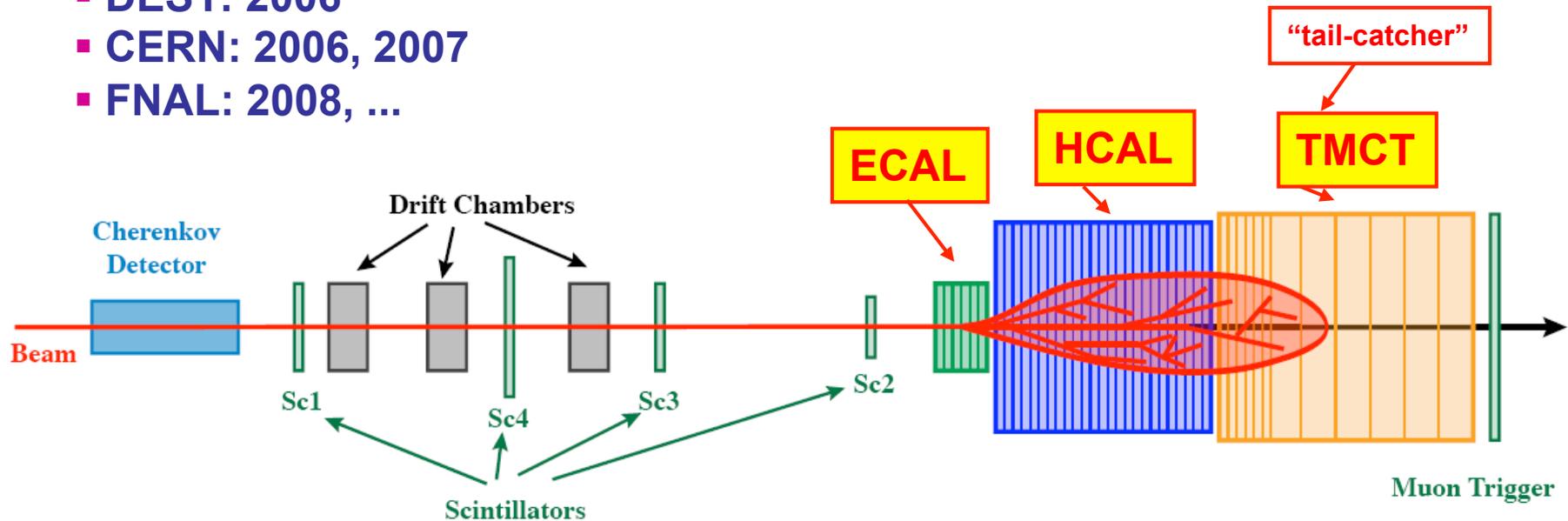
Material	X_0/cm	ρ_M/cm	λ_1/cm	X_0/λ_1
Fe	1.76	1.69	16.8	9.5
Cu	1.43	1.52	15.1	10.6
W	0.35	0.93	9.6	27.4
Pb	0.56	1.00	17.1	30.5



★ A number of technological options being studied (mainly) by the CALICE collab: CALorimetry for the LInear Collider Experiment

Backup: CALICE

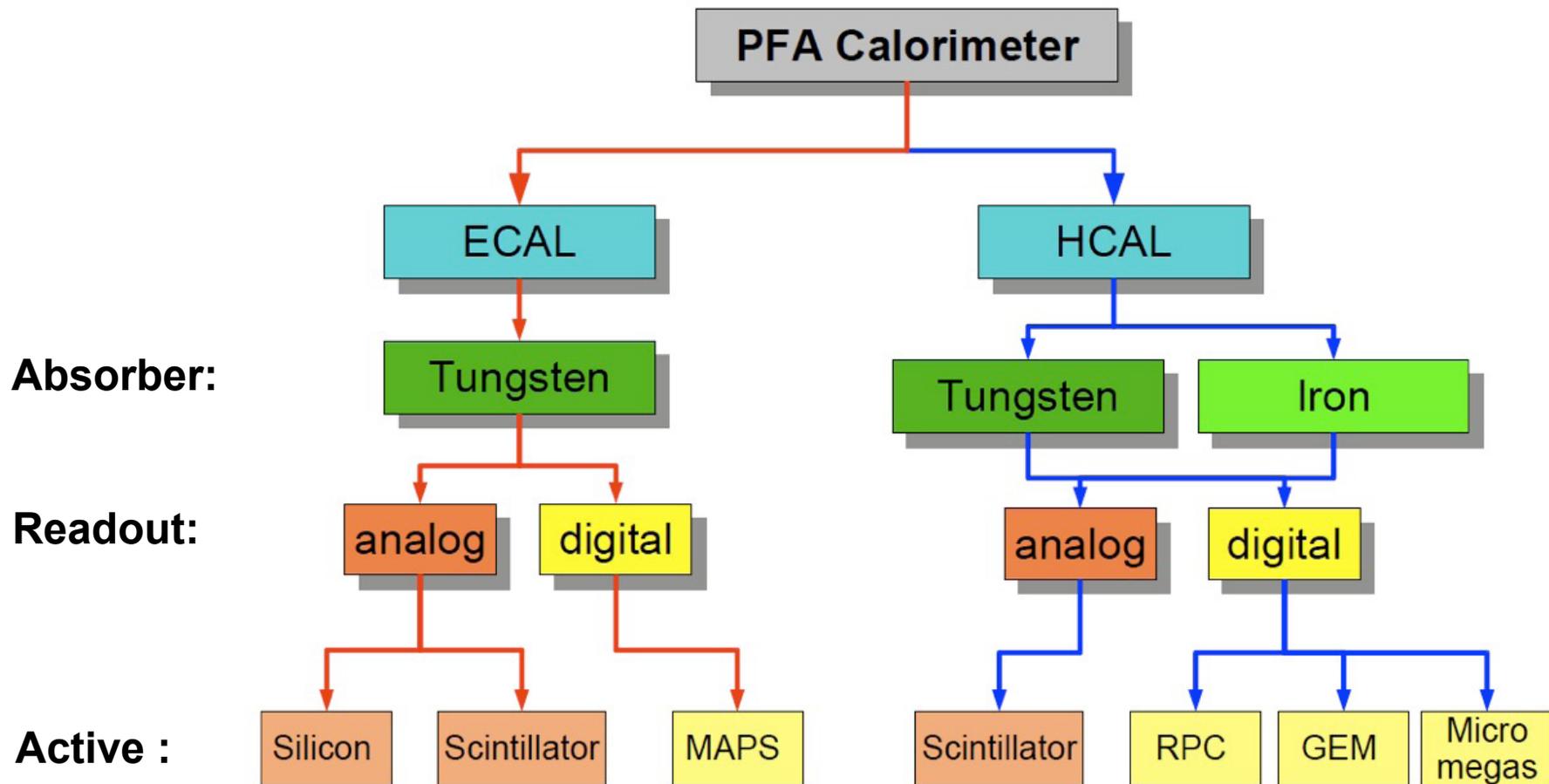
- ★ Approximately 330 scientists and engineers from 57 institutes in 17 countries (Africa, Americas, Asia, Europe)
- ★ Extensive test beam campaign
 - DESY: 2006
 - CERN: 2006, 2007
 - FNAL: 2008, ...



- ★ Wide variety of beam energies and particle species
 - 2 GeV to 80 GeV
 - muons, e^\pm , π^\pm , unseparated hadrons
- ★ Different technologies (to date 1 HCAL, 1 TCMT, 2 ECAL)

LC PFlow Calorimetry options

★ Various options for high granularity sampling calorimeters...



★ A number of interesting issues...

Backup: PandoraPFA Overview

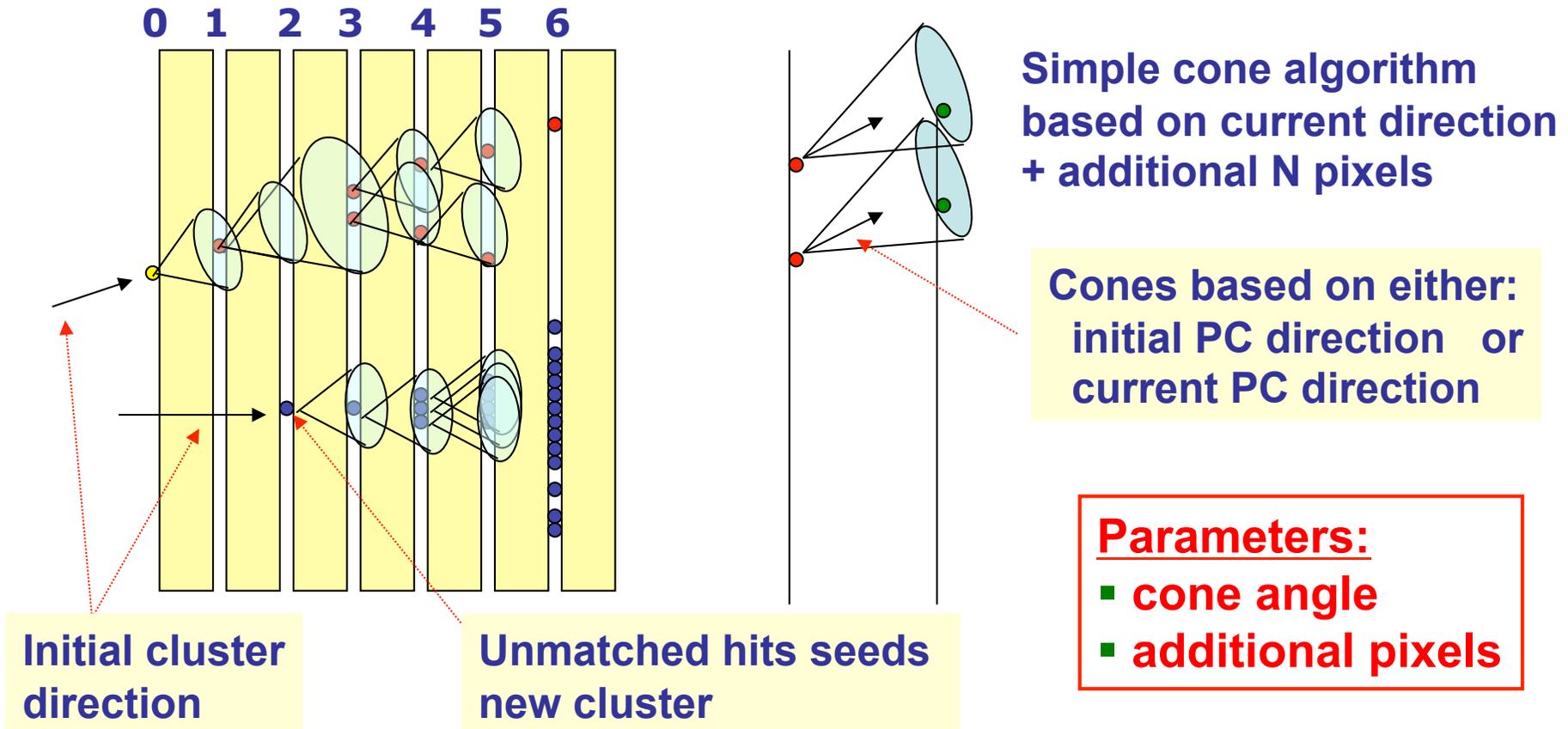
- ★ ECAL/HCAL reconstruction and PFA performed in a single algorithm
 - ★ Applicable to multiple detector concepts
 - ◆ Used to study conceptual designs
 - ★ Use **tracking** information to help **ECAL/HCAL** clustering
- ★ Fairly sophisticated algorithm : few x 10⁴ lines of code

Eight Main Stages:

- i. Track classification/extrapolation
- ii. Loose clustering in ECAL and HCAL
- iii. Topological linking of clearly associated clusters
- iv. Coarser grouping of clusters
- v. Iterative reclustering
- vi. Photon Identification/Recovery
- vii. Fragment removal
- viii. Formation of final Particle Flow Objects
(reconstructed particles)

ii) ECAL/HCAL Clustering

- ★ Tracks used to “seed” clusters
- ★ Start at inner layers and work outward
- ★ Associate hits with existing Clusters
- ★ If no association made form new Cluster
- ★ **Very simple** cone based algorithm



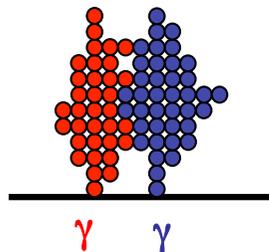
iii) Topological Cluster Association

- ✦ By design, clustering errs on side of caution
i.e. clusters tend to be split
- ✦ Philosophy: easier to put things together than split them up
- ✦ Clusters are then associated together in two stages:
 - 1) Tight cluster association – clear topologies
 - 2) Loose cluster association – fix what's been missed

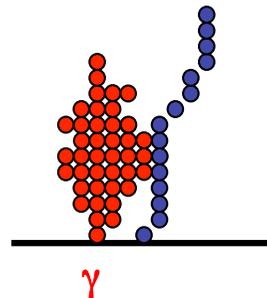
★ Photon ID

- ★ Photon ID plays important role
- ★ **Simple** “cut-based” photon ID applied to all clusters
- ★ Clusters tagged as photons are immune from association procedure – just left alone

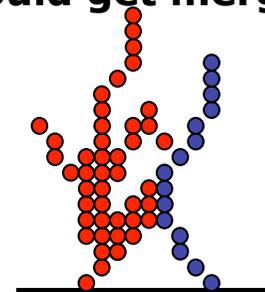
Won't merge



Won't merge



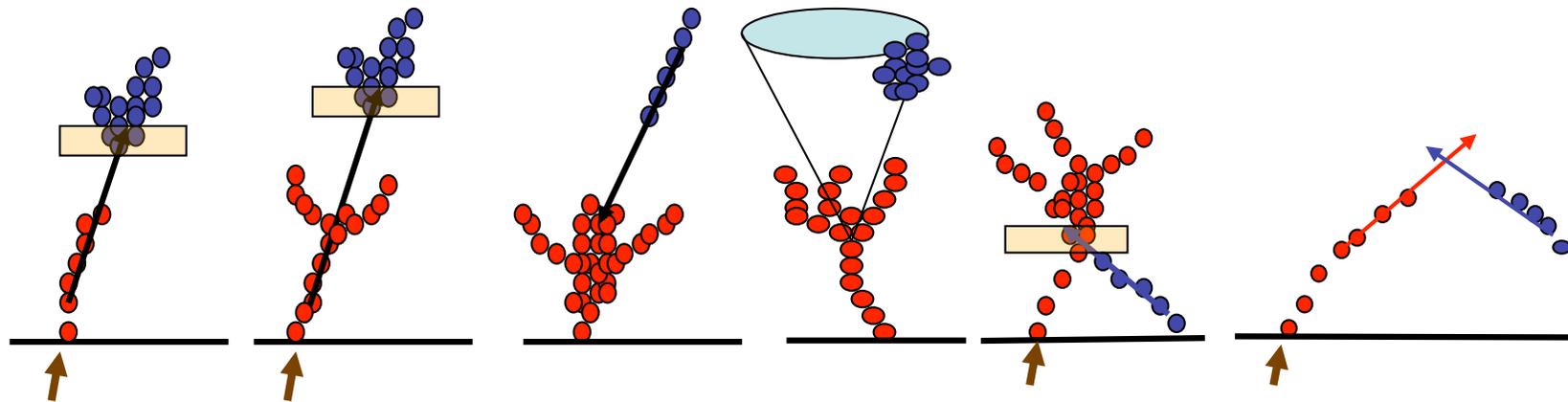
Could get merged



★ Clusters associated using a number of topological rules

Clear Associations:

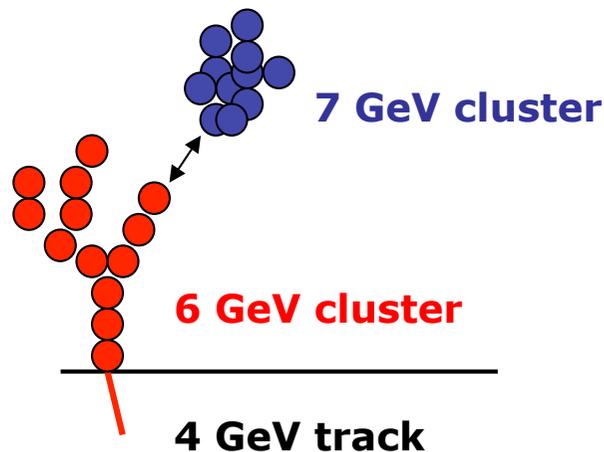
- Join clusters which are clearly associated making use of high granularity + tracking capability: **very few mistakes**



Less clear associations:

e.g.

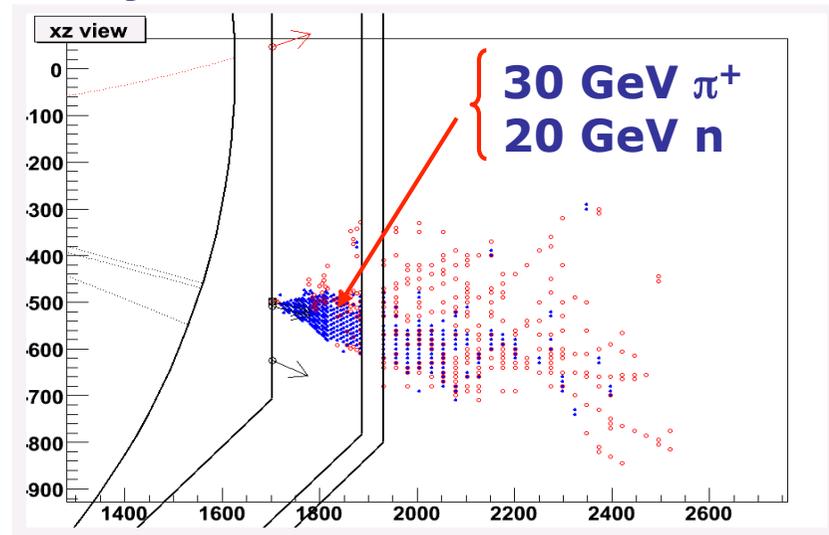
Proximity



Use E/p consistency to veto clear mistakes

v) Iterative Reclustering

- ★ At some point, in high density jets (high energies) reach the limit of “pure” particle flow
 - ◆ i.e. can't cleanly resolve neutral hadron in hadronic shower



The ONLY(?) way to address this is “statistically”



e.g. if have 30 GeV track pointing to 50 GeV cluster
SOMETHING IS WRONG

★ If track momentum and cluster energy inconsistent : **RECLUSTER**

e.g.



Change clustering parameters until cluster splits
and get sensible track-cluster match

NOTE:

- clustering guided by track momentum
- more powerful than subtraction (Energy Flow)

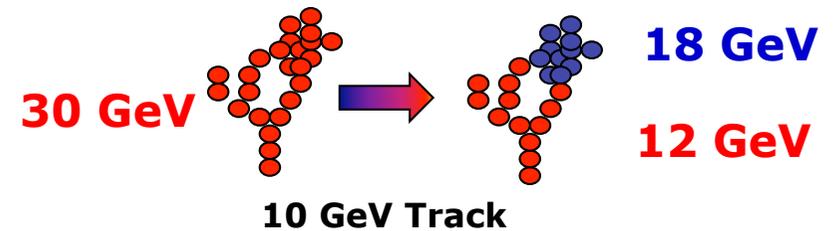
This is very important for higher energy jets

Iterative Reclustering Strategies

① Cluster splitting

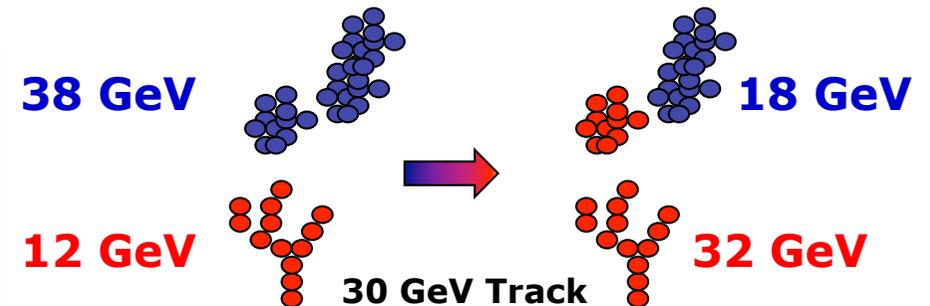
Reapply **entire** clustering algorithm to **hits** in “dubious” cluster. Iteratively reduce cone angle until cluster splits to give acceptable energy match to track

★ + plug in alternative clustering algorithms



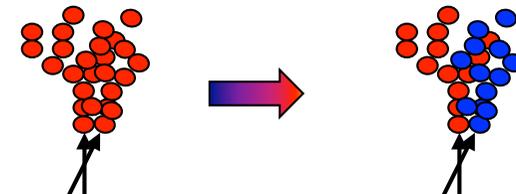
② Cluster merging with splitting

Look for clusters to add to a track to get sensible energy association. If necessary iteratively split up clusters to get good match.



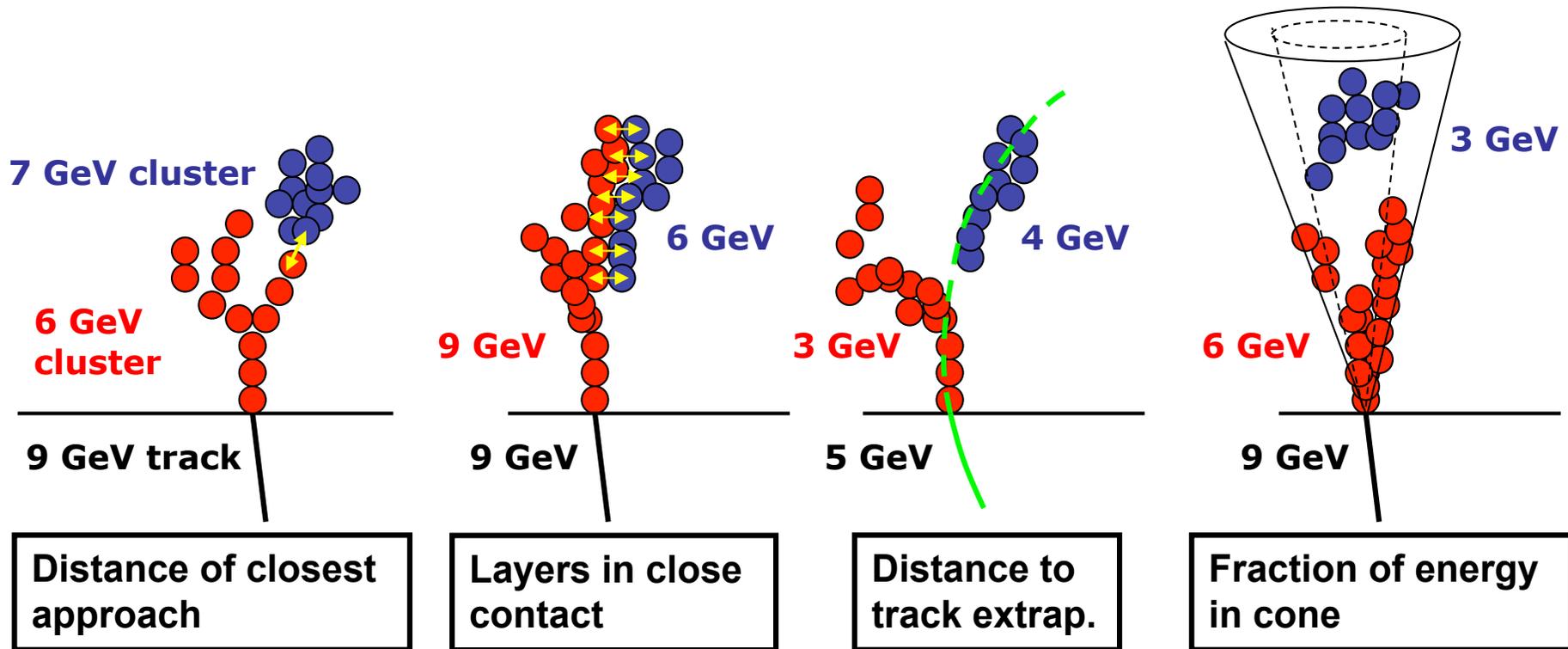
③ Track association ambiguities

In dense environment may have multiple tracks matched to same cluster. Apply above techniques to get ok energy match.



viii) Fragment removal : basic idea

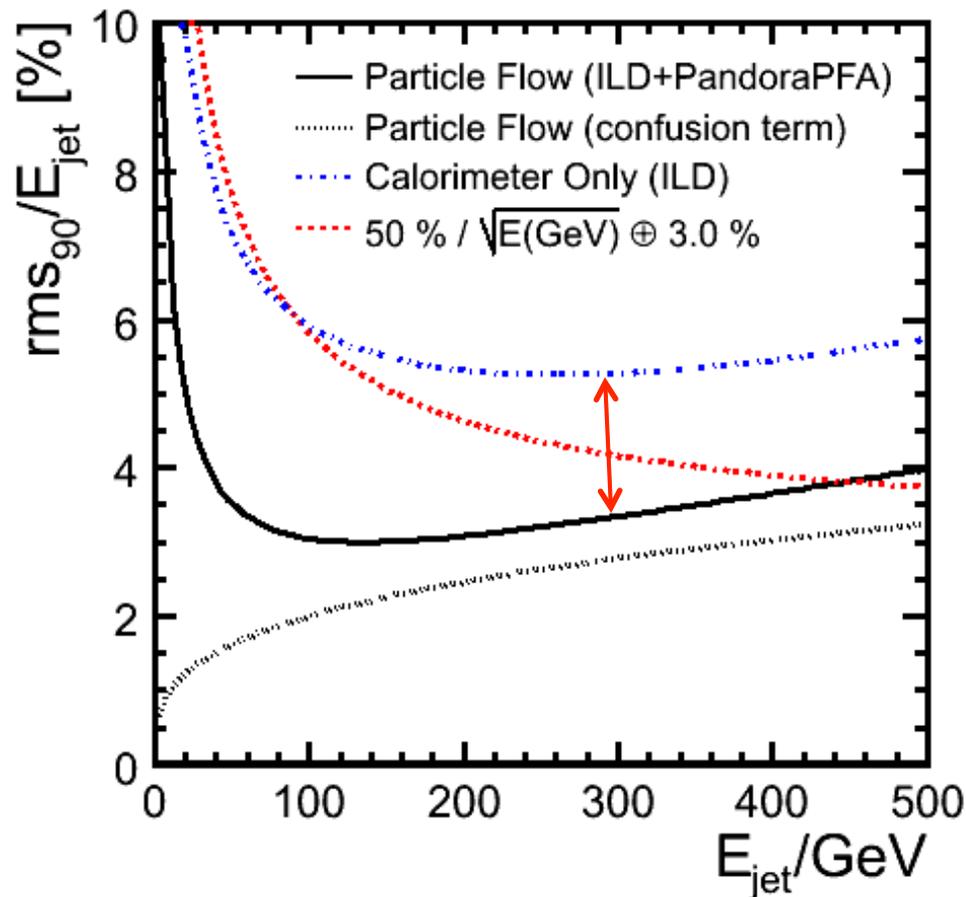
- ★ Look for “evidence” that a cluster is associated with another



- ★ Convert to a numerical evidence score E
- ★ Compare to another score “required evidence” for matching, R , based on change in E/p chi-squared, location in ECAL/HCAL etc.
- ★ If $E > R$ then clusters are merged
- ★ Rather *ad hoc* but works well – but works well

Backup: PFA vs Conventional Calorimetry

- ★ ILD detector concept intended for PFA. Also good conventional calorimeters
 - ◆ ECAL $\sim 15\%/\sqrt{E}$; HCAL $\sim 55\%/\sqrt{E}$
- ★ Interesting to compare PFA and pure energy sum with ILD and SiD



Comments:

- PandoraPFA: PFA **ALWAYS** wins over pure calorimetric
 - adding information...
- Confusion dominates at high E
- PandoraPFA/ILD: Resolution better than 4 % for $E_{JET} < 500$ GeV