

Fragmentation Functions of light charged hadrons

HEP phenomenology joint Cavendish-DAMTP seminar

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Outline

1 Fragmentation Functions: the basics

- ▶ factorisation, evolution
- ▶ higher-order corrections, theoretical constraints
- ▶ FF fits: why should we bother?
- ▶ are current FF sets good?

2 The NNFF1.0 analysis

- ▶ data set and fit settings
- ▶ the NNPDF methodology: parametrisation and uncertainty representation
- ▶ results: fit quality, perturbative stability, dependence on the data set/kinematic cuts
- ▶ is the NNFF1.0 set better than currently available sets?

3 Summary and outlook

- ▶ global fits, simultaneous fits

DISCLAIMER

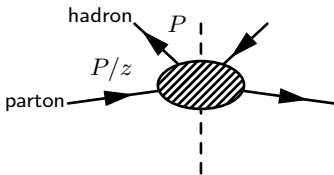
This is not a review talk on Fragmentation Functions
Focus on topics which I've worked on recently

[[JHEP 1503 \(2015\) 046](#); [EPJ C77 \(2017\) 516](#); [arXiv:1709.03400](#)]

1. Fragmentation Functions: the basics

Hadrons in the final state: Fragmentation Functions

FFs allow for a proper field-theoretic definition as matrix elements of bilocal operators



collinear transition
of a massless parton i
into a massless hadron h
with fractional momentum z
no local OPE \implies no lattice formulation
[Rev.Mod.Phys. 67 (1995) 157]

$$D_i^h(z) = \frac{1}{12\pi} \sum_X \int dy^- e^{-i\frac{P^+}{z}y^-} \text{Tr} [\gamma^+ \langle 0 | \psi(y) \mathcal{P} | h(P) X \rangle \langle h(P) X | \mathcal{P}' \bar{\psi}(0) | 0 \rangle]$$

with light-cone coordinates and appropriate gauge links \mathcal{P} , \mathcal{P}'

$$y = (y^+, y^-, \mathbf{y}_\perp), \quad y^+ = (y^0 + y^z)/\sqrt{2}, \quad y^- = (y^0 - y^z)/\sqrt{2}, \quad \mathbf{y}_\perp = (y^x, y^y)$$

All these definitions have ultraviolet divergences which must be renormalised
in order to define finite FFs to be used in the factorisation formulas
(FFs, like PDFs, are scheme dependent)

The definition above can be generalised to include longitudinal/transverse polarisations

Factorisation of physical observables [Adv.Ser.Direct.HEP 5 (1988) 1]

- 1 A variety of sufficiently inclusive processes allow for a factorised description

short-distance part
hard interaction of partons
process-dependent kernels

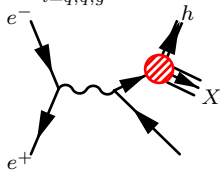
factorisation
← scheme & scale μ →

long-distance part
nucleon structure
universal PDFs/FFs

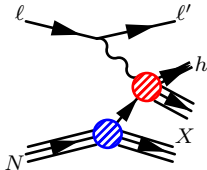
- 2 Physical observables are written as a convolution of coefficient functions and FFs

$$\mathcal{O}_I = \sum_{i=q,\bar{q},g} C_{Ii}(y, \alpha_s(\mu^2)) \otimes D_i(y, \mu^2) + \text{p.s. corrections}$$

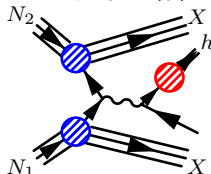
$$f \otimes g = \int_x^1 \frac{dy}{y} f\left(\frac{x}{y}\right) g(y)$$



$e^+ + e^- \rightarrow h + X$
single-inclusive
annihilation (SIA)



$l + N \rightarrow l' + h + X$
semi-inclusive deep-
inelastic scattering (SIDIS)



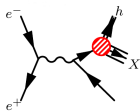
$N_1 + N_2 \rightarrow h + X$
high- p_T hadron production in
proton-proton collisions (PP)

- 3 Coefficient functions allow for a perturbative expansion

$$C_{If}(y, \alpha_s) = \sum_{k=0} a_s^k C_{If}^{(k)}(y), \quad a_s = \alpha_s / (4\pi)$$

- 4 After factorisation, all quantities (including FFs) depend on μ

Factorisation of physical observables

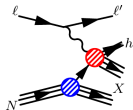


$e^+ + e^- \rightarrow h + X$
single-inclusive
annihilation (SIA)

$$\frac{d\sigma^h}{dz} = F_T^h(z, Q^2) + F_L^h(z, Q^2) = F_2^h(x, Q^2)$$

$$F_{k=T,L,2}^h = \frac{4\pi\alpha_{\text{em}}^2}{Q^2} \langle e^2 \rangle \left\{ D_{\Sigma}^h \otimes C_{k,q}^S + n_f D_g^h \otimes C_{k,g}^S + D_{\text{NS}}^h \otimes C_{k,q}^{\text{NS}} \right\}$$

up to NNLO [PLB 386 (1996) 422; NPB 487 (1997) 233; PLB 392 (1997) 207]



$l + N \rightarrow l' + h + X$
semi-inclusive deep-
inelastic scattering (SIDIS)

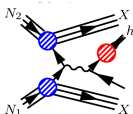
$$\frac{d\sigma^h}{dx dy dz} = \frac{2\pi\alpha_{\text{em}}^2}{Q^2} \left[\frac{1+(1-y)^2}{y} 2F_1^h + \frac{2(1-y)}{y} F_L^h \right]$$

$$2F_1^h = e_q^2 \left\{ q \otimes D_q^h + \frac{\alpha_s}{2\pi} \left[q \otimes C_{qq}^1 \otimes D_q^h + q \otimes C_{gq}^1 \otimes D_g^h + g \otimes C_{qg}^1 \otimes D_q^h \right] \right\}$$

$$F_L^h = \frac{\alpha_s}{2\pi} \sum_{q,\bar{q}} e_q^2 \left[q \otimes C_{qq}^L \otimes D_q^h + q \otimes C_{gq}^L \otimes D_g^h + g \otimes C_{qg}^L \otimes D_q^h \right]$$

up to NLO [NPB 160 (1979) 301; PRD 57 (1998) 5811]

partial NNLO [PRD 95 (2017) 034027]



$N_1 + N_2 \rightarrow h + X$
high- p_T hadron production
in pp collisions (PP)

$$E_h \frac{d^3\sigma}{dp_h^3} = \sum_{a,b,c} f_a \otimes f_b \otimes \hat{\sigma}_{ab}^c \otimes D_c^h$$

$$= \sum_{i,j,k} \int \frac{dx_a}{x_a} \int \frac{dx_b}{x_b} \int \frac{dz}{z^2} f^{i/p_a}(x_a) f^{j/p_b}(x_b) D^{h/k}(z) \hat{\sigma}^{ij \rightarrow k} \delta(\hat{s} + \hat{t} + \hat{u})$$

up to NLO [PRD 67 (2003) 054004; PRD 67 (2003) 054005]

Evolution of FFs: DGLAP equations [NPB 126 (1977) 298]

- ① A set of $(2n_f + 1)$ integro-differential equations (n_f =number of active flavours)

$$\frac{\partial}{\partial \ln \mu^2} D_i(x, \mu^2) = \sum_j^{n_f} \int_x^1 \frac{dz}{z} P_{ji}(z, \alpha_s(\mu^2)) D_j\left(\frac{x}{z}, \mu^2\right)$$

- ② Often written in a convenient basis of FFs

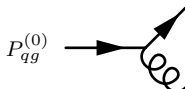
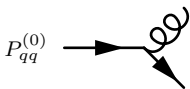
$$D_{\text{NS};\pm} = (D_q \pm D_{\bar{q}}) - (D_{q'} \pm D_{\bar{q}'}) \quad D_{\text{NS};v} = \sum_q^{n_f} (D_q - D_{\bar{q}}) \quad D_{\Sigma} = \sum_q^{n_f} (D_q + D_{\bar{q}})$$

$$\frac{\partial}{\partial \ln \mu^2} D_{\text{NS};\pm,v}(x, \mu^2) = P^{\pm,v}(x, \mu_F^2) \otimes D_{\text{NS};\pm,v}(x, \mu^2)$$

$$\frac{\partial}{\partial \ln \mu^2} \begin{pmatrix} D_{\Sigma}(x, \mu^2) \\ D_g(x, \mu^2) \end{pmatrix} = \begin{pmatrix} P^{qq} & 2n_f P^{gq} \\ \frac{1}{2n_f} P^{qg} & P^{gg} \end{pmatrix} \otimes \begin{pmatrix} D_{\Sigma}(x, \mu^2) \\ D_g(x, \mu^2) \end{pmatrix}$$

- ③ With perturbative computable (time-like) splitting functions

$$P_{ji}(z, \alpha_s) = \sum_{k=0} a_s^{k+1} P_{ji}^{(k)}(z), \quad a_s = \alpha_s / (4\pi)$$



Splitting functions: LO and NLO

$$P_{qq}^{(0)}(x) = C_F(2p_{qq}(x) + 3\delta(1-x))$$

$$P_{ps}^{(0)}(x) = 0$$

$$P_{qg}^{(0)}(x) = 2n_f p_{qg}(x)$$

$$P_{gg}^{(0)}(x) = 2C_F p_{gg}(x)$$

$$P_{ss}^{(0)}(x) = C_A(4p_{ss}(x) + \frac{11}{3}\delta(1-x)) - \frac{2}{3}n_f\delta(1-x)$$

LO: 1973

$$P_{ss}^{(1)+}(x) = 4C_A C_F \left(p_{qq}(x) \left[\frac{67}{18} - \zeta_2 + \frac{11}{6}H_0 + H_{0,0} \right] + p_{qq}(-x) \left[\zeta_2 + 2H_{-1,0} - H_{0,0} \right] \right. \\ \left. + \frac{14}{3}(1-x) + \delta(1-x) \left[\frac{17}{24} + \frac{11}{3}\zeta_2 - 3\zeta_3 \right] \right) - 4C_F n_f \left(p_{qq}(x) \left[\frac{5}{6} + \frac{1}{3}H_0 \right] + \frac{2}{3}(1-x) \right) \\ + \delta(1-x) \left[\frac{1}{12} + \frac{2}{3}\zeta_2 \right] + 4C_F^2 \left(2p_{qq}(x) \left[H_{1,0} - \frac{3}{4}H_0 + H_2 \right] - 2p_{qq}(-x) \left[\zeta_2 + 2H_{-1,0} \right. \right. \\ \left. \left. - H_{0,0} \right] - (1-x) \left[1 - \frac{3}{2}H_0 \right] - H_0 - (1+x)H_{0,0} + \delta(1-x) \left[\frac{3}{8} - 3\zeta_2 + 6\zeta_3 \right] \right)$$

$$P_{ss}^{(1)-}(x) = P_{ss}^{(1)+}(x) + 16C_F \left(C_F - \frac{C_A}{2} \right) \left(p_{qq}(-x) \left[\zeta_2 + 2H_{-1,0} - H_{0,0} \right] - 2(1-x) \right. \\ \left. - (1+x)H_0 \right)$$

$$P_{ps}^{(1)}(x) = 4C_F n_f \left(\frac{20}{9} \frac{1}{x} - 2 + 6x - 4H_0 + x^2 \left[\frac{8}{3}H_0 - \frac{56}{9} \right] + (1+x) \left[5H_0 - 2H_{0,0} \right] \right)$$

$$P_{qg}^{(1)}(x) = 4C_A n_f \left(\frac{20}{9} \frac{1}{x} - 2 + 25x - 2p_{qg}(-x)H_{-1,0} - 2p_{qg}(x)H_{1,1} + x^2 \left[\frac{44}{3}H_0 - \frac{218}{9} \right] \right. \\ \left. + 4(1-x) \left[H_{0,0} - 2H_0 + xH_1 \right] - 4\zeta_2 x - 6H_{0,0} + 9H_0 \right) + 4C_F n_f \left(2p_{qg}(x) \left[H_{1,0} + H_{1,1} + H_2 \right. \right. \\ \left. \left. - \zeta_2 \right] + 4x^2 \left[H_0 + H_{0,0} + \frac{5}{2} \right] + 2(1-x) \left[H_0 + H_{0,0} - 2xH_1 + \frac{29}{4} \right] - \frac{15}{2} - H_{0,0} - \frac{1}{2}H_0 \right)$$

$$P_{gg}^{(1)}(x) = 4C_A C_F \left(\frac{1}{x} + 2p_{gg}(x) \left[H_{1,0} + H_{1,1} + H_2 - \frac{11}{6}H_1 \right] - x^2 \left[\frac{8}{3}H_0 - \frac{44}{9} \right] + 4\zeta_2 - 2 \right. \\ \left. - 7H_0 + 2H_{0,0} - 2H_1 x + (1+x) \left[2H_{0,0} - 5H_0 + \frac{37}{9} \right] - 2p_{gg}(-x)H_{-1,0} \right) - 4C_F n_f \left(\frac{2}{3}x \right. \\ \left. - p_{gg}(x) \left[\frac{2}{3}H_1 - \frac{10}{9} \right] \right) + 4C_F^2 \left(p_{gg}(x) \left[3H_1 - 2H_{1,1} \right] + (1+x) \left[H_{0,0} - \frac{7}{2} + \frac{7}{2}H_0 \right] - 3H_{0,0} \right. \\ \left. + 1 - \frac{3}{2}H_0 + 2H_1 x \right)$$

$$P_{ss}^{(1)}(x) = 4C_A n_f \left(1 - x - \frac{10}{9}p_{ss}(x) - \frac{13}{9} \left(\frac{1}{x} - x^2 \right) - \frac{2}{3}(1+x)H_0 - \frac{2}{3}\delta(1-x) + 4C_A^2 \left(27 \right. \right. \\ \left. \left. + (1+x) \left[\frac{11}{3}H_0 + 8H_{0,0} - \frac{27}{2} \right] + 2p_{ss}(-x) \left[H_{0,0} - 2H_{-1,0} - \zeta_2 \right] - \frac{67}{9} \left(\frac{1}{x} - x^2 \right) - 12H_0 \right. \right. \\ \left. \left. - \frac{44}{3}x^2 H_0 + 2p_{ss}(x) \left[\frac{67}{18} - \zeta_2 + H_{0,0} + 2H_{1,0} + 2H_2 \right] + \delta(1-x) \left[\frac{8}{3} + 3\zeta_3 \right] \right) + 4C_F n_f \left(2H_0 \right. \right. \\ \left. \left. + \frac{21}{3x} + \frac{10}{3}x^2 - 12 + (1+x) \left[4 - 5H_0 - 2H_{0,0} \right] \right)$$

NLO: 1980

Splitting functions: NNLO

$$P_{q\bar{q}}^{(2)} = 10C_A^2 P_{q\bar{q}}^{(2)} + 2C_A C_F P_{q\bar{q}}^{(2)} + \dots$$

$$P_{q\bar{q}}^{(2)} = \dots$$

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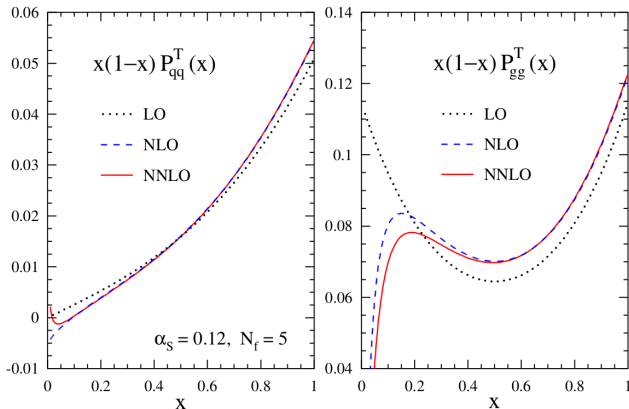
$$P_{q\bar{q}}^{(2)} = \dots$$

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NNLO:2012

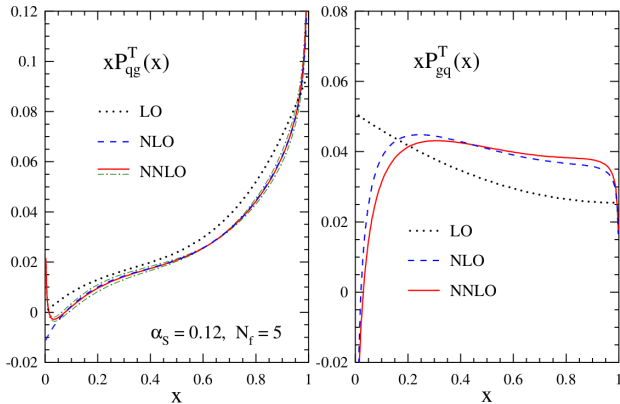
Properties of splitting functions

- 1 At LO [*Sov. J. Nucl. Phys.* 15 (1973) 438; *NPB* 126 (1977) 298; *NPB* 136 (1978) 445]
time-like and space-like splitting functions are equal, provided $P_{qq}^{S,(0)} \leftrightarrow P_{qq}^{T,(0)}$
- 2 At NLO [*NPB* 175 (1980) 27, *PLB* 97 (1980) 497, *PRD* 48 (1993) 116]
time-like and space-like splitting functions are related by analytic continuation
- 3 at NNLO [*PLB* 638 (2006) 61, *PLB* 659 (2008) 290, *NPB* 854 (2012) 133]
an uncertainty still remains on the exact form of $P_{qq}^{(2)}$ (it does not affect its log behavior)



Properties of splitting functions

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Properties of splitting functions

Must be careful with fixed-order splitting functions as $z \rightarrow 0$ ($m = 1, \dots, 2k + 1$)

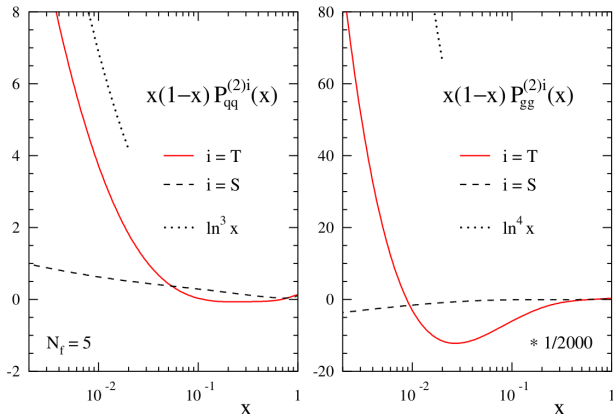
SPACE-LIKE CASE

$$P_{ji} \propto \frac{a_s^{k+1}}{x} \log^{k+1-m} \frac{1}{x}$$

TIME-LIKE CASE

$$P_{ji} \propto \frac{a_s^{k+1}}{z} \log^{2(k+1)-m-1} z$$

Soft gluon logarithms diverge more rapidly in the TL case than in the SL case: as z decreases, the unresummed SGLs spoil the convergence of the FO series for $P(z, a_s)$ if $\log \frac{1}{z} \geq \mathcal{O}(a_s^{-1/2})$



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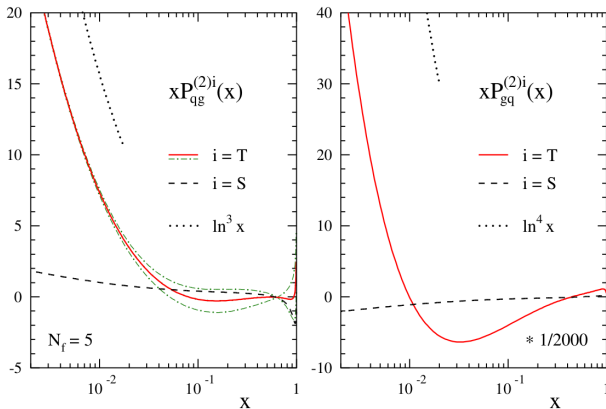
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Theoretical constraints

1 Momentum sum rule

$$\sum_h \int_0^1 dz z D_i^h(z, \mu^2) = 1 \quad \forall \text{ parton } i$$

2 Charge sum rule

$$\sum_h \int_0^1 dz e_h D_i^h(z, \mu^2) = e_i \quad \forall \text{ parton } i$$

where $e_{h(i)}$ is the electric charge of the hadron h (parton i)

3 Charge conjugation symmetry

$$D_{q(\bar{q})}^{h^+} = D_{\bar{q}(q)}^{h^-} \quad D_g^{h^+} = D_g^{h^-} \quad \forall \text{ hadron species } h^\pm$$

4 Isospin symmetry of the strong interaction

$$D_u^{\pi^+} = D_d^{\pi^-} \quad D_d^{\pi^+} = D_u^{\pi^-}$$

approximate, as $m_u \sim m_d$, but no phenomenological evidences of violation

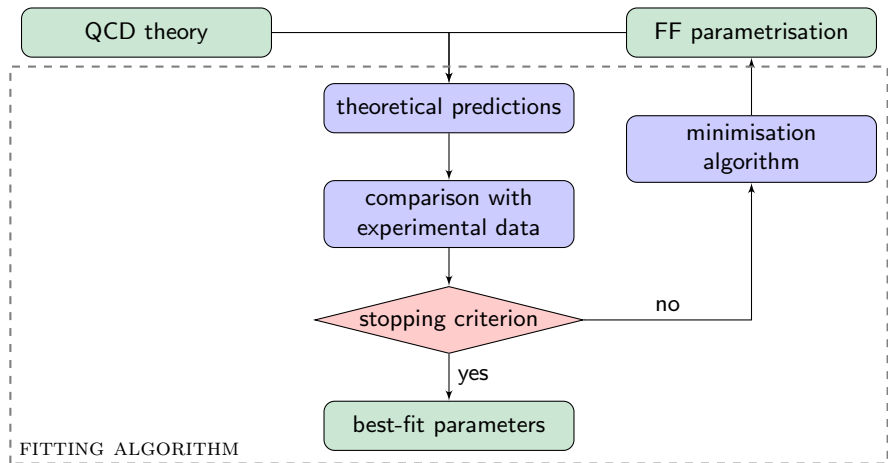
5 Positivity of cross sections

implies that FFs should be positive-definite at LO

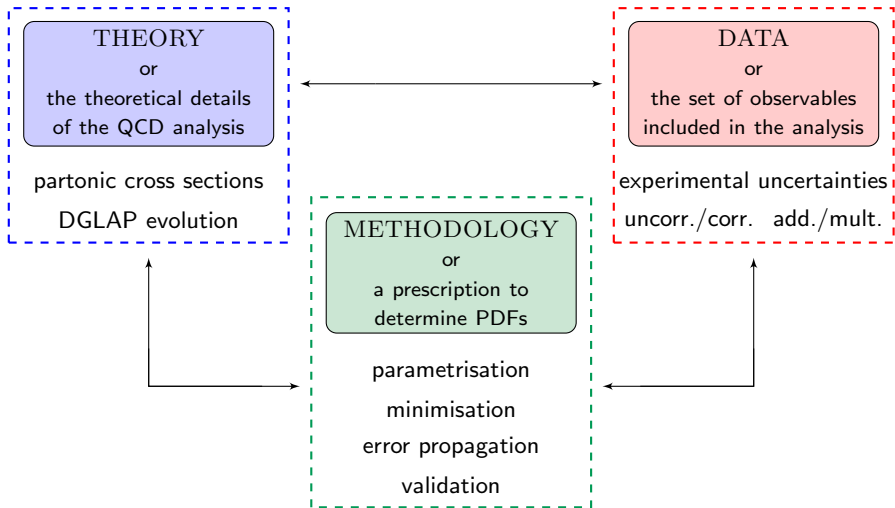
Determining FFs from data: a (global) QCD analysis

Determine the probability density $\mathcal{P}[D]$ in the space of FFs $[D]$

$$\langle \mathcal{O}[D] \rangle = \int \mathcal{D}D \mathcal{P}[D] \mathcal{O}[D] \quad \sigma_{\mathcal{O}}[D] = \left[\int \mathcal{D}D \mathcal{P}[D] (\mathcal{O}[D] - \langle \mathcal{O}[D] \rangle)^2 \right]^{1/2}$$



A global QCD analysis: the ingredients we need



Each of these ingredients is a source of uncertainty in the FF determination

Available FF sets (status 2017)

		DHESS	HKNS	JAM	NNFF
DATA	SIA	✓	✓	✓	✓
	SIDIS	✓	✗	✗	✗
	PP	✓	✗	✗	✓
METH.	statistical treatment	Iterative Hessian 68% - 90%	Hessian $\Delta\chi^2 = 15.94$	Monte Carlo	Monte Carlo
	parametrisation	standard	standard	standard	neural network
THEORY	pert. order	(N)NLO	NLO	NLO	LO, NLO, NNLO
	HF scheme	ZM(GM)-VFN	ZM-VFN	ZM-VFN	ZM-VFN
	hadron species	$\pi^\pm, K^\pm, p/\bar{p}, h^\pm$	$\pi^\pm, K^\pm, p/\bar{p}$	π^\pm, K^\pm	$\pi^\pm, K^\pm, p/\bar{p}$
latest update	PRD 91 (2015) 014035 PRD 95 (2017) 094019	PTEP 2016 (2016) 113B04	PRD 94 (2016) 114004	EPJ C77 (2017) 516	

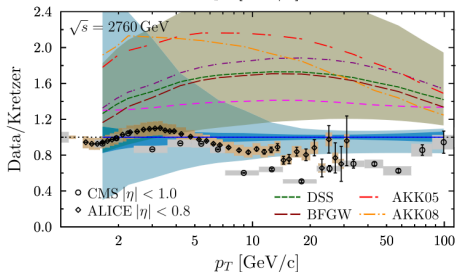
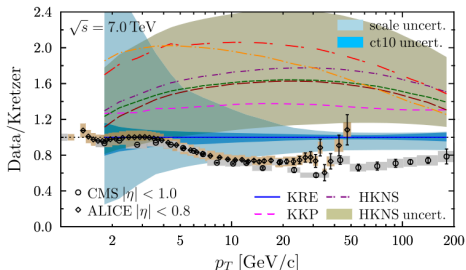
+ some others (including analyses for specific hadrons)

BKK95 [ZPB 65 (1995) 471]	π^\pm, K^\pm	AESS11 [PRD 83 (2011) 034002]	η
BKK96 [PRD 53 (1996) 3553]	K^0	SKMNA13 [PRD 88 (2013) 054019]	π^\pm, K^\pm
DSV97 [PRD 57 (1998) 5811]	Λ^0	LSS15 [PRD 96 (2016) 074026]	SIDIS only
BFGW00 [EPJ C19 (2001) 89]	h^\pm		

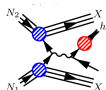
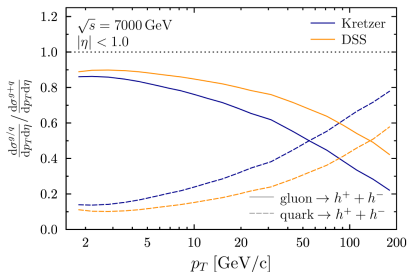
Focus on π and K which constitute the largest fraction in measured yields

Fragmentation functions: why should we bother?

Example 1: Ratio of the inclusive charged-hadron spectra measured by CMS and ALICE



Figures taken from [NPB 883 (2014) 615]



$$E \frac{d^3\sigma}{dp_T^3} = \sum_{a,b,c} f_a \otimes f_b \otimes \hat{\sigma}_{ab}^c \otimes D_c^h$$

Predictions from all available FF sets are not compatible with CMS and ALICE data, not even within scale and PDF/FF uncertainties
 → How well do we know the gluon FF?

Fragmentation functions: why should we bother?

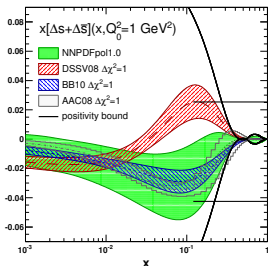
Example 2: The strange polarised parton distribution at $Q^2 = 2.5 \text{ GeV}^2$ ($\Delta s = \Delta \bar{s}$)

NNPDFpol1.0 [NPB 874 (2013) 36]
 $\int_0^1 dx [\Delta s + \Delta \bar{s}] = -0.13 \pm 0.09$

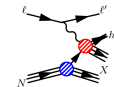
JAM17 [PRL 119 (2017) 132001]
 $\int_0^1 dx [\Delta s + \Delta \bar{s}] = -0.03 \pm 0.10$

First moment constrained by
 $a_3 = \int_0^1 dx [\Delta u^+ - \Delta d^+] = 1.2701 \pm 0.0025$

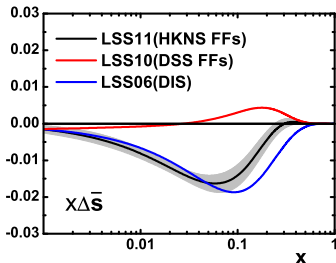
$a_8 = \int_0^1 dx [\Delta u^+ + \Delta d^+ - 2\Delta s^+] = 0.585 \pm 0.176$



directly from SIDIS Kaon data



indirectly from DIS + SU(3)



$$\frac{d\sigma}{dx dy} = \frac{2\pi\alpha_{\text{em}}^2}{Q^2} [(2-y)g_1]$$

$$\frac{d\sigma^h}{dx dy dz} = \frac{2\pi\alpha_{\text{em}}^2}{Q^2} \left[\frac{1+(1-y)^2}{y} 2g_1^h + \frac{2(1-y)}{y} g_L^h \right]$$

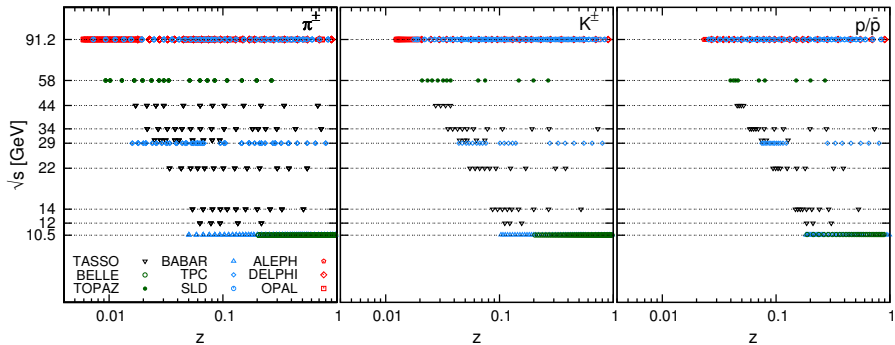
If SIDIS data is used to determine Δs , K^\pm FFs for different sets lead to different results. Such results may differ significantly among them and w.r.t. the results obtained from DIS
 → How well do we know kaon FFs?

Figure taken from [PRD 84 (2011) 014002]

2. The NNFF1.0 analysis

[EPJ C77 (2017) 516]

The dataset



CERN-LEP: ALEPH [ZP C66(1995) 353] DELPHI [EPJ C18(2000) 203] OPAL [ZP C63(1994) 181]

KEK: BELLE ($n_f = 4$) [PRL 111(2013) 062002] TOPAZ [PL B345(1995) 335]

DESY-PETRA: TASSO [PL B94(1980) 444, ZP C17(1983) 5, ZP C42(1989) 189]

SLAC: BABAR ($n_f = 4$) [PR D88(2013) 032011] SLD [PR D58(1999) 052001] TPC [PRL 61(1988) 1263]

$$\frac{d\sigma^h}{dz} = \frac{4\pi\alpha^2(Q^2)}{Q^2} \mathcal{F}_2^h(z, Q^2) \quad h = \pi^+ + \pi^-, K^+ + K^-, p + \bar{p} \quad \text{possibly normalised to } \sigma_{\text{tot}}$$

$$N_{\text{dat}}^{\pi^\pm} = 428$$

$$N_{\text{dat}}^{K^\pm} = 385$$

$$N_{\text{dat}}^{p/\bar{p}} = 360$$

From observables to fragmentation functions

$$\mathcal{F}_2^h = \langle e^2 \rangle \left\{ C_{2,q}^S \otimes D_\Sigma^h + n_f C_{2,g}^S \otimes D_g^h + C_{2,q}^{NS} \otimes D_{NS}^h \right\}$$

$$\langle e^2 \rangle = \frac{1}{n_f} \sum_{q=1}^{n_f} \hat{e}_q^2 \quad D_\Sigma^h = \sum_{q=1}^{n_f} D_{q^+}^h \quad D_{NS}^h = \sum_{q=1}^{n_f} \left(\frac{\hat{e}_q^2}{\langle e^2 \rangle} - 1 \right) D_{q^+}^h \quad D_{q^+}^h = D_q^h + D_{\bar{q}}^h$$

Coefficient functions and splitting functions known up to NNLO

[NPB 751 (2006) 18; NPB 749 (2006) 1; PLB 638 (2006) 61; NPB 845 (2012) 133]

$$\begin{aligned} F_2^{h,n_f=5} &= \frac{1}{5} \left[(2\hat{e}_u^2 + 3\hat{e}_d^2) C_{2,q}^S + 3(\hat{e}_u^2 - \hat{e}_d^2) C_{2,q}^{NS} \right] \otimes (D_{u^+}^h + D_{c^+}^h) \\ &+ \frac{1}{5} \left[(2\hat{e}_u^2 + 3\hat{e}_d^2) C_{2,q}^S - 2(\hat{e}_u^2 - \hat{e}_d^2) C_{2,q}^{NS} \right] \otimes (D_{d^+}^h + D_{s^+}^h + D_{b^+}^h) \\ &+ (2\hat{e}_u^2 + 3\hat{e}_d^2) C_{2,g}^S \otimes D_g^h \end{aligned}$$

No sensitivity to individual quark and antiquark FFs

Limited sensitivity to flavour separation via the variation of \hat{e}_q with Q^2
 $\hat{e}_u^2/\hat{e}_d^2(Q^2 = 10 \text{ GeV}) \sim 4 \Rightarrow D_{u^+}^h, D_{d^+}^h + D_{s^+}^h$; $\hat{e}_u^2/\hat{e}_d^2(Q^2 = M_Z) \sim 0.8 \Rightarrow D_\Sigma^h$
 Flavor separation between uds and c, b quarks achieved thanks to tagged data

Direct sensitivity to D_g^h only beyond LO, as $C_{2,g}^S$ is $\mathcal{O}(\alpha_s^2)$, and tenous
 Indirect sensitivity to D_g^h via scale violations in the time-like DGLAP evolution

The NNPDF methodology: parametrisation

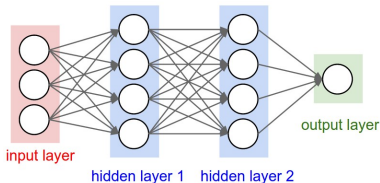
- ① Neural network (NN), *i.e.* a generator of random functions in the space of FFs

$$zD_i^h(z, Q_0^2) = \mathcal{F}_i^h(z, \{\mathbf{c}\}) \quad \mathcal{F}_i^h(z, \{\mathbf{c}\}) \text{ is a feed-forward neural network}$$

in terms of a huge set of parameters ($\mathcal{O}(200)$ per PDF set)

$$\{\mathbf{c}\} = \{\omega_{ij}^{(L-1), D_i^h}, \theta_i^{(L), D_i^h}\}$$

- ② What a feed-forward NN exactly is?



$$\xi_i^{(l)} = g \left(\sum_j^{n_l-1} \omega_{ij}^{(l-1)} \xi_j^{(l-1)} - \theta_i^{(l)} \right)$$

$$g(y) = \frac{1}{1 + e^{-y}}$$

- ▶ made of neurons grouped into layers (define the architecture)
- ▶ each neuron receives input from neurons in the preceding layer (feed-forward NN)
- ▶ activation $\xi_i^{(l)}$ determined by a set of parameters (**weights** and **thresholds**)
- ▶ activation determined according to a **non-linear function** (except the last layer)

⇒ **potentially non-smooth**

⇒ **bias due to the parametrisation reduced as much as possible**

The NNPDF methodology: uncertainty representation

- 1 Generate (*art*) replicas of (*exp*) data according to the distribution

$$\mathcal{O}_i^{(art)(k)} = \mathcal{O}_i^{(exp)} + r_i^{(k)} \sigma_{\mathcal{O}_i}, \quad i = 1, \dots, N_{\text{dat}}, \quad k = 1, \dots, N_{\text{rep}}$$

where $r_i^{(k)}$ are (Gaussianly distributed) random numbers for each k -th replica ($r_i^{(k)}$ can be generated with any distribution, not necessarily Gaussian)

- 2 Validate the Monte Carlo sample size against experimental data
- 3 Perform a fit for each replica $k = 1, \dots, N_{\text{rep}}$
- 4 Compact computation of observables and their uncertainties (PDF replicas are equally probable members of a statistical ensemble)

$$\langle \mathcal{O}[D(x, Q^2)] \rangle = \frac{1}{N_{\text{rep}}} \sum_{k=1}^{N_{\text{rep}}} \mathcal{O}[D^{(k)}(x, Q^2)]$$

$$\sigma_{\mathcal{O}}[D(x, Q^2)] = \left[\frac{1}{N_{\text{rep}} - 1} \sum_{k=1}^{N_{\text{rep}}} \left(\mathcal{O}[D^{(k)}(x, Q^2)] - \langle \mathcal{O}[D(x, Q^2)] \rangle \right)^2 \right]^{1/2}$$

⇒ **no need to rely on linear approximation**

⇒ **computational expensive: need to perform N_{rep} fits instead of one**

Fit settings

Physical parameters: consistent with the NNPDF3.1 PDF set [EPJ C77 (2017) 663]

$$\alpha_s(M_Z) = 0.118, \alpha(M_Z) = 1/127, m_c = 1.51 \text{ GeV}, m_b = 4.92 \text{ GeV}$$

Solution of DGLAP equations: numerical solution in z -space as implemented in APFEL
extensive benchmark performed up to NNLO [JHEP 1503 (2015) 046]

Parametrisation: each FF is parametrised with a feed-forward neural network (2-5-3-1)

$$D_i^h(Q_0, z) = \text{NN}(x) - \text{NN}(1), \quad Q_0 = 5 \text{ GeV}$$

$$h = \pi^+ + \pi^-, h = K^+ + K^-, h = p + \bar{p} \quad i = u^+, d^+ + s^+, c^+, b^+, g$$

$$\text{we assume charge conjugation, from which } D_{q^+}^{\pi^+} = D_{q^+}^{\pi^-}$$

initial scale above m_b , but below the lowest c.m. energy of the data, avoid threshold crossing

Heavy flavours: heavy-quark FFs are parametrised independently at the initial scale Q_0

Hadron mass corrections: included exactly à la Albino-Kniehl-Kramer [NPB 803 (2008) 42]

Kinematic cuts: $z \rightarrow 0$: contributions $\propto \ln z$; $z \rightarrow 1$: contributions $\propto \ln(1 - z)$

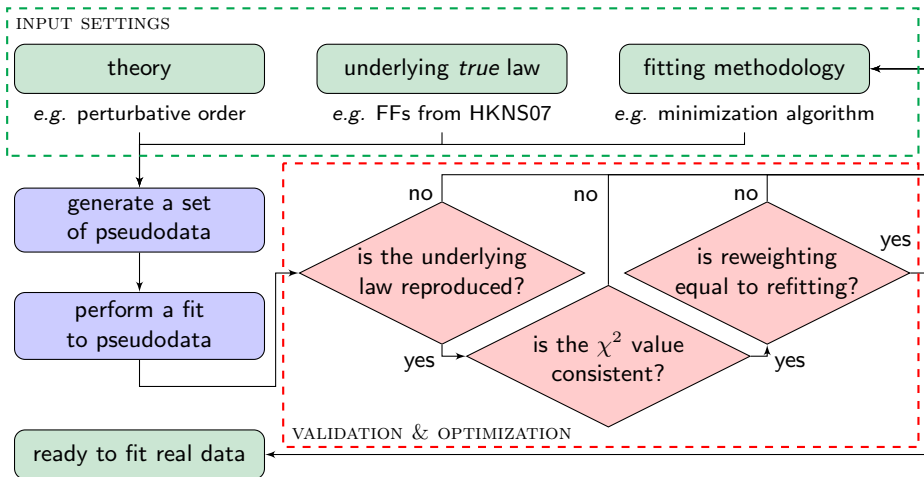
$$z_{\min} = 0.075, z_{\min} = 0.02 (\sqrt{s} = M_Z); z_{\max} = 0.90$$

Momentum sum rule: check a posteriori that

$$\sum_{h=\pi^\pm, K^\pm, p/\bar{p}} \int_{z_{\min}}^1 dz z D_i^h(z, Q) < N \quad N \begin{cases} = 1 & \text{for } i = g \\ = 2 & \text{for } i = u^+, c^+, b^+ \\ = 4 & \text{for } i = d^+ + s^+ \end{cases}$$

Methodology validation: closure tests [JHEP 1504 (2015) 040]

Validation and optimization of the fitting strategy with known underlying physical law



Full control of procedural uncertainties

Closure tests: levels

- ① Level 0: generate pseudodata D_i^0 with zero uncertainty (but $(\text{cov})_{ij}$ in the χ^2 is the data covariance matrix)
→ fit quality can be arbitrarily good, if the fitting methodology is efficient: $\chi^2/N_{\text{dat}} \sim 0$
→ validate fitting methodology (parametrisation, minimisation)
→ interpolation and extrapolation uncertainty

- ② Level 1: generate pseudodata D_i^1 with stochastic fluctuations (no replicas)

$$D_i^1 = (1 + r_i^{\text{nor}} \sigma_i^{\text{nor}}) \left(D_i^0 + \sum_p^{N_{\text{sys}}} r_{i,p}^{\text{sys}} \sigma_{i,p}^{\text{sys}} + r_i^{\text{stat}} \sigma_i^{\text{stat}} \right)$$

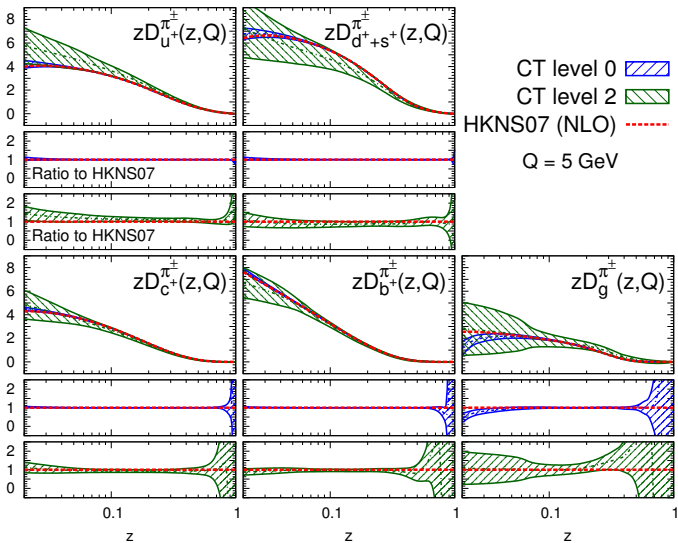
- experimental uncertainties are not propagated into FFs: $\chi^2/N_{\text{dat}} \sim 1$
→ functional uncertainty (a large number of functional forms with equally good χ^2)

- ③ Level 2: generate N_{rep} Monte Carlo pseudodata replicas $D_i^{2,k}$ on top of Level 1

$$D_i^{2,k} = (1 + r_i^{\text{nor},k} \sigma_i^{\text{nor}}) \left(D_i^1 + \sum_p^{N_{\text{sys}}} r_{i,p}^{\text{sys},k} \sigma_{i,p}^{\text{sys}} + r_i^{\text{stat},k} \sigma_i^{\text{stat}} \right)$$

- propagate the fluctuations due to experimental uncertainties into FFs: $\chi^2/N_{\text{dat}} \sim 1$
→ input FFs lie within the one-sigma band of the fitted FFs with a probability of $\sim 68\%$
→ data uncertainty

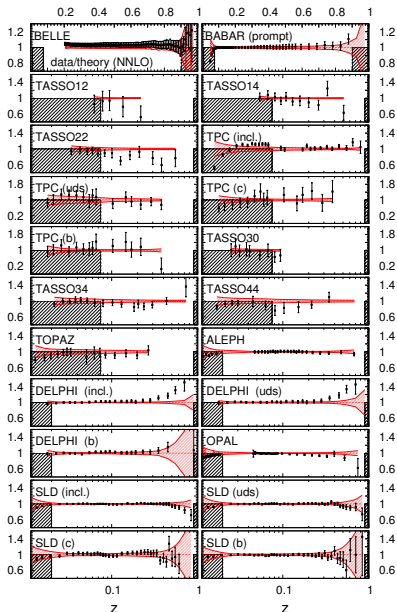
Closure testing NNFF1.0



$$\chi^2/N_{\text{dat}} = 0.0001 \text{ (L0)}$$

$$\chi^2/N_{\text{dat}} = 1.0262 \text{ (L1)}$$

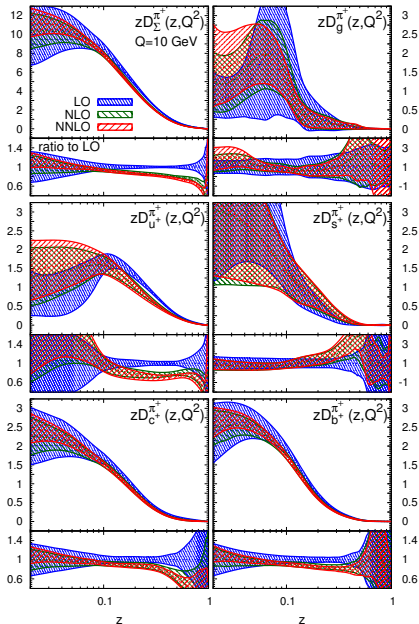
Fit quality: π^+



Exp.	NNLO theory		remarks
	N_{dat}	χ^2/N_{dat}	
BELLE	70	0.09	lack of correlations
BABAR	40	0.78	✓
TASSO12	4	0.87	small sample
TASSO14	9	1.70	} data fluctuations
TASSO22	8	1.91	
TPC	13	0.85	
TPC-UDS	6	0.49	✓
TPC-C	6	0.52	✓
TPC-B	6	1.43	✓
TASSO34	9	1.00	✓
TASSO44	6	2.34	data fluctuations
TOPAZ	5	0.80	✓
ALEPH	23	0.78	✓
DELPHI	21	1.86	tension with OPAL
DELPHI-UDS	21	1.54	tension with OPAL
DELPHI-B	21	0.95	✓
OPAL	24	1.84	tension with DELPHI
SLD	34	0.83	✓
SLD-UDS	34	0.52	✓
SLD-C	34	1.06	✓
SLD-B	34	0.36	✓
TOTAL	428	0.87	✓

Overall good description of the dataset
 Signs of tension OPAL vs DELPHI (inclusive)
 Anomalously small χ^2/N_{dat} for BELLE

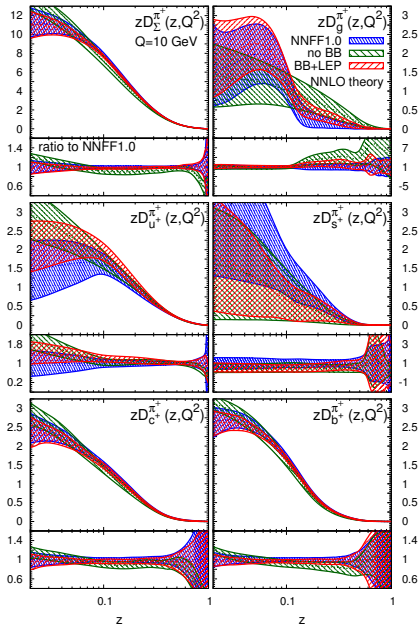
Dependence upon perturbative order: π^+



Exp.	N_{dat}	LO χ^2/N_{dat}	NLO χ^2/N_{dat}	NNLO χ^2/N_{dat}
BELLE	70	0.60	0.11	0.09
BABAR	40	1.91	1.77	0.78
TASSO12	4	0.70	0.85	0.87
TASSO14	9	1.55	1.67	1.70
TASSO22	8	1.64	1.91	1.91
TPC	13	0.46	0.65	0.85
TPC-UDS	6	0.78	0.55	0.49
TPC-C	6	0.55	0.53	0.52
TPC-B	6	1.44	1.43	1.43
TASSO34	9	1.16	0.98	1.00
TASSO44	6	2.01	2.24	2.34
TOPAZ	5	1.04	0.82	0.80
ALEPH	23	1.68	0.90	0.78
DELPHI	21	1.44	1.79	1.86
DELPHI-UDS	21	1.30	1.48	1.54
DELPHI-B	21	1.21	0.99	0.95
OPAL	24	2.29	1.88	1.84
SLD	34	2.33	1.14	0.83
SLD-UDS	34	0.95	0.65	0.52
SLD-C	34	3.33	1.33	1.06
SLD-B	34	0.45	0.38	0.36
TOTAL	428	1.44	1.02	0.87

Excellent perturbative convergence
 FFs almost stable from NLO to NNLO
 LO FF uncertainties larger than HO

Dependence upon the dataset: π^+

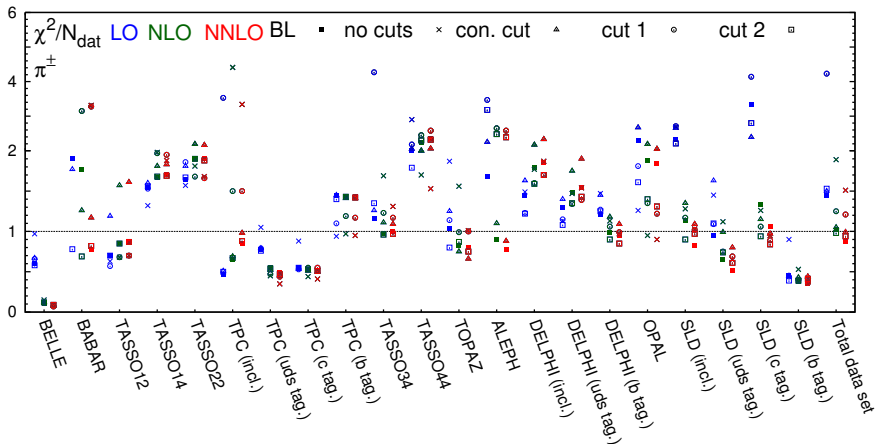


NNLO theory Exp.	N_{dat}	χ^2/N_{dat}	no BB χ^2/N_{dat}	BB+LEP χ^2/N_{dat}
BELLE	70	0.09	[4.92]	0.09
BABAR	40	0.78	[144]	0.88
TASSO12	4	0.87	0.52	[0.87]
TASSO14	9	1.70	1.38	[1.71]
TASSO22	8	1.91	1.29	[2.15]
TPC	13	0.85	2.12	[2.15]
TPC-UDS	6	0.49	0.54	[0.77]
TPC-C	6	0.52	0.74	[0.58]
TPC-B	6	1.43	1.60	[1.48]
TASSO34	9	1.00	1.17	[1.38]
TASSO44	6	2.34	2.52	[1.97]
TOPAZ	5	0.80	0.92	[1.72]
ALEPH	23	0.78	0.57	0.74
DELPHI	21	1.86	1.97	1.82
DELPHI-UDS	21	1.54	1.56	1.42
DELPHI-B	21	0.95	1.01	0.95
OPAL	24	1.84	1.75	1.92
SLD	34	0.83	0.87	0.95
SLD-UDS	34	0.52	0.53	0.63
SLD-C	34	1.06	0.69	0.96
SLD-B	34	0.36	0.49	0.37
TOTAL		0.87	1.06	0.82

no BB: larger uncertainties; different gluon shape and different light flavour separation
 BB+LEP: comparable uncertainties; slightly different size of gluon and light flavoured quarks

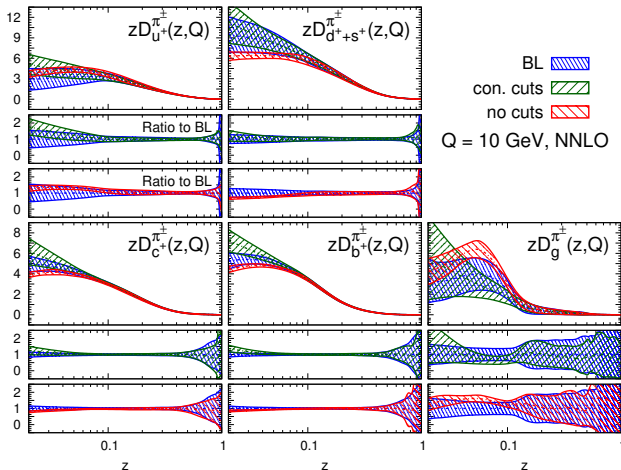
Dependence upon kinematic cuts: π^+

BL		no cuts		con. cut		cut1		cut2	
$z_{\min}^{(m_Z)}$	z_{\min}	$z_{\min}^{(m_Z)}$	z_{\min}	$z_{\min}^{(m_Z)}$	z_{\min}	$z_{\min}^{(m_Z)}$	z_{\min}	$z_{\min}^{(m_Z)}$	z_{\min}
0.02	0.075	0.00	0.00	0.05	0.10	0.01	0.05	0.01	0.075



Dependence upon kinematic cuts: π^+

BL		no cuts		con. cut		cut1		cut2	
$z_{\min}^{(m_Z)}$	z_{\min}	$z_{\min}^{(m_Z)}$	z_{\min}	$z_{\min}^{(m_Z)}$	z_{\min}	$z_{\min}^{(m_Z)}$	z_{\min}	$z_{\min}^{(m_Z)}$	z_{\min}
0.02	0.075	0.00	0.00	0.05	0.10	0.01	0.05	0.01	0.075

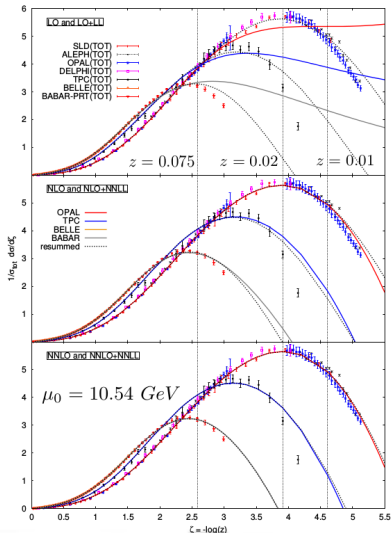


Small- z resummed Fragmentation Functions [PRD 95 (2017) 054003]

436 Total data Points:

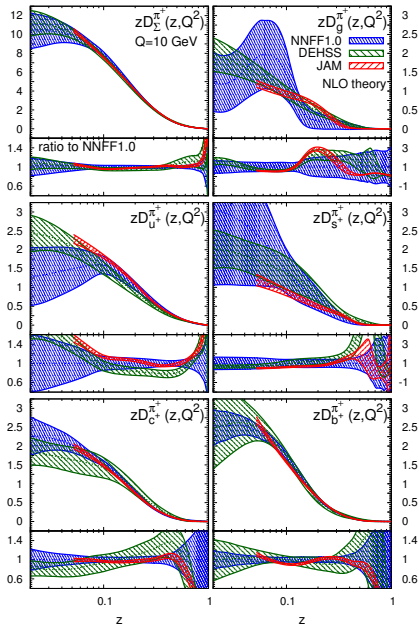
- LEP cut ($z = 0.01$) due to inconsistency between OPAL and ALEPH
- TPC lower cut ($z = 0.02$) based on difference of energy fraction $z = 2 E_h/Q$ and three momentum fraction $x_p = z - 2m_h^2/(zQ^2) + \mathcal{O}(1/Q^4)$ in c.m.s being less than at least 15%

accuracy	χ^2	χ^2/dof
LO	1260.78	2.89
NLO	354.10	0.81
NNLO	330.08	0.76
LO+LL	405.54	0.93
NLO+NNLL	352.28	0.81
NNLO+NNLL	329.96	0.76



Slide: courtesy of D. P. Anderle

Comparison with other FF determinations: π^+



DEHSS [PRD 91 (2015) 014035]
 (+SIDIS + PP)

JAM [PRD 94 (2016) 114004]
 (almost same dataset as NNFF1.0)

different cuts at small z

$D_{\Sigma}^{\pi^+}$: excellent mutual agreement
 both c.v. and unc. (bulk of the dataset)

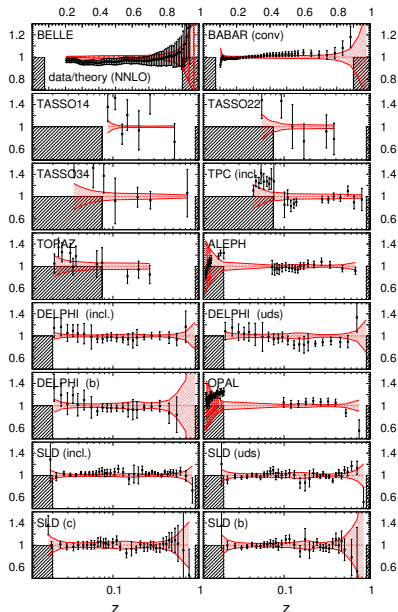
$D_g^{\pi^+}$: slight disagreement
 different shapes, larger uncertainties
 DEHSS: data; JAM: parametrisation

$D_{u^+}^{\pi^+}, D_{s^+}^{\pi^+}$: good overall agreement
 excellent with JAM, though larger uncertainties
 slightly different shape w.r.t. DEHSS (dataset)

$D_{c^+}^{\pi^+}, D_{b^+}^{\pi^+}$: good overall agreement
 excellent with JAM, same uncertainties
 slightly different shape w.r.t. DEHSS (dataset)

Fit quality: K^+

Exp.	N_{dat}	NNLO theory	
		χ^2/N_{dat}	remarks
BELLE	70	0.32	lack of correlations
BABAR	43	0.95	✓
TASSO12	3	1.02	} small sample
TASSO14	9	2.07	
TASSO22	6	2.62	
TPC	13	1.01	
TASSO34	5	0.36	} small sample
TOPAZ	3	0.99	
ALEPH	18	0.56	✓
DELPHI	22	0.34	✓
DELPHI-UDS	22	1.32	✓
DELPHI-B	22	0.52	✓
OPAL	10	1.66	tension with other M_Z data
SLD	35	0.57	✓
SLD-UDS	35	0.93	✓
SLD-C	34	0.38	✓
SLD-B	35	0.62	✓
TOTAL	385	0.73	✓



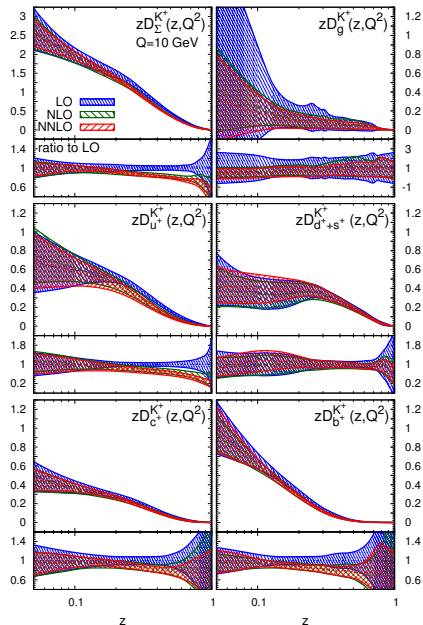
- Overall good description of the dataset
- Excellent BELLE/BABAR consistency
- Signs of tension OPAL vs DELPHI (inclusive)
- Anomalously small χ^2/N_{dat} for BELLE
- Dependence upon the data set and kin cuts similar to pions

Dependence upon perturbative order: K^+

Exp.	N_{dat}	LO χ^2/N_{dat}	NLO χ^2/N_{dat}	NNLO χ^2/N_{dat}
BELLE	70	0.21	0.32	0.32
BABAR	43	2.86	1.11	0.95
TASSO12	3	1.10	1.03	1.02
TASSO14	9	2.17	2.13	2.07
TASSO22	6	2.14	2.77	2.62
TPC	13	0.94	1.09	1.01
TASSO34	5	0.27	0.44	0.36
TOPAZ	3	0.61	1.19	0.99
ALEPH	18	0.47	0.55	0.56
DELPHI	22	0.28	0.33	0.34
DELPHI-UDS	22	1.38	1.49	1.32
DELPHI-B	22	0.58	0.49	0.52
OPAL	10	1.67	1.57	1.66
SLD	35	0.86	0.62	0.57
SLD-UDS	35	1.31	1.02	0.93
SLD-C	34	0.92	0.47	0.38
SLD-B	35	0.59	0.67	0.62
TOTAL	385	1.02	0.78	0.73

Excellent perturbative convergence
FFs almost stable from NLO to NNLO
LO FF uncertainties larger than HO

i	N^{i+1}/N^i	D_g	D_Σ	D_{c+}	D_{b+}
0	NLO/LO [%]	95-300	70-80	65-80	70-85
1	NNLO/NLO [%]	70-130	90-100	90-110	95-115



Comparison with other FF determinations: K^+

DEHSS [PRD 95 (2017) 094019]
(+SIDIS +PP)

JAM [PRD 94 (2016) 114004]
(almost same dataset as NNFF1.0)

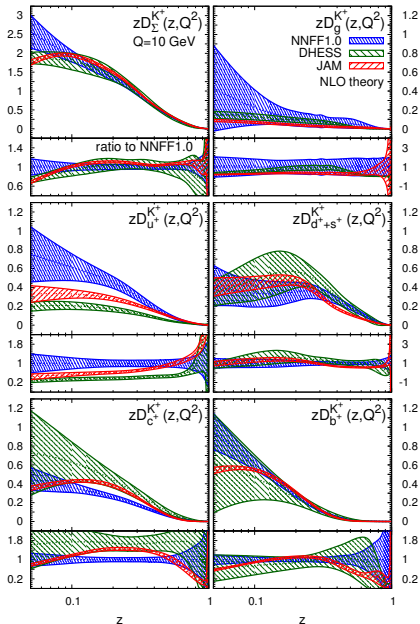
$D_{\Sigma}^{\pi^+}$: excellent agreement (both c.v. and unc.)
bulk of the dataset

$D_g^{\pi^+}$: good mutual agreement
similar shapes, larger uncertainties
DEHSS: data; JAM: parametrisation

$D_{u^+}^{\pi^+}$: mutual sizable disagreement
differences in dataset and parametrisation
comparable uncertainties in the data region

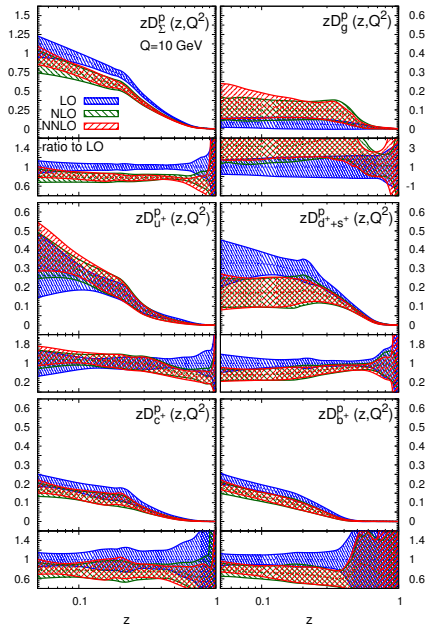
$D_{d^+}^{\pi^+} + D_{s^+}^{\pi^+}$: fair mutual agreement
differences in dataset and parametrisation
comparable uncertainties in the data region

$D_{c^+}^{\pi^+}, D_{b^+}^{\pi^+}$: excellent mutual agreement
uncertainties similar to JAM
DHESS shows inflated uncertainties



Dependence upon perturbative order: p/\bar{p}

Exp.	N_{dat}	LO χ^2/N_{dat}	NLO χ^2/N_{dat}	NNLO χ^2/N_{dat}
BABAR	43	0.10	0.31	0.50
BELLE	29	4.74	2.75	1.25
TASSO12	3	0.69	0.70	0.72
TASSO14	9	1.32	1.25	1.22
TASSO22	9	0.98	0.92	0.93
TPC	20	1.04	1.10	1.08
TASSO30	2	0.25	0.19	0.18
TASSO34	6	0.82	0.81	0.78
TOPAZ	4	0.79	1.21	0.19
ALEPH	26	1.36	1.43	1.28
DELPHI	22	0.48	0.49	0.49
DELPHI-UDS	22	0.47	0.46	0.45
DELPHI-B	22	0.89	0.89	0.91
SLD	36	0.66	0.65	0.64
SLD-UDS	36	0.77	0.76	0.78
SLD-C	36	1.22	1.22	1.21
SLD-B	35	1.12	1.29	1.33
TOTAL	360	1.31	1.13	0.98



Excellent perturbative convergence
 FFs almost stable from NLO to NNLO
 LO FF uncertainties larger than HO
 Dependence upon data set and kin cuts
 similar to pions and kaons

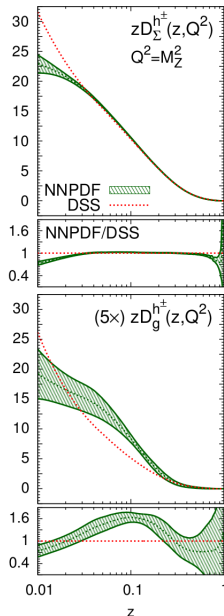
Fragmentation functions of unidentified charged hadrons

Combine the information from identified π^\pm , K^\pm and p/\bar{p} FFs with that from residual light charged hadrons [arXiv:1709.03400]

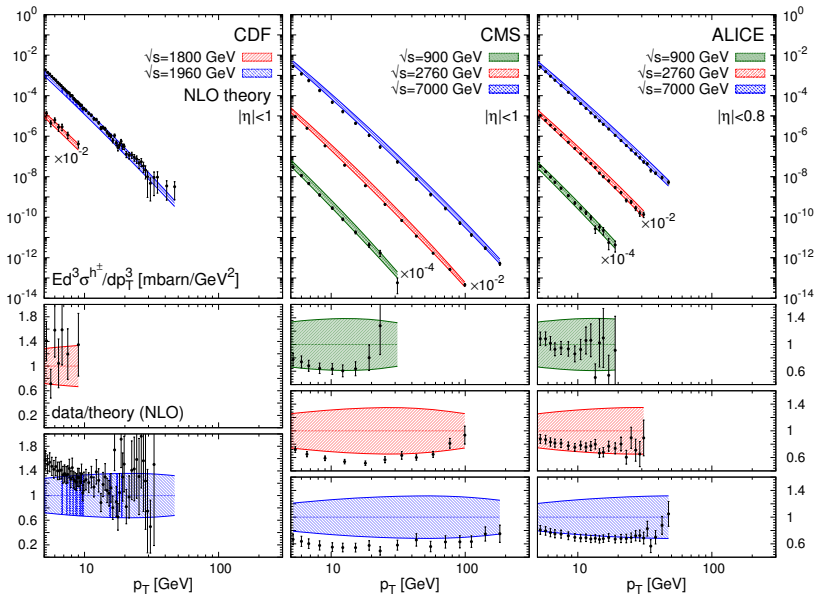
Preliminary analysis done consistently with NNFF1.0 (NLO)

Additional F_L data (non-vanishing $\mathcal{O}(\alpha_s)$ contribution at LO)

Experiment	Observable	\sqrt{s} [GeV]	N_{dat}	χ^2/N_{dat}
TASSO14	F_2 (incl.)	14.00	15 (20)	1.23
TASSO22	F_2 (incl.)	22.00	15 (20)	0.51
TPC	F_2 (incl.)	29.00	21 (34)	1.65
TASSO35	F_2 (incl.)	35.00	15 (20)	1.14
TASSO44	F_2 (incl.)	44.00	15 (20)	0.68
ALEPH	F_2 (incl.)	91.20	32 (35)	1.04
	F_L (incl.)	91.20	19 (21)	0.36
DELPHI	F_2	91.20	21 (27)	0.65
	F_2 (uds tagged)	91.20	21 (27)	0.17
	F_2 (b tagged)	91.20	21 (27)	0.82
	F_L (incl.)	91.20	20 (22)	0.72
	F_L (b tagged)	91.20	20 (22)	0.44
OPAL	F_2 (incl.)	91.20	20 (22)	2.41
	F_2 (uds tagged)	91.20	20 (22)	0.90
	F_2 (c tagged)	91.20	20 (22)	0.61
	F_2 (b tagged)	91.20	20 (22)	0.21
	F_L (incl.)	91.20	20 (22)	0.31
SLD	F_2	91.28	34 (40)	0.75
	F_2 (uds tagged)	91.28	34 (40)	1.03
	F_2 (c tagged)	91.28	34 (40)	0.62
	F_2 (b tagged)	91.28	34 (40)	0.97
Total dataset			471 (527)	0.83



Fragmentation functions of unidentified charged hadrons



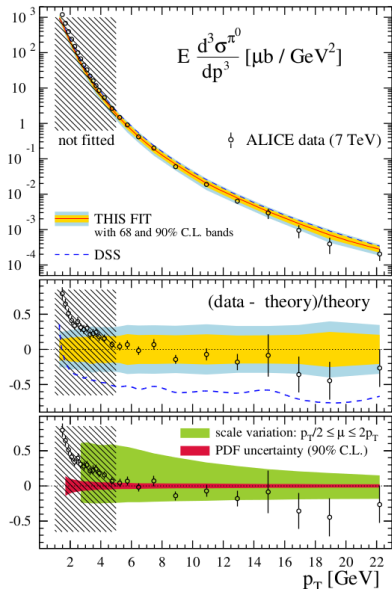
3. Summary and outlook

More global fits

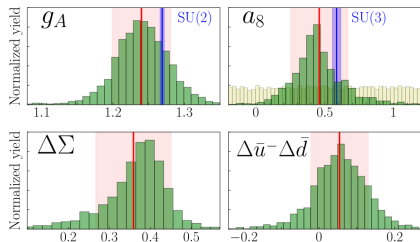
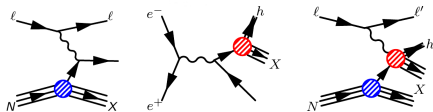
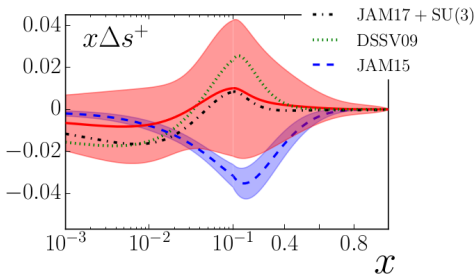
pions: $\chi^2_{\text{tot}}/N_{\text{dat}} = 1.19$

experiment	data type	norm. N_i	# data in fit	χ^2	
TPC [48]	incl.	1.043	17	17.3	
	uds tag	1.043	9	2.1	
	c tag	1.043	9	5.9	
	b tag	1.043	9	9.2	
TASSO [49]	34 GeV	incl.	1.043	11	30.2
	44 GeV	incl.	1.043	7	22.2
SLD [19]	incl.	0.986	28	15.3	
	uds tag	0.986	17	18.5	
	c tag	0.986	17	16.1	
	b tag	0.986	17	5.8	
ALEPH [16]	incl.	1.020	22	22.9	
DELPHI [17]	incl.	1.000	17	28.3	
OPAL [18, 20]	uds tag	1.000	17	33.3	
	b tag	1.000	17	10.6	
	incl.	1.000	21	14.0	
	u tag	0.786	5	31.6	
	d tag	0.786	5	33.0	
	s tag	0.786	5	51.3	
	c tag	0.786	5	30.4	
	b tag	0.786	5	14.6	
BABAR [28]	incl.	1.031	45	46.4	
BELLE [29]	incl.	1.044	78	44.0	
HERMES [30]	π^+ (p)	0.980	32	27.8	
	π^- (p)	0.980	32	47.8	
	π^+ (d)	0.981	32	40.3	
	π^- (d)	0.981	32	59.1	
COMPASS [31] prel.	π^+ (d)	0.946	199	174.2	
	π^- (d)	0.946	199	229.0	
PHENIX [21]	π^0	1.112	15	15.8	
STAR [33-36]	$0 \leq \eta \leq 1$	π^0	1.161	7	5.7
	$0.8 \leq \eta \leq 2.0$	π^0	0.954	7	2.7
	$ \eta < 0.5$	π^\pm	1.071	8	4.3
	$ \eta < 0.5$	$\pi^+, \pi^-/\pi^+$	1.006	16	17.2
	ALICE [32]	7 TeV	π^0	0.766	11
TOTAL:			973	1154.6	

[PRD 91 (2015) 014035; PRD 95 (2017) 094019]



Simultaneous fits [PRL 119 (2017) 132001]



$g_A = 1.24 \pm 0.04$ $a_8 = 0.46 \pm 0.21$
 confirmation of SU(2) symmetry to $\sim 2\%$
 $\sim 20\%$ SU(3) breaking $\pm 20\%$

$$\Delta s^+ = -0.03 \pm 0.09$$

$$\Delta\Sigma = 0.36 \pm 0.09 \quad \Delta u - \Delta d = 0.05 \pm 0.08$$

process	target	N_{dat}	χ^2
DIS	$p, d, {}^3\text{He}$	854	854.8
SIA (π^\pm, K^\pm)		850	997.1
SIDIS (π^\pm)			
HERMES	d	18	28.1
HERMES	p	18	14.2
COMPASS	d	20	8.0
COMPASS	p	24	18.2
SIDIS (K^\pm)			
HERMES	d	27	18.3
COMPASS	d	20	18.7
COMPASS	p	24	12.3
Total:		1855	1969.7

Conclusions

- 1 A number of hard-scattering processes require an appropriate knowledge of FFs
 - ▶ probing nucleon momentum, spin and flavour
 - ▶ underlying spatial distributions and the dynamics of nuclear matter
- 2 FFs are poorly known in comparison to PDFs
 - ▶ limited set of available data, observables often require PDFs and FFs simultaneously
 - ▶ troubles in describing some observables in pp and SIDIS from current FF sets
- 3 New analysis based on the NNPDF methodology, NNFF1.0
 - ▶ at LO, NLO and NNLO, based on SIA data for π^\pm , K^\pm and p/\bar{p}
 - ▶ completely closure-tested, addresses methodological issues in previous analyses
 - ▶ detailed study of the stability of the results upon variations of the data set/kin cuts
 - ▶ FF uncertainties (gluon) seem to be underestimated in previous determinations
 - ▶ differences in shapes, to be further investigated
 - ▶ good description of the hadron spectra at the LHC within uncertainties
 - ▶ applicability limited by insensitivity to favoured/unfavoured FFs
- 4 Future improvements
 - ▶ More global fits
 - ▶ Simultaneous fits of FFs and PDFs

Dependence on α_s

