Particle Physics



Part II, Lent Term 2004 HANDOUT VII

1

ELECTROWEAK UNIFICATION



Electroweak Unification

Glashow (1961), Weinberg (1967) and Salam (1968) model treats EM and WEAK interactions as different manifestations of a UNIFIED force.

★ It is somewhat ad hoc

★ But gives concrete predictions - i.e. a testable theory

★ provides perfect description of precise data

"Basic idea" - start with 4 massless bosons, $\{W^+, W^0, W^-\}$ and B^0 . The neutral bosons mix to give physical BOSONs, (the particles we see), *i.e.* the W^{\pm} , Z^0 and γ .

$$egin{pmatrix} W^+ \ W^0 \ W^- \end{pmatrix}, B o egin{pmatrix} W^+ \ Z^0 \ W^- \end{pmatrix}, \gamma$$

Physical Fields : W^+ , W^+ $\mathbf{Z^0}$, A (photon)

$$\mathbf{Z}^0 = \mathbf{W}^0 \cos \theta_W - \mathbf{B} \sin \theta_W$$

$$\mathbf{A} = \mathbf{W}^{\mathbf{0}} \sin \theta_{\mathbf{W}} + \mathbf{B} \cos \theta_{\mathbf{W}}$$

 $heta_W$: weak mixing angle

 \mathbf{W}^{\pm} and $\mathbf{Z}^{\mathbf{0}}$ 'acquire' mass via the HIGGS MECHANISM

The beauty of the model is that it makes exact predictions:

★ Weak coupling constant: $e = g \sin \theta_w$

 \star The mass of the ${
m Z}^{0}$ boson

$$M_{\mathbf{Z}^0} = rac{M_{\mathbf{W}}}{\cos heta_W}$$

 $igstar{\mathbf{\star}}$ The couplings of the $\mathbf{Z}^{m{v}}$ boson

★ ONLY 3 free parameters !

IF we know $\{\alpha_{em}, G_{\rm F}, \sin \theta_W\}$ everything else is FIXED, i.e. predict $M_{\rm W}, M_{\rm Z^0}$, couplings, etc.



WEAK Neutral Current (NC) interactions are mediated by the \mathbb{Z}^0 boson.



- **WEAK NC NEVER changes flavour**
- ★ Z⁰ couplings are a "MIXTURE" of weak and electro-magnetic couplings
- \star WEAK NC couplings therefore depend on $\sin^2 heta_W$

 Z^0 couplings are a mixture of EM (VECTOR) and WEAK (VECTOR-AXIAL-VECTOR) couplings

$$rac{g}{\cos heta_W}rac{1}{2}\gamma^\mu (C_V-C_A\gamma^5)$$

Form of neutral current couplings are determined by the WEAK MIXING ANGLE θ_W

ELECTROWEAK CHARGES : NON-EXAMINABLE

EM γ : Charge $Qe = Qg\sin\theta_W$

Fermion	\boldsymbol{Q}	$2C_V$	$2C_A$
$ u_e, \mu_ u, \mu_ au$	0	0	0
e^- , μ^- , $ au^-$	-1	-1	0
u , c , t	$+\frac{2}{3}$	$+\frac{2}{3}$	0
$oldsymbol{d}, oldsymbol{s}, oldsymbol{b}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0

<u>WEAK CC W[±]:</u> Charge : $g/\sqrt{2}$

Fermion	I_3	$2C_V$	$2C_A$
$ u_e, \mu_ u, \mu_ au$	$+\frac{1}{2}$	1	1
e^-,μ^-, au^-	$=\frac{1}{2}$	1	1
u , c , t	$+\frac{1}{2}$	1	1
d , s, b	$-\frac{1}{2}$	1	1

<u>WEAK NC Z⁰</u>: Charge $g/\cos\theta_W$

$$egin{array}{rcl} C_V &=& (I_3-2{
m sin}^2 heta_WQ) \ C_A &=& I_3 \end{array}$$

Fermion	\boldsymbol{Q}	I_3	$2C_V$	$2C_A$
$ u_e,\mu_ u,\mu_ au$	0	$+\frac{1}{2}$	+1	+1
e^- , μ^- , $ au^-$	-1	$-\frac{1}{2}$	-1+ $4 \sin^2 \theta_W$	-1
<i>u</i> , <i>c</i> , <i>t</i>	$+\frac{2}{3}$	$+\frac{2}{3}$	+1- $\frac{8}{3}$ sin ² θ_W	+1
d , s, b	$-\frac{1}{3}$	$-\frac{2}{3}$	$-1+\frac{4}{3}\sin^2\theta_W$	-1

Summary of Standard Model Vertices

★ At this point have discussed all fundamental fermions and their interactions with the force carrying bosons.

q

q

d'

★ Interactions characterized by SM vertices

ELECTROMAGNETIC (QED)



Couples to CHARGE

Does NOT change FLAVOUR

 $\alpha_{\rm s} = \frac{{\bf g_s}^2}{4\pi}$

STRONG (QCD)

WEAK Charged Current



Does NOT change

FLAVOUR

Couples to COLOUR

Changes FLAVOUR

For QUARKS: coupling BETWEEN generations



Does NOT change FLAVOUR

Drawing Feynman Diagrams

If all are particles (or all anti-particles) e.g.





In all cases only Standard Model vertices allowed.
 Try to keep things as simple as possible.



or "How to Determine if a process is allowed"

Draw SIMPLEST Feynman diagram using Standard Model vertices. Bearing in mind:

- **★** Similar diagrams for particles/anti-particles
- NEVER have a vertex connecting a LEPTON to a QUARK

conservation of lepton number conservation of baryon number

- ★ Only the WEAK CC vertex changes FLAVOUR within generations for leptons within/between generations for quarks
- Onservation of
- ★ Energy is it kinematically allowed
- ★ Charge
- ★ Angular Momentum
- **B** Parity
- **★** Conserved in EM/STRONG interactions
- CAN be violated in CC and NC WEAK interactions
- **O Check SYMMETRY for IDENTICAL particles in**
- the final state
- **★** BOSONS : $\psi(1,2) = +\psi(2,1)$ **★** FERMIONS : $\psi(1,2) = -\psi(2,1)$

(see Questions 14 and 15 on the problem sheet)

Experimental Tests of the Standard Model

★ The idea of electroweak unification under-pins the modern view of particle physics

★ From 1989-2000 experimental measurements at CERN provided precise tests of the Standard Model



- ★ Highest energy e^+e^- collider ever built $\sqrt{s} = 90 - 200 \text{ GeV}$
- ★ Large = 26 km circumference
- \star Designed as a ${
 m Z}^{0}$ and ${
 m W}^{\pm}$ Boson Factory



- **★** Four experiments combined: 16,000,000 Z^0 and 30,000 W^+W^- events
- ★ Precise measurements of the properties of Z^0 and W bosons provide the most stringent test of our current understanding of particle physics





TRACKING



- 0.437 T Axial Magnetic Field
- Track curvature $\propto 1/p_{\perp}$
- $(\sigma_{p_{\perp}}/p_{\perp})^2 = 0.02^2 + 0.0015^2 . (p_{\perp}/GeV)^2$

ELECTRO-MAGNETIC CALORIMETRY



- ECAL = 11705 Lead-Glass blocks
- ECAL coverage $\sim 98~\%~4\pi$
- ECAL Energy Resolution ~ 3 % at 45 GeV

Particle Identification



Different particles leave different signals in the various detector components allowing almost unambiguous identification.









Quarks, which appear as jets of hadrons, look very different to leptons which (usually) appear as a single track



In $e^+e^- \rightarrow Z^0 \rightarrow \tau^+\tau^-$ event, the tau leptons decay within the detector (lifetime $\sim 10^{-13} s$), here $\tau^- \rightarrow e^-\overline{\nu}_e \nu_{\tau}$ and $\tau^+ \rightarrow \mu^+ \nu_{\mu} \overline{\nu}_{\tau}$.

(see Question 16 on the problem sheet)



Consider the process of $\mathrm{e^+e^-}
ightarrow \mathrm{q}\overline{\mathrm{q}}$

- **★** Previously, $\sqrt{s} < 50~{
 m GeV}$ only considered an intermediate photon.
- **★** At higher energies also have the Z^0 exchange diagram (plus $Z^0 \gamma$ interference).



BREIT-WIGNER resonance



 \star At $\sqrt{s} \sim M_{{f Z}^0}$ the ${f Z}^0$ diagram dominates.

 $\begin{array}{l} \mbox{BREIT-WIGNER formula for } {\rm e}^+ {\rm e}^- \rightarrow {\rm Z}^0 \rightarrow {\rm f} \overline{{\rm f}} \mbox{ (where } {\rm f} \overline{{\rm f}} \mbox{ is any fermion-antifermion pair)} \\ \mbox{centre-of-mass energy } \sqrt{s} = E_{\rm CM} = E_{e^+} + E_{e^-} \\ \mbox{σ({\rm e}^+ {\rm e}^- \rightarrow {\rm Z}^0 \rightarrow {\rm f} \overline{{\rm f}}$)} = g \frac{\pi}{E_e^2} \frac{\Gamma_{ee} \Gamma_{{\rm f} \overline{{\rm f}}}}{(E_{\rm CM} \cdot M_Z)^2 + \Gamma_Z^2/4} \\ \mbox{with } g = \frac{2J_Z + 1}{(2S_{e^+} + 1)(2S_{e^-} + 1)} \\ \mbox{giving} \\ \mbox{σ({\rm e}^+ {\rm e}^- \rightarrow {\rm Z}^0 \rightarrow {\rm f} \overline{{\rm f}}$)} = \frac{3\pi}{4E_e^2} \frac{\Gamma_{ee} \Gamma_{{\rm f} \overline{{\rm f}}}}{(\sqrt{s} \cdot M_Z)^2 + \Gamma_Z^2/4} \\ \\ \mbox{$= \frac{3\pi}{\sqrt{s}} \frac{\Gamma_{ee} \Gamma_{{\rm f} \overline{{\rm f}}}}{(\sqrt{s} \cdot M_Z)^2 + \Gamma_Z^2/4} \\ \end{array} } \end{array}$

★ Γ_Z is the TOTAL DECAY WIDTH, *i.e.* the sum over the partial widths for the different decay modes.

$$\Gamma_{Z} = \Gamma_{ee} + \Gamma_{\mu\mu} + \Gamma_{\tau\tau} + \Gamma_{q\overline{q}} + \Gamma_{\nu\overline{\nu}}$$

At peak of the resonance $\sqrt{s}=M_Z$

$$\sigma(\mathrm{e^+e^-}\!\rightarrow\!\mathrm{Z^0}\!\rightarrow\!\mathrm{f}\overline{\mathrm{f}}) = rac{12\pi}{M_Z^2}rac{\Gamma_{ee}\Gamma_{\mathrm{f}\overline{\mathrm{f}}}}{\Gamma_Z^2}$$

<u>NOTE:</u> There are a number of equivalent forms sometimes quoted in the textbooks, *e.g.*

$$\frac{12\pi M_Z^2}{\sqrt{s}}\frac{\Gamma_{ee}\Gamma_{\rm f\bar{f}}}{(s\text{-}M_Z^2)^2\text{+}M_Z^2\Gamma_Z^2}$$

In the limit that $\Gamma \ll M_Z$ these are all equivalent. (see Question 12 on the problem sheet)

Measurement of M_Z and Γ_Z



One subtle feature : the measurements have to be corrected for well-known QED effects due to radiation from the e^+e^- beams. This radiation has the effect of reducing the centre-of-mass energy of the e^+e^- collision which smears out the resonance.

 e^+ z^0 \bar{q} $e^ z^0$ q

(see Question 11 on the problem sheet)

M_Z measured with precision 2 parts in 10^5

★ To achieve this required a detailed understanding of the accelerator and astrophysics ! Tidal distortions of the earth by the moon cause the rock surrounding the accelerated to be distorted. The nominal radius of LEP changes by 0.15 mm compared to radius of 4.3 km. This is enough to change the centre-of-mass energy !

★ Also need a train timetable ! Leakage currents from the TGV rail via lake Geneva follow the path of least resistance... using LEP as a conductor.



Accounting for these effects (and many others):

$M_Z = 91.1875 \pm 0.0021 \, { m GeV}$

★ An incredible achievement and powerful test of our understanding of the Standard Model of particle physics.

Shape of measured Breit-Wigner distribution also gives:

$$egin{array}{rcl} \Gamma_Z &=& 2.4952 \pm 0.0023 \, {
m GeV} \ \sigma^0_{
m a \overline{a}} &=& 41.540 \pm 0.037 \, {
m nb} \end{array}$$

Number of Generations

★ So far only discussed 3 generations of fermions, *e.g.* $\{e^-, \mu^-, \tau^-\}$

★ What about a possible fourth generation ?

$$\begin{pmatrix} e^- \ d \\
u_e \ u \end{pmatrix}, \begin{pmatrix} \mu^- \ s \\
u_\mu \ c \end{pmatrix}, \begin{pmatrix} \tau^- \ b \\
u_ au \ t \end{pmatrix}, +?$$

★ The Z⁰ boson couples to ALL fermions, including neutrinos. Therefore the total decay width, Γ_Z has contributions from all fermions $m_f < M_Z/2$

$$\begin{split} \Gamma_{Z} &= \Gamma_{ee} + \Gamma_{\mu\mu} + \Gamma_{\tau\tau} + \Gamma_{qq} + \Gamma_{\nu\overline{\nu}} \\ \text{with } \Gamma_{\nu\overline{\nu}} &= \Gamma_{\nu_{e}\overline{\nu}_{e}} + \Gamma_{\nu_{\mu}\overline{\nu}_{\mu}} + \Gamma_{\nu_{\tau}\overline{\nu}_{\tau}} \end{split}$$

- ★ If there were an additional generation, it seems likely that the fourth generation neutrino would be light and, if so, would be produced at LEP, $e^+e^- \rightarrow Z^0 \rightarrow \nu \overline{\nu}$
- ★ Wouldn't observe the neutrinos directly, but could infer their presence from the effect on the Z⁰ resonance curve

At the peak of the ${
m Z}^0$ resonance $\sqrt{s}=M_Z$

$$\sigma^0_{
m far f} ~=~ rac{12\pi}{M_Z^2}rac{\Gamma_{ee}\Gamma_{
m far f}}{\Gamma_Z^2}$$

A fourth generation neutrino would INCREASE the Z^0 decay rate and thus increase Γ_Z . As a result one would observe a DECREASE the measured peak cross sections for the visible final states.

★ Measure the $e^+e^- \rightarrow Z^0 \rightarrow f\overline{f}$ cross-sections for all visible decay modes (*i.e.* all fermions apart from $\nu\overline{\nu}$)

EXAMPLES:



★ Have already measured M_Z and Γ_Z from the shape of the Breit-Wigner resonance. Therefore obtain $\Gamma_{\rm ff}$ from the peak cross-sections in each decay mode using

$$\sigma^0_{
m far f}~=~rac{12\pi}{M_Z^2}rac{\Gamma_{ee}\Gamma_{
m far f}}{\Gamma_Z^2}$$

Note, obtain Γ_{ee} from

$$\sigma^0_{ee} ~=~ rac{12\pi}{M_Z^2} rac{\Gamma^2_{ee}}{\Gamma^2_Z}$$

★ Can relate the partial widths to the measured TOTAL width (from the resonance curve)

$$\Gamma_{Z} ~=~ \Gamma_{ee} + \Gamma_{\mu\mu} + \Gamma_{ au au} + \Gamma_{qq} + N_{
u}\Gamma_{
u
u}$$

where N_{ν} is the number of neutrinos species and $\Gamma_{\nu\nu}$ is the partial width for a single neutrino species.

The difference between the measured value of Γ_Z and the sum of the partial widths for all visible final states gives the "invisible" width.

Γ_Z	2494.8 ± 4.1 MeV
Γ_{ee}	83.7 ± 0.2 MeV
$\Gamma_{\mu\mu}$	84.0 ± 0.3 MeV
$\Gamma_{ au au}$	83.9 ± 0.4 MeV
$\Gamma_{\mathbf{q}\overline{\mathbf{q}}}$	1745.3 ± 3.5 MeV
$N_ u \Gamma_{ u u}$	497.3 ± 3.5 MeV

In the Standard Model calculate

	$\Gamma_{ u u}$	=	$167{ m MeV}$
therefore	$N_{ u}$	=	$\underline{497.3\pm3.5}$
			167
		=	2.98 ± 0.02

3 generations of light neutrinos ($m_
u < rac{M_{
m Z^0}}{2}$)

 \Rightarrow Probably only 3 GENERATIONS !



In addition:

- ★ $\Gamma_{ee}, \Gamma_{\mu\mu}, \Gamma_{\tau\tau}$ are consistent ⇒ universality of the lepton couplings to the Z⁰
- ★ $\Gamma_{q\overline{q}}$ is consistent with the expected value which assumes 3 COLOURS - yet more evidence for colour

Parity Violation in \mathbf{Z}^{0} Decays

EXAMPLE: $e^+e^- ightarrow \mu^+\mu^-$

- ★ Parity is conserved in the strong and EM interactions
- ★ Parity is maximally violated in the WEAK charged current interaction.

W-bosons mainly couple to LH particles

What about the WEAK neutral current ?

- ★ Parity IS violated in the WEAK neutral current
- ★ The Z⁰ is a 'mixture' of a parity conserving VECTOR field and a parity violating 'W-like' field.

Perform a 'parity' violation experiment analogous to that of Handout VI page 13 : FORWARD-BACKWARD asymmetry



If parity is conserved the number of μ^- observed in FORWARD hemisphere will be equal to number observed in BACKWARD hemisphere



For data recorded at $\sqrt{s} = M_{\mathbf{Z}^0}$:

 $A_{FB} = 0.0171 \pm 0.0010$

i.e. a small but statistically significant non-zero asymmetry \Rightarrow PARITY VIOLATED

EXPLANATION

 $Z^0 f \overline{f}$ coupling is a mixture of VECTOR and VECTOR – AXIAL-VECTOR couplings.

$$rac{g}{\cos heta_W} rac{1}{2} \gamma^\mu (C_V - C_A \gamma^5)$$

Mixture determined by WEAK MIXING ANGLE θ_W . For leptons

$$C_V = (1 - 4 \sin^2 \theta_W)$$

 $C_A = 1$

The measured asymmetry:



Small asymmetry implies $(1-4 \sin^2 heta_{W}) \sim 0$.

By measuring the asymmetry measure $\sin^2 \theta_W$

ALL LEP
$$A_{FB}$$
:
 $\sin^2 \theta_W = 0.23099 \pm 0.0053$
LEP $\rightarrow M_{70}$ and $\sin^2 \theta_W$



★ e⁺e⁻ collisions Ws produced in pairs.
 ★ In Standard Model 3 possible diagrams for e⁺e⁻ → W⁺W⁻





Cross section sensitive to presence of the Triple Gauge Boson vertex $Z^0W^+W^-$ <u>1996-2000</u>, LEP operated above the threshold for W^+W^- production $\sqrt{s} > 2M_W$



Cross section agrees with Standard Model prediction. Confirmation of the existence of the $Z^0W^+W^-$ vertex

$\mathbf{W^+W^-}$ Decay at LEP

In Standard Model: $W^{\pm}\ell\nu$ and $W^{\pm}q\overline{q}$ couplings are equal.



EXPECT (assuming 3 COLOURS)

★ Br(W[±] → qq) = $\frac{2}{3}$ ★ Br(W[±] → $\ell\nu$) = $\frac{1}{3}$ QCD corrections ~ $(1 + \alpha_s/\pi)$ ➡

 $Br(W^{\pm} \rightarrow q\overline{q}) = 0.675$



W^+W^- Events in OPAL



W-Boson Mass and Width

- ★ Unlike $e^+e^- \rightarrow Z^0$, W boson production at LEP is not a resonant process
- $\star M_{W}$ measured differently.
- **★** Reconstruct invariant mass distribution.
- **\star** Use measured lepton/jet momenta and energies to estimate $M_{\mathbf{W}}$ on an event-by-event basis



In the Standard Model the W-boson decay width is given by:

$$\begin{split} \Gamma(W^- \to e^- \overline{\nu}_{\rm e}) &= \frac{g_w^2 M_{\rm W}}{48\pi} \\ &= \frac{G_{\rm F} M_{\rm W}^3}{6\sqrt{2}\pi} \end{split}$$

From μ -decay : $G_F = 1.166 \times 10^{-5} \text{ GeV}^{-2}$. From LEP measure : $Mw = 80.423 \pm 0.038 \text{ GeV}$. Therefore predict partial width

$$\Rightarrow \Gamma(W^- \to e^- \overline{\nu}_{\rm e}) = 227 \,{
m MeV}$$

Total width is the sum over all partial widths:

W^{-}	\rightarrow	$e^-\overline{ u}_{ m e}$
W^{-}	\rightarrow	$\mu^-\overline{ u}_\mu$
W^{-}	\rightarrow	$ au^-\overline{ u}_ au$
W^{-}	\rightarrow	$d ar{\mathrm{u}}$
W^{-}	\rightarrow	$s\overline{ extbf{c}}$

Consequently, $\underline{\text{IF}}$ the W-coupling to leptons and quarks is equal, and there are 3 colours

$$egin{array}{rcl} \Gamma &=& \sum_i \Gamma_i = (3+2 imes 3) \Gamma(W^- o e^- \overline{
u}_{
m e}) \ &pprox & 2.1 \ {
m GeV} \end{array}$$

Compare with measured value (LEP) $2.1 \pm 0.1~{
m GeV}$

★ Universal coupling strength

★ Yet more evidence for colour !

(see Question 13 on the problem sheet)



Now have 5 precise measurements of fundamental parameters of the Standard Model

★
$$\alpha_{em}$$

★ G_{F} =(1.16632±0.00002)×10⁻⁵ GeV⁻²
★ M_{W} = (80.423±0.038) GeV
★ $M_{Z^{0}}$ = (91.1875±0.0021) GeV
★ $\sin^{2}\theta_{W}$ = 0.23143±0.00015

In the Standard Model, ONLY 3 are independent.

Their consistency is an incredibly powerful test of the Standard Model of Electroweak Interactions !

This (in)consistency is the subject of the first part of the last lecture (HANDOUT VIII)